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Remote sensing of ocean sediment volume reverberation

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NAVAL POSTGRADUATE SCHOOL
Monterey, California

THESIS

REMOTE SENSING OF OCEAN SEDIMENT
VOLUME REVERBERATION

by

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December 1986

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Co-Advisor Alan B. Coppens

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19. ABSTRACT (continued)

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Remote Sensing of Ocean Sediment Volume Reverberation

by

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requirements for the degree of

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ABSTRACT

An experimental study was performed to establish a technique for measuring the volume reverberation from ocean sediments. Two types of sediments (aggregate and fine sand) were used in this study. The inhomogeneity within the sediment caused considerable sample-to-sample fluctuation in the scattered waveform. This fluctuation was removed by spatial averaging to obtain a mean value over the sampling area. A approximate model for volume reverberation from sediments was developed for an acoustic pulse with an exponential decay. The results are promising. Combining the model and the experimental results, the volume scattering coefficient obtained for the aggregate is 0.0624 $\pm$ 0.007 m^{-3} and for fine sand is 0.0413 $\pm$ 0.007 m^{-3}. The latter result is close to the coefficient obtained from a cloud-of-small-spheres model for wavelengths much greater than the particle size.

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The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

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I. INTRODUCTION

In hydrography, the character of the bottom should be determined for nautical charting, particularly in harbors, anchorage areas or other areas where the bottom characteristic is a significant factor to be considered for navigation safety. Conventional sampling methods, using clamshell snappers (Umbach, 1976), are used to define the characteristics of the bottom surface layer. It is tedious and time consuming, especially in off-shore geologic investigations. If some kind of theory or model existed to remotely classify the sediments, the task could be carried out easier and faster. Moreover, this ability would permit nautical charts to contain much more information.

In the ocean bottom, the magnitude and nature of the sound scattering are functions of both the particle size of the bottom and surface (bottom) relief (Mckinney and Anderson, 1964). The sound echo from sediments is subject to three types of reflecting or scattering (Clark, Proni, Seem, Tsai, 1985) :

1) coherent reflection from the water-sediment interface; the signal amplitude will be approximately that given by spherical spreading of the wave front from the image source modified by the plane wave reflection coefficient (Clay, 1966),
2) incoherent or statistically variable scattering from the surface irregularities of the sediment, and
3) incoherent scattering from within the volume of the sediment caused by the acoustically irregular matrix of the sediment.

Items 1 and 2 arise from the surface of the sediments and item 3 from the sound pulse penetrating into the sediment volume and then being scattered back to the transducer by the granular matrix of the sediment. Since different sediments have different acoustic matrices, they have different volume reverberation characteristics and there should exist a mathematical relationship between sediment properties and the volume reverberation.

The major goal of this experiment was to establish a fundamental laboratory procedure for the remote sensing of ocean sediment volume reverberation. This was to be accomplished by accurately measuring the properties of a pulse reflected from the

sediment. In application, since the reflected sound pulse is received by the same transducer, i.e., "monostatic sonar", our discussion is restricted to "back-reflection" and "backscattering".

II. BACKGROUND

Bradshaw (1981) used Monterey #31 fine sand, the same material used in this experiment, to study the sound propagation into a fast bottom medium. In his study, air bubbles were removed from within the sediment based on heating the water sand system. Bleach was added at a ratio of one-half gallon bleach to 70 gallons of water plus sand in order to control biologic growth. The physical properties, such as density, porosity, speed of sound, reflecton coefficient etc., were measured. Kosnik (1984) used a high pressure water jet to remove the air bubbles from the water/sand mixture. However, no volume scattering measurements were made by either investigator.

Morse and Ingard (1968) give a theoretical derivation on incoherent scattering. Under the assumptions that : 1) the scattering objects are quite small compared with wave length λ, 2) the dimensions of scattering region are much larger than λ, 3) the scatterers are all spheres, and 4) the scatterers are populated sparsely and no mutiple scattering existed, the incoherently scattered intensity I_{is}, per unit incident intensity I_i, at angle θ to the incident wave, for frequency $\omega/2\pi$, is

$$I_{is}/I_i = N V \frac{(2\pi)^{1/2}}{9} K^4 a^6 |\gamma_K + \gamma_\rho \cos\theta|^2 \qquad (2.1)$$

$$(\frac{1}{8} K^2 a^2 \sin^2(1/2)\theta) \exp(-2K^2 a^2 \sin^2(1/2)\theta)$$

where N is the total number of scatterers within unit volume, K is the wave number for the mixture, a is the radius of scatterers. Furthermore, for monostatic sonar, the volume scattering coefficient for unit volume can be reduced as

$$s_v = N (2\pi)^{1/2} K^6 a^8 |\gamma_K - \gamma_\rho|^2 \qquad (2.2)$$

where

$$\gamma_K = \frac{K_n - K_o}{K_o}$$

$$\gamma_\rho = \frac{3\rho_n - 3\rho_o}{2\rho_n - \rho_o}$$

and κ_n is the compressibility of the scatterer, κ_o is the compressibility of the fluid, ρ_n is the density of the scatterer and ρ_o is the density of fluid.

For a small ($ka << 1$) rigid sphere, the backscattering cross section is given (Urick, 1983) as

$$\sigma = 2.8\,(\pi a^2)(K a)^4$$

Note that, as a single sphere, it must be a single scattering. The scattering coefficient for unit volume can be obtained as

$$s_v = N \sigma \qquad (2.3)$$

Both theories are not very appropriate for the real ocean sediment volume reverberation. However, these are the only two theories available. The backscattering of sound from the ocean bottom has been studied for many years, but unfortunately no papers were found to discuss the volume reverberation of ocean sediments.

III. DESCRIPTION OF VOLUME REVERBERATION

As sound propagates in a fluid, part of the sound is intercepted and reradiated by inhomogeneites in the fluid. The reradiation of sound is called scattering. The total of the scattering contributions from all the scatterers is called reverberation (Urick, 1983).

Volume reverberation is defined as sound scattered back to the transducer by scattering centers in the volume of the sea (National Defense Research Commitee, 1969). Volume reverberation may be considered as a blending of large number of echoes. It has been studied mostly in the Deep Scattering layer , a region of high biological activity. Reverberation level, in decibels, is used to measure volume reverberation. Consider a directional projector in an ocean containing a large number of volume scatterers (Figure 3.1). Let the axial intensity at unit distance be I_0. At a distance r where there is a volume element dV of volume scatterers, the incident intensity is

$$I_i = I_0 / r^2$$

The scattered intensity 1 m from the volume dV is

$$dI_s(1) = I_i \, s_v \, dV$$

where s_v is the volume scattering coefficient. The scattered intensity back at the receiver is

$$\begin{aligned} dI_s(r) &= I_i \, s_v \, dV / r^2 \\ &= (I_0 / r^4) \, s_v \, dV \end{aligned}$$

and the scattered intensity from all scatterers contributing to the scattered intensity at time t is

$$I_s(r) = (I_0 / r^4) \, s_v \, V$$

where V is the total volume contributing for the geometry of Figure 3.1 calculated by (Urick, 1983)

$$V = \Omega \, r^2 \, c\tau / 2$$

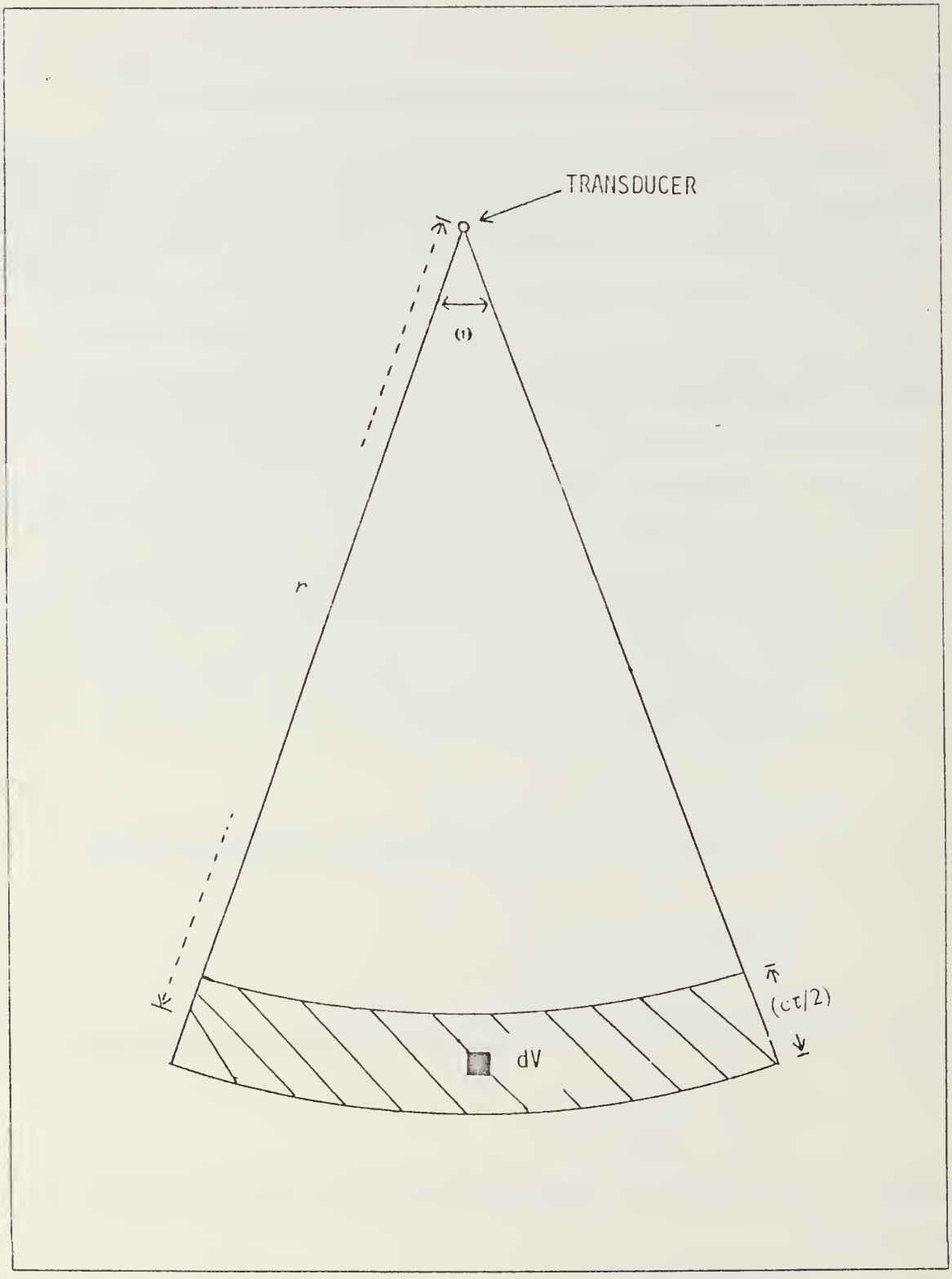

Figure 3.1 Portion of ocean scattering.

where Ω is the solid angle of the sound beam, τ is the pulse length and c is the sound speed, so

$$I_s(r) = (I_0 r^{-2}) s_v \Omega c\tau/2$$

The reverberation level is

$$RL = 10 \text{ LOG } I_s(r)/I_{ref}$$
$$= SL - TL + S_v + 10 \text{ LOG } (\Omega c\tau/2)$$

where TL is the transmission loss for spherical spreading 20LOG(r) and S_v is the scattering strength for unit volume 10LOG(s_v). In Deep Scattering Layer studies, this reverberation level equation is sufficient, because the received pulse is regarded as totally coming from volume reverberation, i.e. negligible reflection and surface scattering. Furthermore, the derivation of V is based on a square acoustic pulse. But for a real transducer, the square pulse is transformed into a pulse with an exponential rise, a flattened top and an exponential decay. The sound pulse reflected from the sediment and received by the transducer combines coherent reflected, incoherent scattering from the surface and volume reverberation.

Let a transducer located in the water send out a sound pulse to a smooth water air interface. The received echo waveform is purely reflection. If the water interface is rough, then the received echo waveform includes both reflection and surface scattering. Since sound energy is scattered by the rough surface, the received waveform amplitude is reduced. Consider first-order scattering and suppose that the surface roughness is the same for every position. The amplitude of the combined sound wave (reflected and scattered) is reduced proportional to the purely reflected wave amplitude. In Figure 3.2(a), the solid line represents an ensemble of reflected waveform, and the dashed line represents an ensemble of reflected and scattered waveform.

The contributions to a pulse reflected from a sediment surface is shown on Figure 3.2(b). The dashed line is the contribution by reflection and surface scattering; again, only first order scattering is considered. The dotted line includes volume reverberation. The level of the signal is raised above that of a dashed line because of energy returned from within the sediment. In particular, the tail decays more slowly than for reflection from the water/air interface. This is the significant feature of sediment volume reverberation that we are after in this paper.

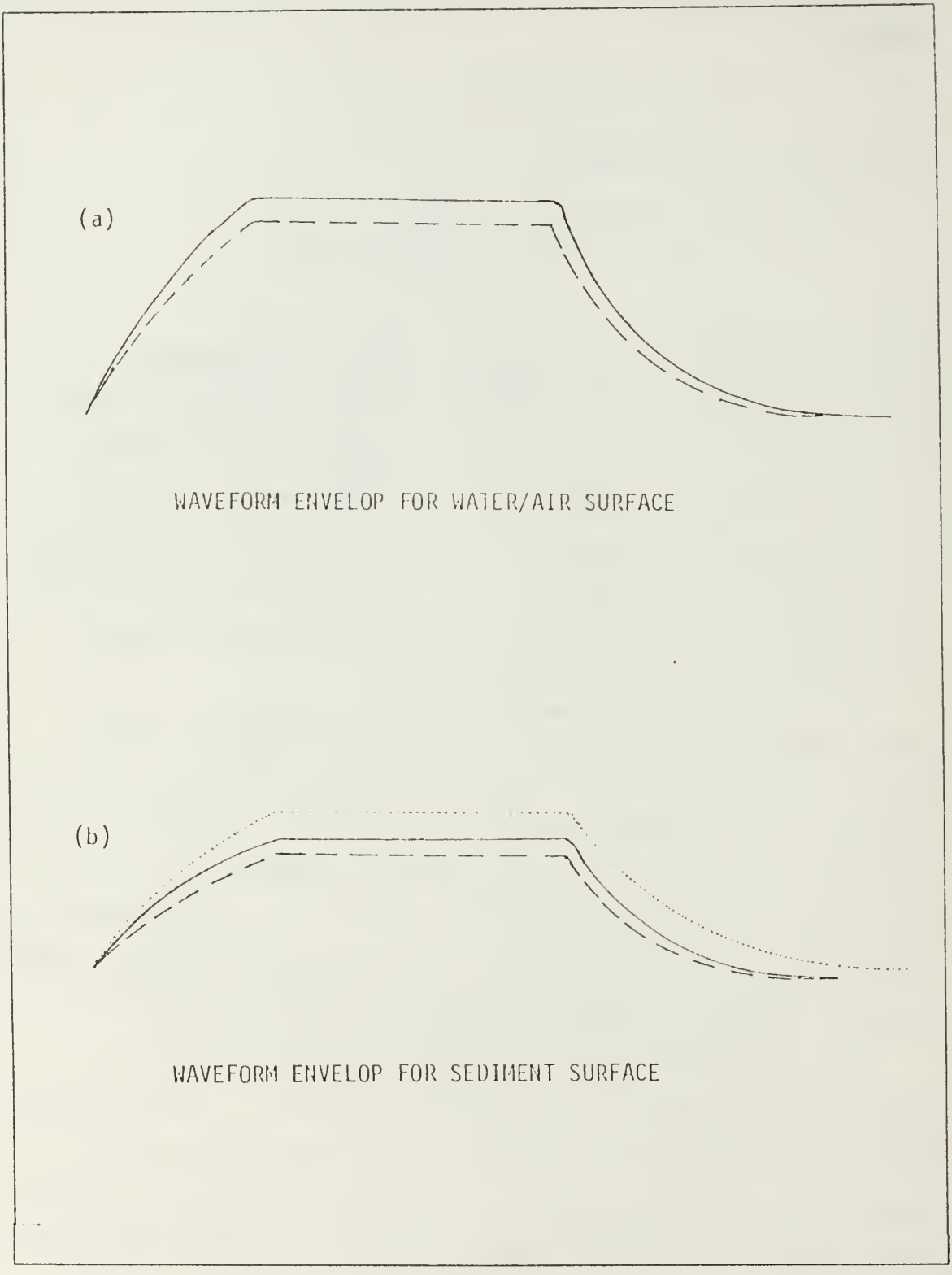

Figure 3.2 Theoretical echo waveform for water and sediment.

Two alternative assumptions have to be made for reflection from the sediment surface : either 1) the surface scattering is negligible compared with volume reverberation, or 2) if it is not negligible, it must have the same amplitude factor as discussed in Figure 3.2(b).

According to these assumptions, if a sediment echo is subtracted from the water echo it will give a measure of the volume reverberation in the sediment (Figure 3.3). The decaying tail of the echo reflected from the smooth water/air interface is an exponential decay,

$$V_W(t) = V_o e^{-\delta t}$$

where $V_W(t)$ is the received voltage at time t, δ is the decay constant, V_o is a constant voltage, and t is the time starting from the beginning of decay. If we assume the sediment echo also decays exponentially, then we will obtain a similar function

$$V_S(t) = V'_o e^{-\eta t}$$

where $V_S(t)$ is the received voltage from sediment at time t and η is a decay constant. If V_W and V_S are both normalized to the same initial value K, the difference becomes

$$V_V(t) = K(e^{-\eta t} - e^{-\delta t}) \qquad (3.1)$$

If both ηt and δt are much less than unity,

$$V_V(t) = K(\eta - \delta)t \qquad t << 1/\eta \text{ and } 1/\delta$$

This initial decay is linear and depends on the difference δ-η.

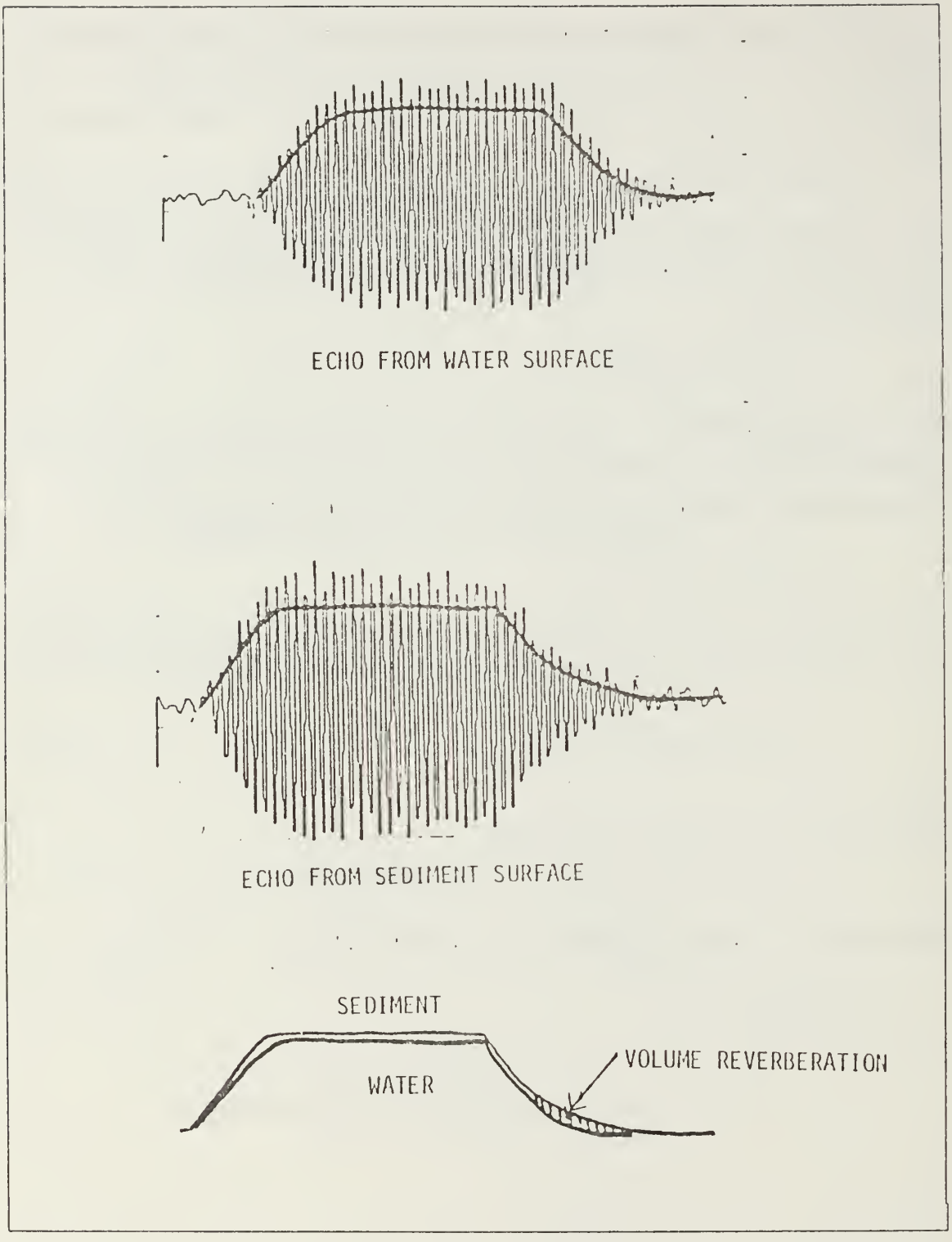

Figure 3.3 Real echo waveform displayed on CRT.

IV. EXPERIMENT DESIGN

A. MATERIAL AND TANK SELECTED

Fresh (tap) water, #30 Monterey fine sand and Monterey Aquarium #2 for a rough gravel sediment were the media used in the experiment. The grain size of #30 fine sand varies from 0.15 mm to 0.7 mm (Bradshaw, 1981) with an average size 0.3 mm. The Aquarium #2 has a mean size 5.3 mm (Diaz, 1986). The sand water mixture was repeatedly stirred to remove air bubble trapped while transferring the sand to different tanks.

Initial experiments were conducted in the NPS anechoic tank to measure the reflection from the water/air surface, with the transducer located at different depth. The second tank, a wooden tank measuring 80 cm x 80 cm x 60 cm, was constructed to hold about 30 cm of aggregate. This tank was lowered and suspended 85 cm below the water/air surface of the anechoic tank. A third tank, a steel glass tank, measuring 70 cm x 70 cm x 60 cm was filled with 24 cm of fine sand or aggregate with 36 cm of water above.

B. ELECTRONIC EQUIPMENT

A schematic drawing of the equipment is shown in Figure 4.1. Except a high pass filter, all components were off-the-shelf. General Radio model 1310 oscillator with a frequency of 182.0 kHz was fed simultaneously into a Hewlett-Packard 5233L frequency counter, and a General Radio Type 396-A tone burst generator was used to generate a 16 cycle pulse. Signal output from Hewlett-Packard HP 467-A amplifier was fed through a Datasonic Transmit Receive (T/R) switch and a small 21 to 28 kHz high pass filter, then into the F-41 transducer. The F-41 transducer was discussed in detail by both Borchardt (1985) and Diaz (1986). Signals returned from the sediment were amplified 20 dB by a Hewlett-Packard 465-A pre-amplifier, then passed through a Spencer-Kennedy Laboratories, Inc. model 302 variable electronic filter (set at 135 kHz high pass) to eliminate low frequency noise before being passed to the digital and analog oscilloscopes.

The waveform displayed on 3091 Nicolet Digital Oscilloscope was sampled and sent as a stream of characters to the computer. To reduce manual operations on the Nicolet 3091 during the experiment, a HP-3421A Data Acquisition and Control Unit

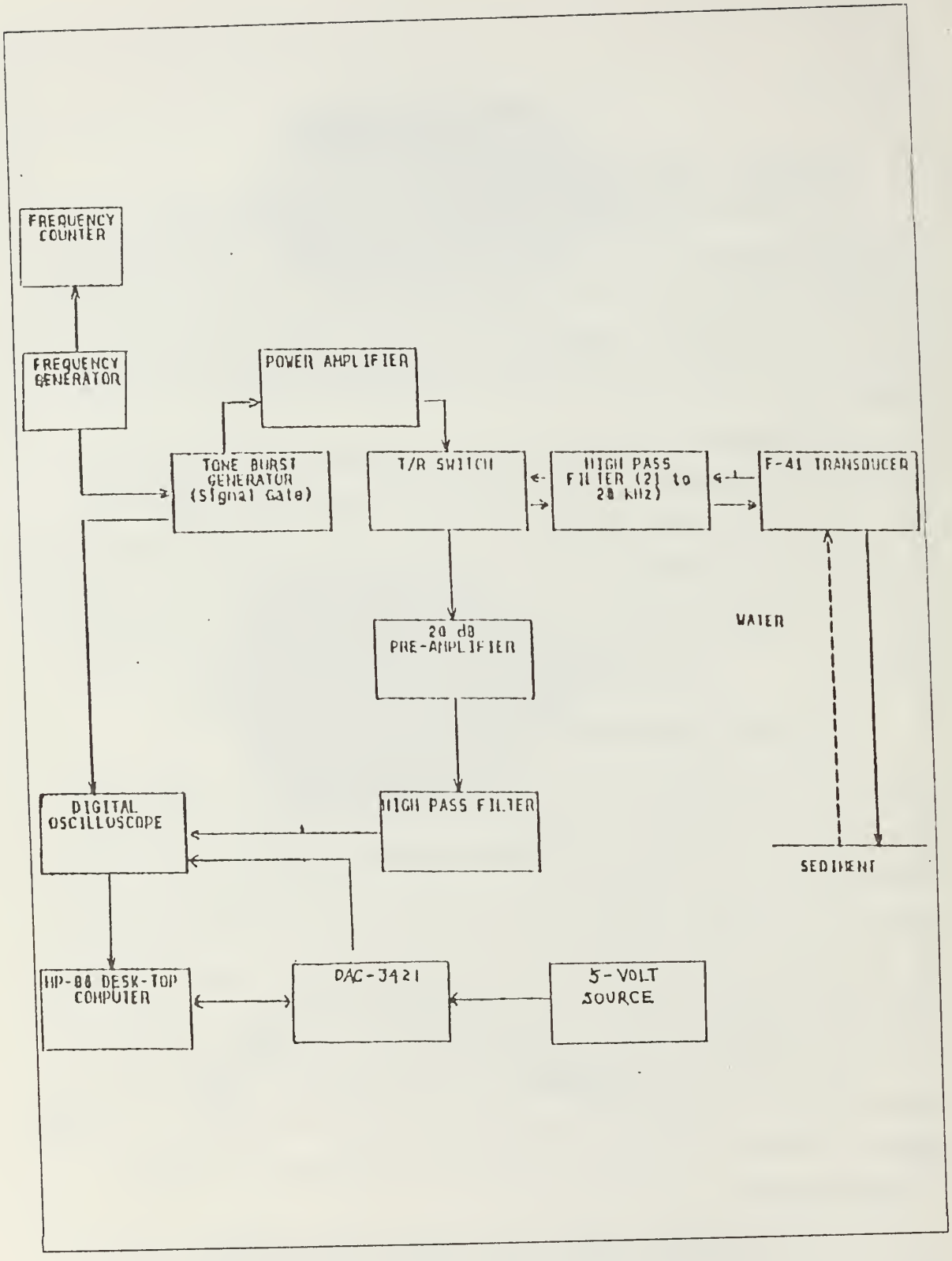

Figure 4.1 Schematic of equipment.

was adopted to receive commands from a HP-86 computer and then automatically operate the Nicolet 3091. However, it was noticed that if the Nicolet 3091 was not "warmed up" enough, the DC-offset jumped up and down, and continual manual adjustment was needed. After 2 or 3 hours of running, it became stable and no further adjustment was required.

C. VERIFICATION OF MEASUREMENTS

No matter how deep the transducer is located below the water/air surface, as long as the transducer is level, the exponential decay of the tail should be the same. In Diaz's thesis, the measurements were inconclusive because the transducer was fixed at one position throughout the experiment. This was not adequate to prove the system functioned properly. To prove that the previous experiments were run properly and results were obtained correctly, a verification was attempted by measuring the reflection from the water/air interface with the same procedure, but with the transducer at various depths. Data set 20 (Figure 4.2) for the transducer 70 cm below the surface, gives a slope of -3.75×10^{-2} Np/μs. Data set 21 (Figure 4.3) was obtained by raising the transducer 15 cm and the slope is -3.77×10^{-2} Np/μs. Both results were close to the previous results obtained by Diaz (1986). After these two data sets were collected, a new transducer mounting was built and adopted to improve the experimental precision and operation ability. The transducer was leveled by a counter-weight on the new carriage. To ensure the system and operation worked properly, more locations were tried to obtain the decay constant of the water/air surface.

Data sets 23 and 24 were obtained at the same transducer depth, but seperated 40 cm horizontally. Data sets 24 and 25 were obtained at the same horizontal position but with 50 cm difference in depth. Data set 26 was acquired by changing 10 cm in both the depth and position from data set 25. Data sets 26 to 28 resulted from changing the depth from 70 cm to 30 cm below the water/air interface. The results of these experiments are listed in Table 1 and show consistencies between each other. Waveform ensembles of the tail for each data set are plotted on Figure 4.4 to Figure 4.9.

The average slope $-3.77 \pm 0.077 \times 10^{-2}$ Np/μs is smaller than $-3.84 \pm 0.14 \times 10^{-2}$ Np/μs which was measured in Diaz's thesis. Statistically, these two slopes are the same. The smaller standard deviation might suggest that the new carriage has achieved a better precision.

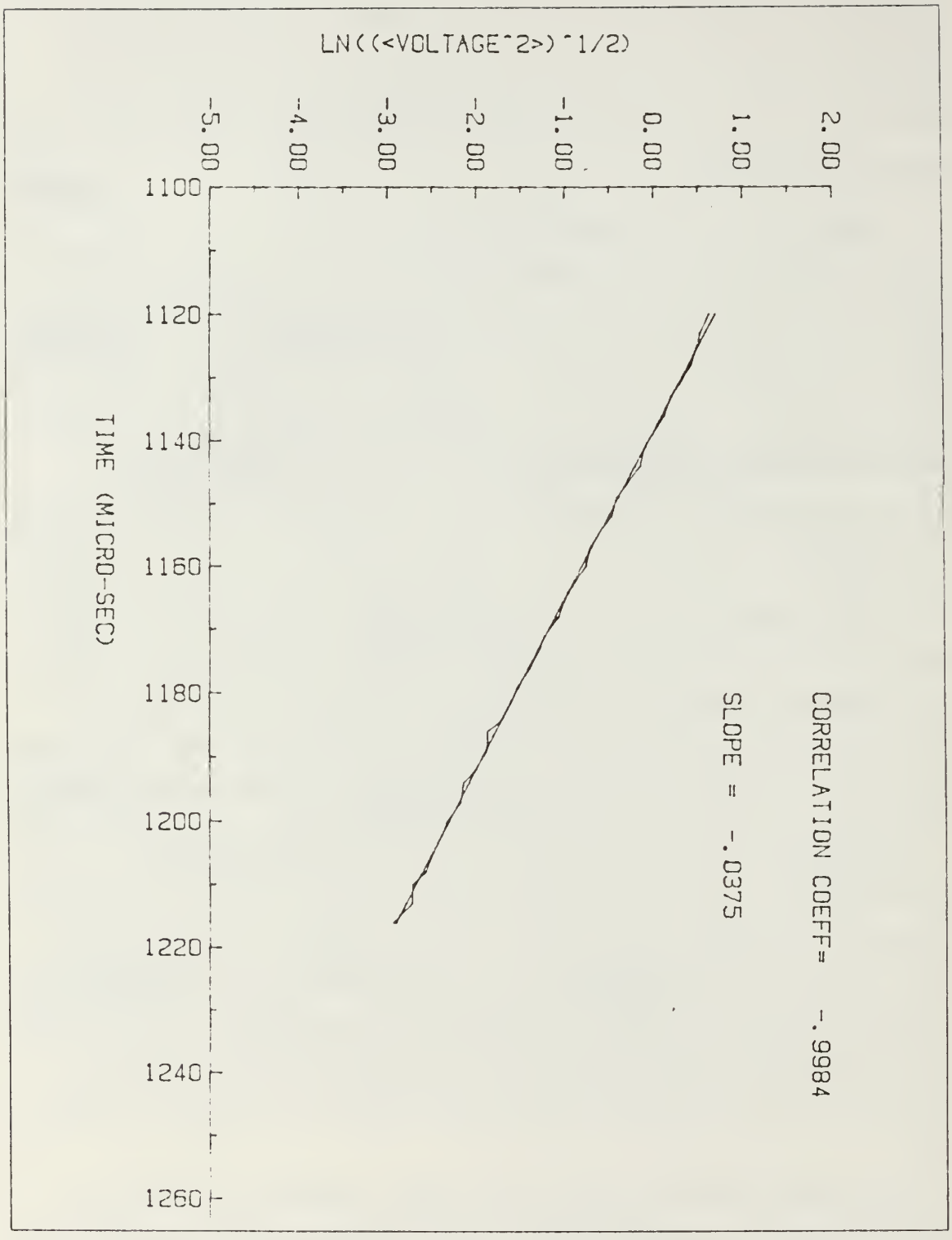

Figure 4.2 Decay envelope for reflection from water/air interface, transducer 70 cm below the surface (data set 20).

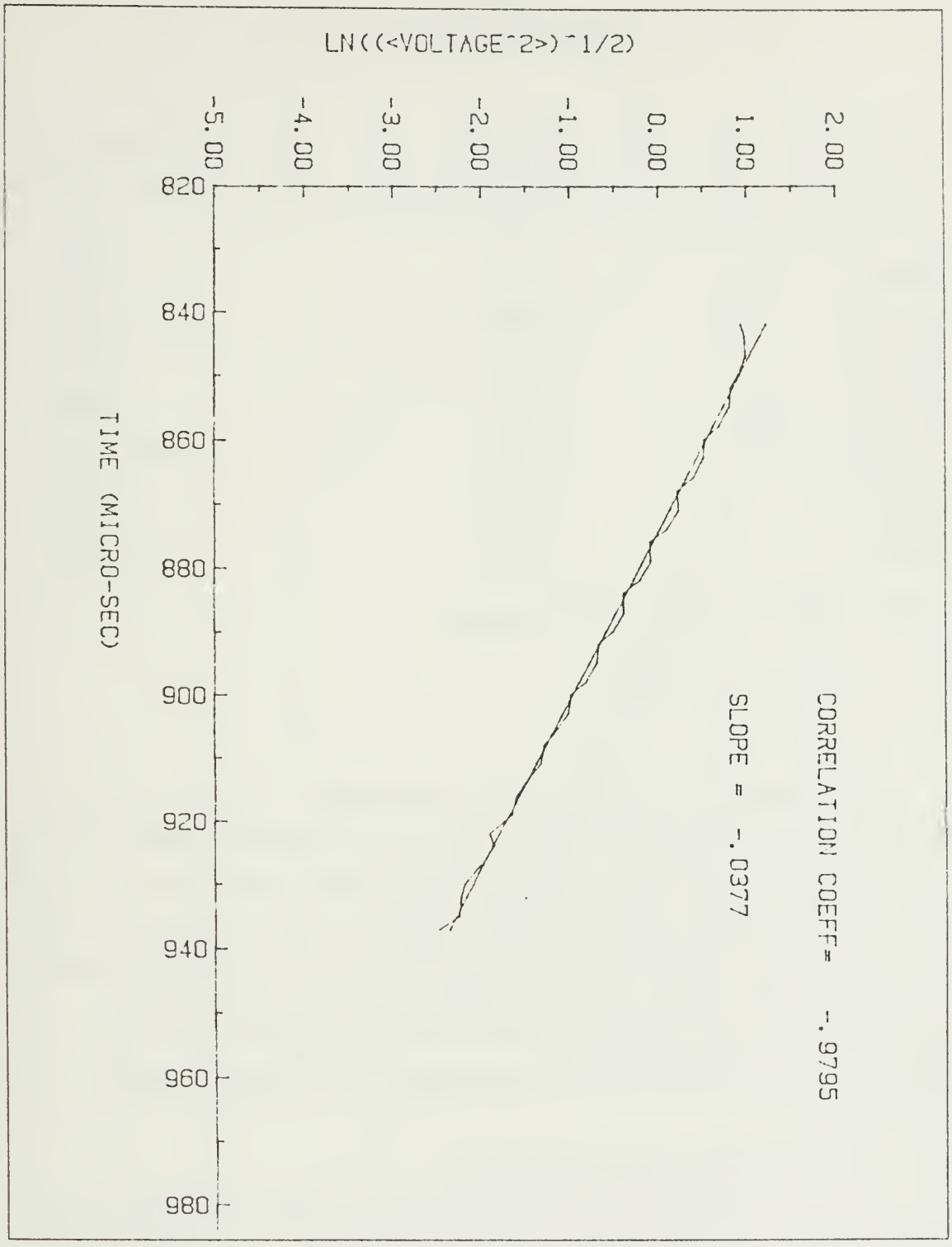

Figure 4.3 Decay envelope for reflection from water/air interface, transducer 55 cm below the surface (data set 21).

TABLE 1
WATER/AIR REFLECTION

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DATA20	-3.75	-0.9984
DATA21	-3.77	-0.9795
DATA22	-3.86	-0.9979
DATA23	-3.62	-0.9724
DATA24	-3.68	-0.9895
DATA25	-3.86	-0.9956
DATA26	-3.80	-0.9679
DATA27	-3.84	-0.9888
DATA28	-3.79	-0.9810

MEAN SLOPE = -3.77×10^{-2} Np/μs

$\sigma = 0.07 \times 10^{-2}$ Np/μs

After dealing with the water/air surface, the transducer was turned over and pointed downward toward the sediment which was contained within the 80 cm x 80 cm x 60 cm wooden tray. Different transducer positions were choosen. Data sets 31 to 33 were at the same depth, but horizontally 3 cm away from each other. The results show the waveform were totally inconsistant. Data sets 33 to 35 were at the same horizontal position but different depths; results were also inconsistant. Above results are presented on Table 2 and plotted on Figure 4.10 through Figure 4.14. So far, experiments reveal the lack of isotropic homogeniety of the volume contributes reverberation.

D. MEASUREMENT CONSIDERATION

During the course of these experiments some other effects were considered and studied to ensure that the experiment was working properly.

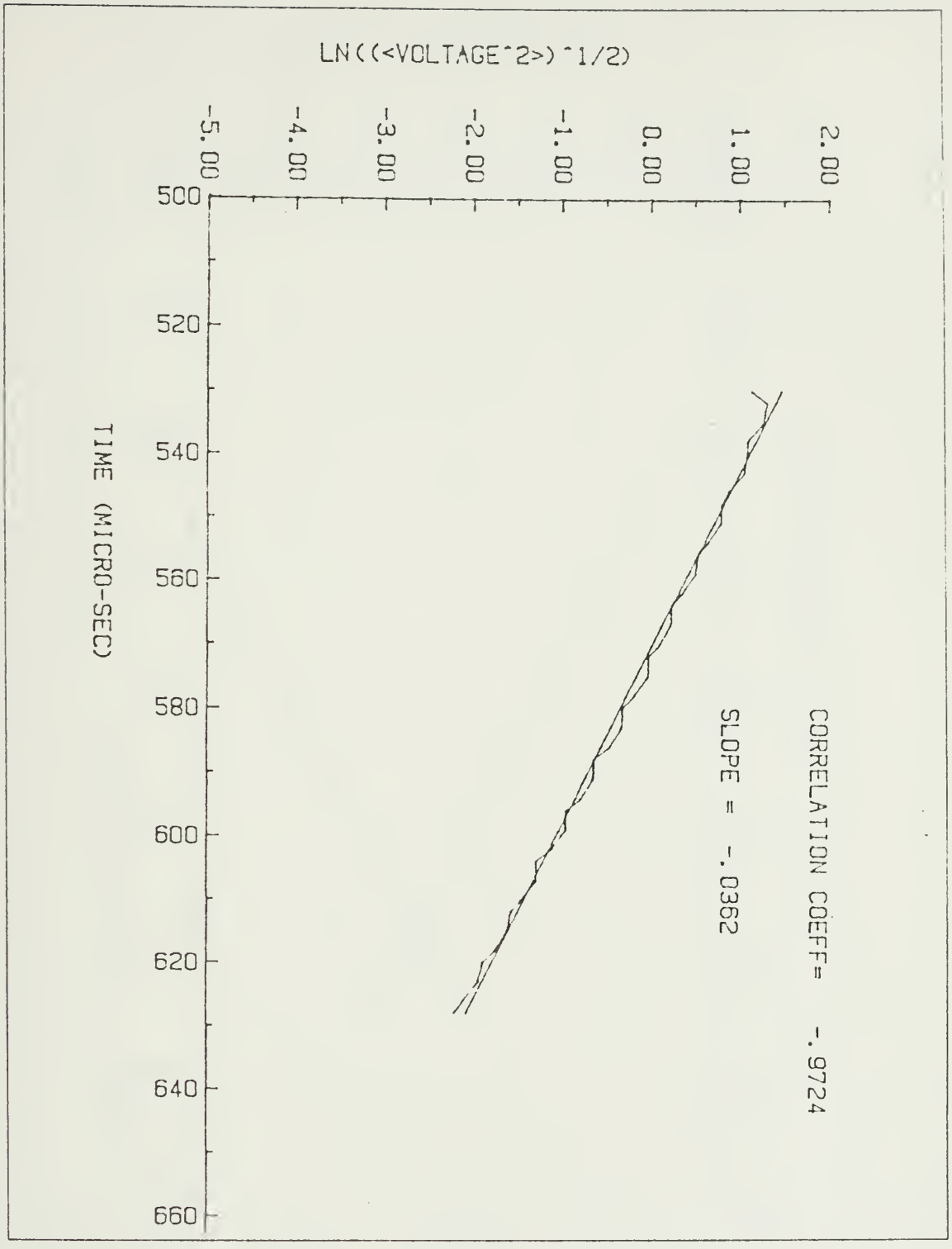

Figure 4.4 Decay envelope for reflection from water/air interface, transducer was 30 cm below surface (data set 23).

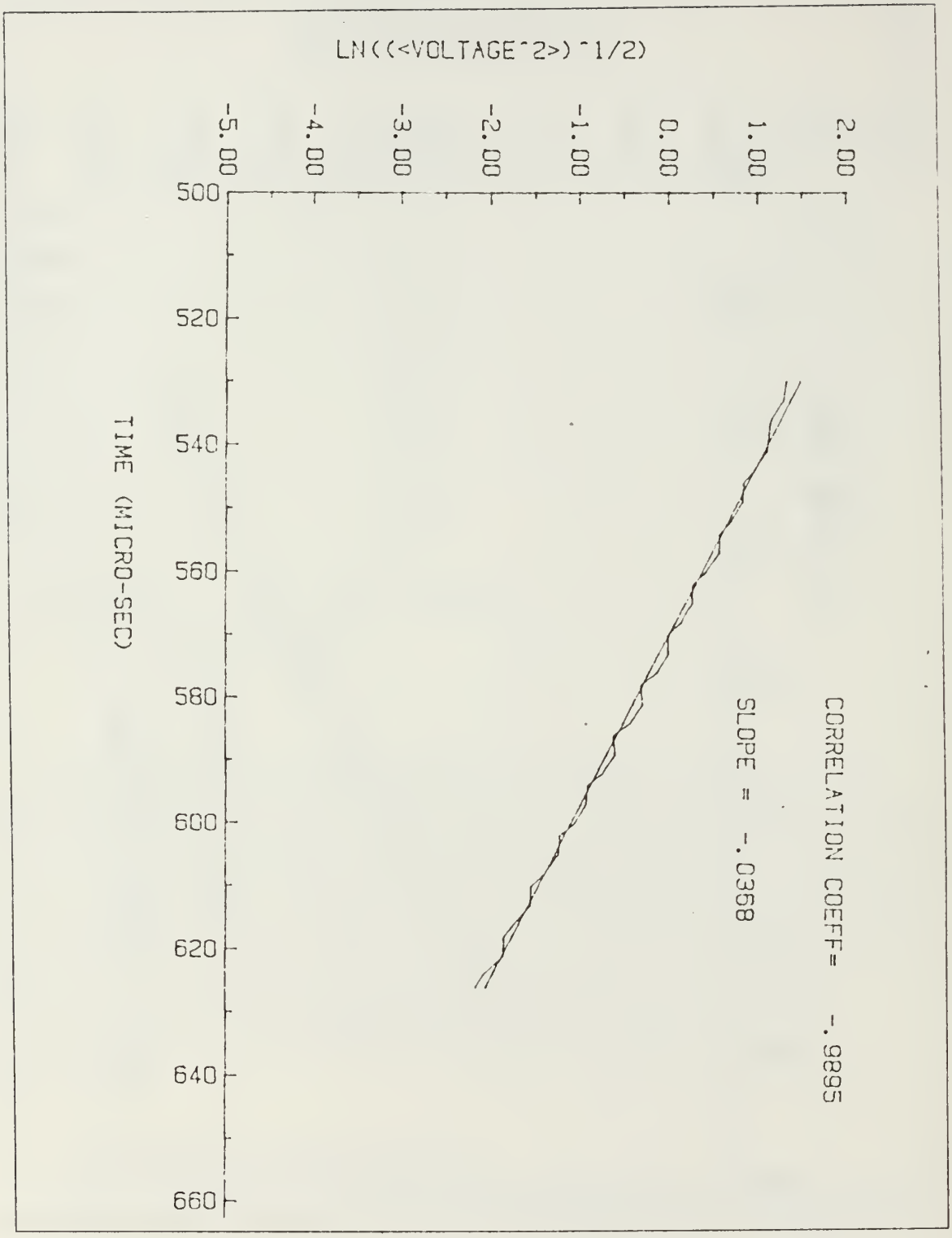

Figure 4.5 Decay envelope for reflection from water/air interface, trnsducer was 30 cm below surface (data set 24).

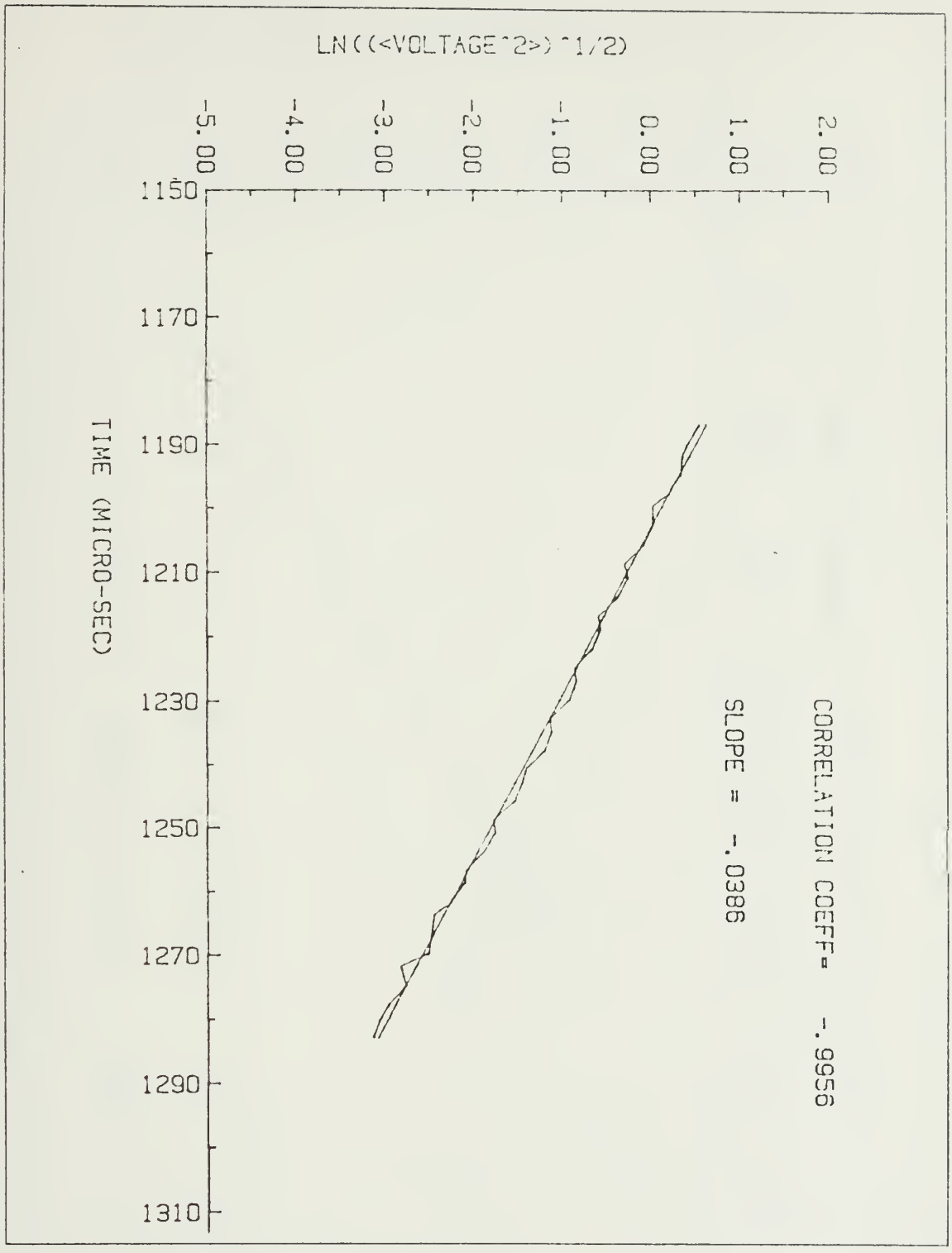

Figure 4.6 Decay envelope for reflection from water/air interface, transducer was 80 cm below surface (data set 25).

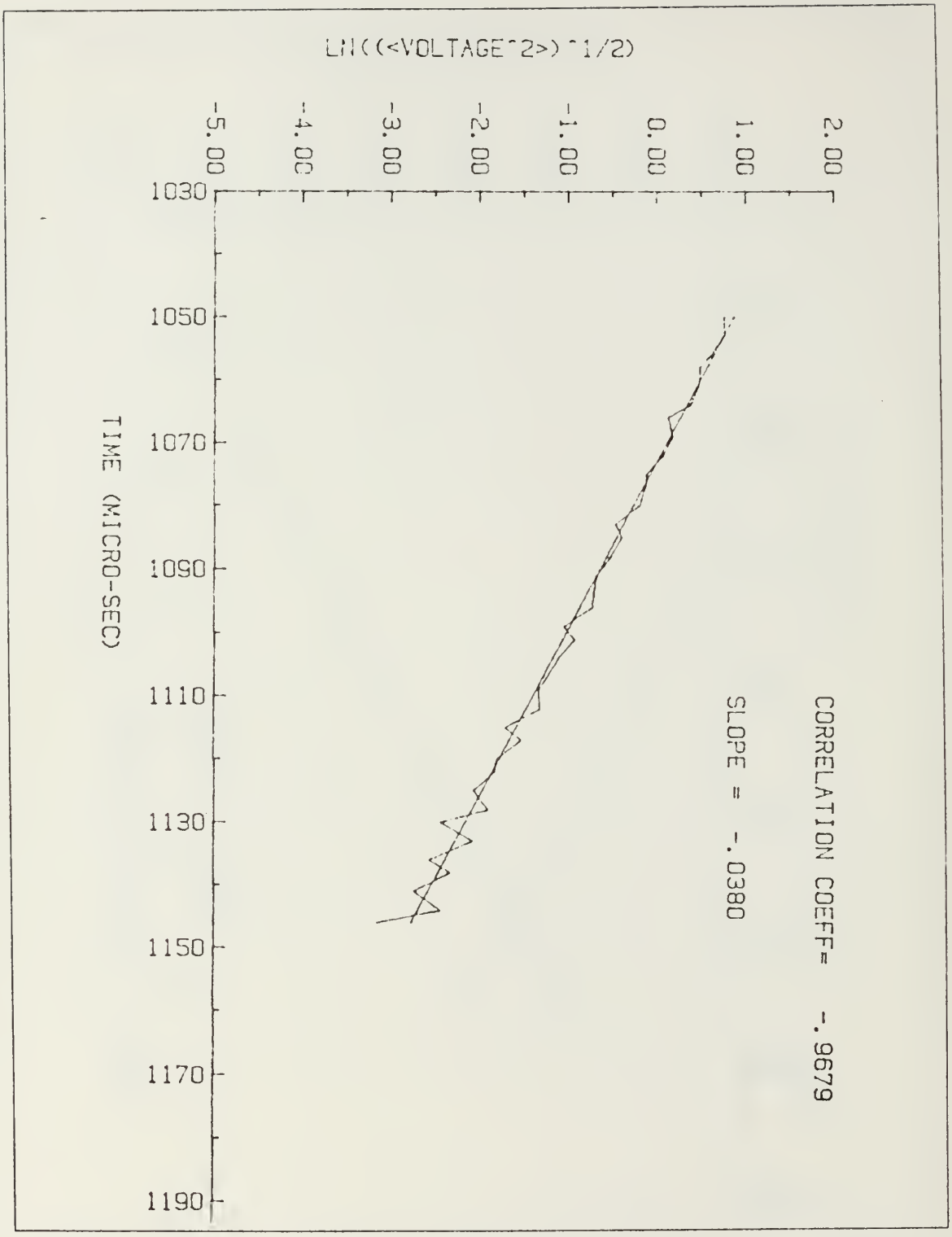

Figure 4.7 Decay envelope for reflection from water/air interface, transducer was 70 cm below surface (data set 26).

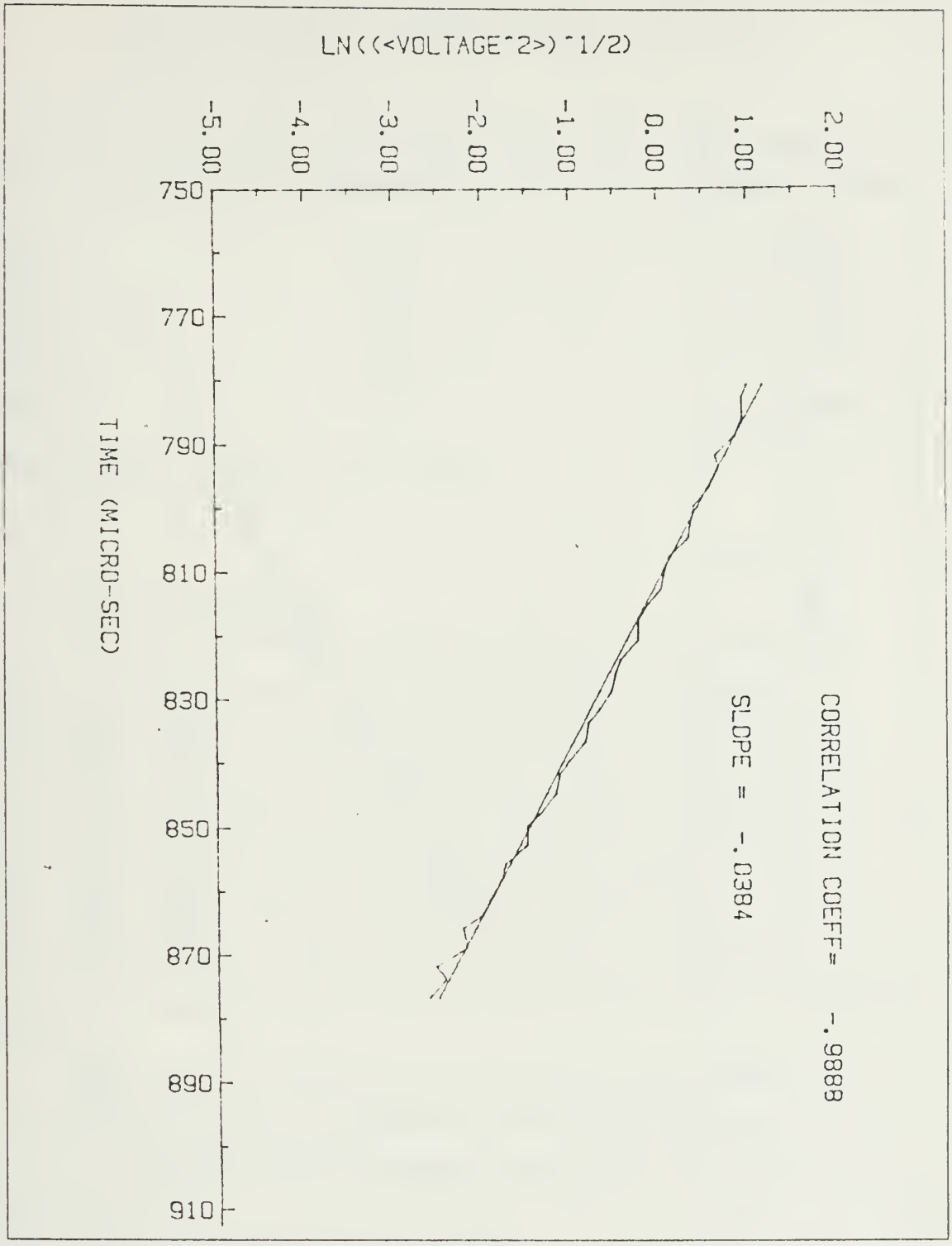

Figure 4.8 Decay envelope for reflection from water/air interface, transducer was 50 cm below surface (data set 27).

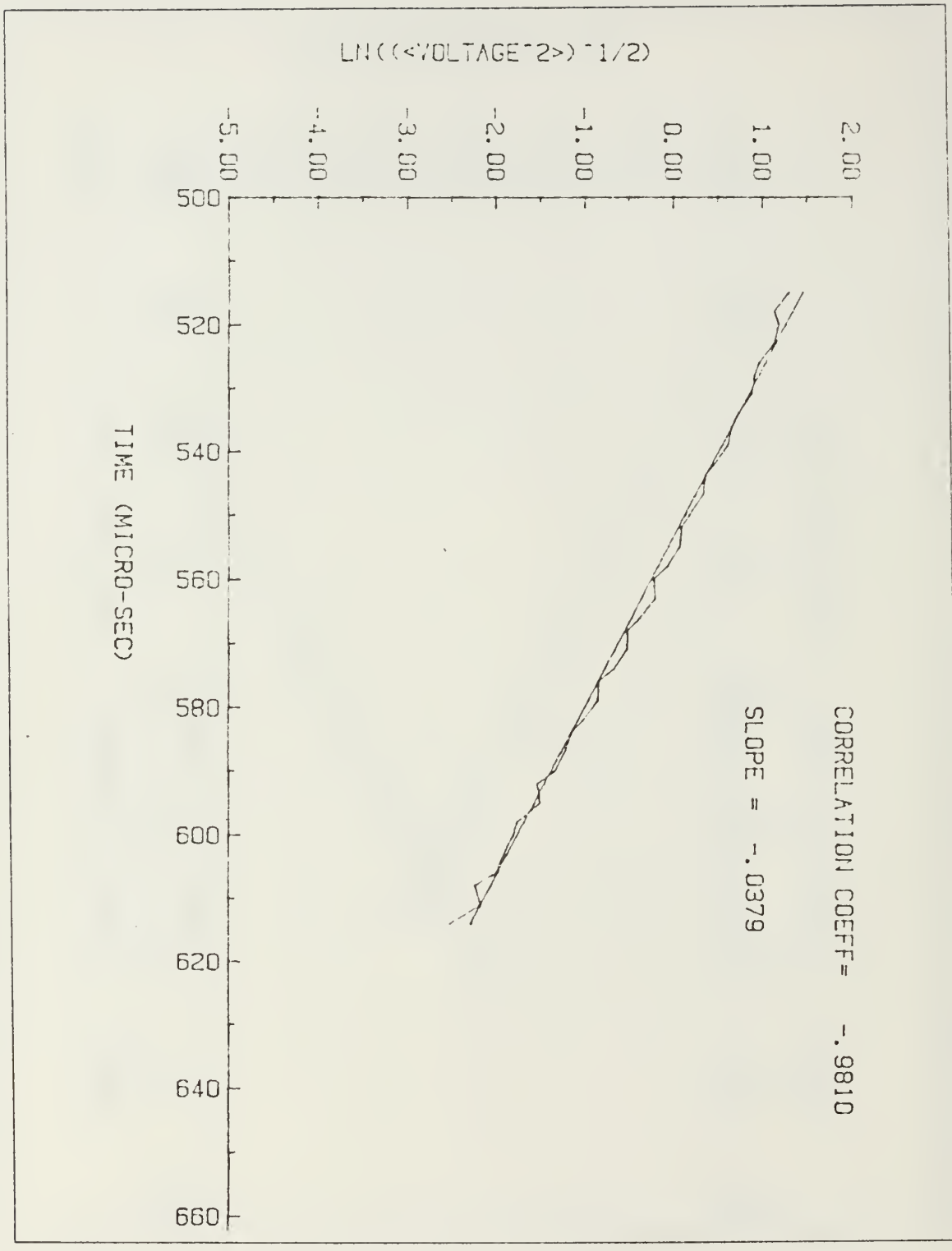

Figure 4.9 Decay envelope for reflection from water/air interface, transducer was 30 cm below surface (data set 28).

TABLE 2

SEDIMENT WATER REFLECTION AND SCATTERING

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DATA31	-2.20	-0.9138
DATA32	-2.98	-0.8908
DATA33	-1.94	-0.7838
DATA34	-3.06	-0.8174
DATA35	-2.90	-0.9844

MEAN SLOPE = -2.62×10^{-2} Np/μs

$\sigma = 0.86 \times 10^{-2}$ Np/μs

1. Effects of Sampling Rate

The sound signal being used was fixed at 182 kHz (5.5 μs period). The Nicolet 3091 digital oscilloscope has as its fastest sampling rate 1 μs which is inadequate to give a precise reproduction of the numeric waveform. However, observations have shown "jitter" in the triggering of the scope, so for consecutive pulses the scope would sample different parts of the waveform. To obtain an accurate waveform, a large number of waveform were sampled and averaged. If sufficient "jitter" is present, the voltage measured in a given bin should vary between the maximum and minimum voltage in the waveform in the vicinity of the corresponding time. Since the sine wave varies between minus and plus, the voltage values were squared before averaging in order to give an accurate representation of the waveform envelope.

To determine the maximum number of samples required for each data set (average waveform), the water/air interface was measured with different number of samples. The results showed that 50 samples for each data set were enough to give a true waveform.

2. Effects of Bottom Reflection Interference

For a 16 cycle signal with a frequency 182 kHz, the pulse length is 88 μs. Since the sound pulse emitted had a decay time of approximately 100 μs, the echo from

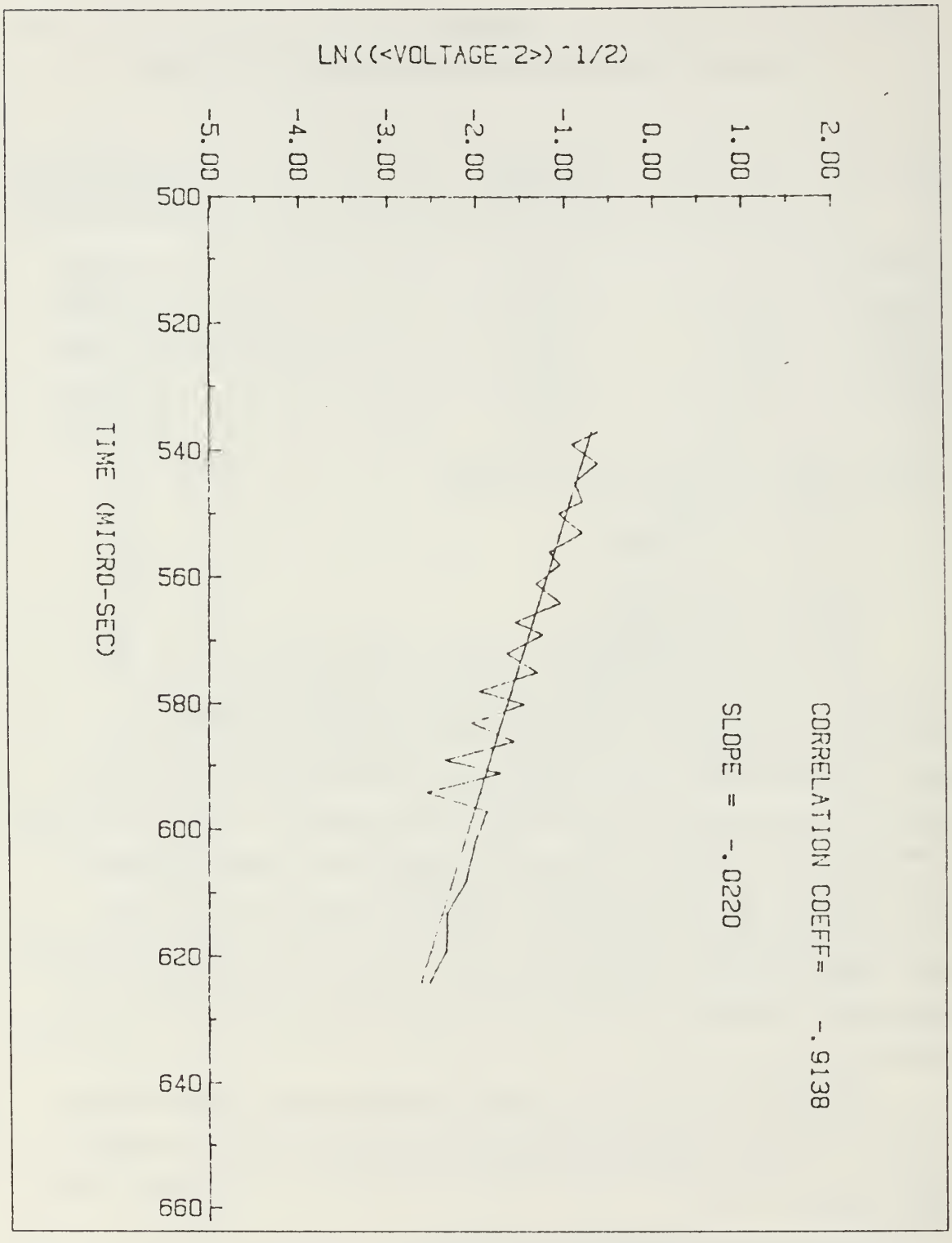

Figure 4.10 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 31).

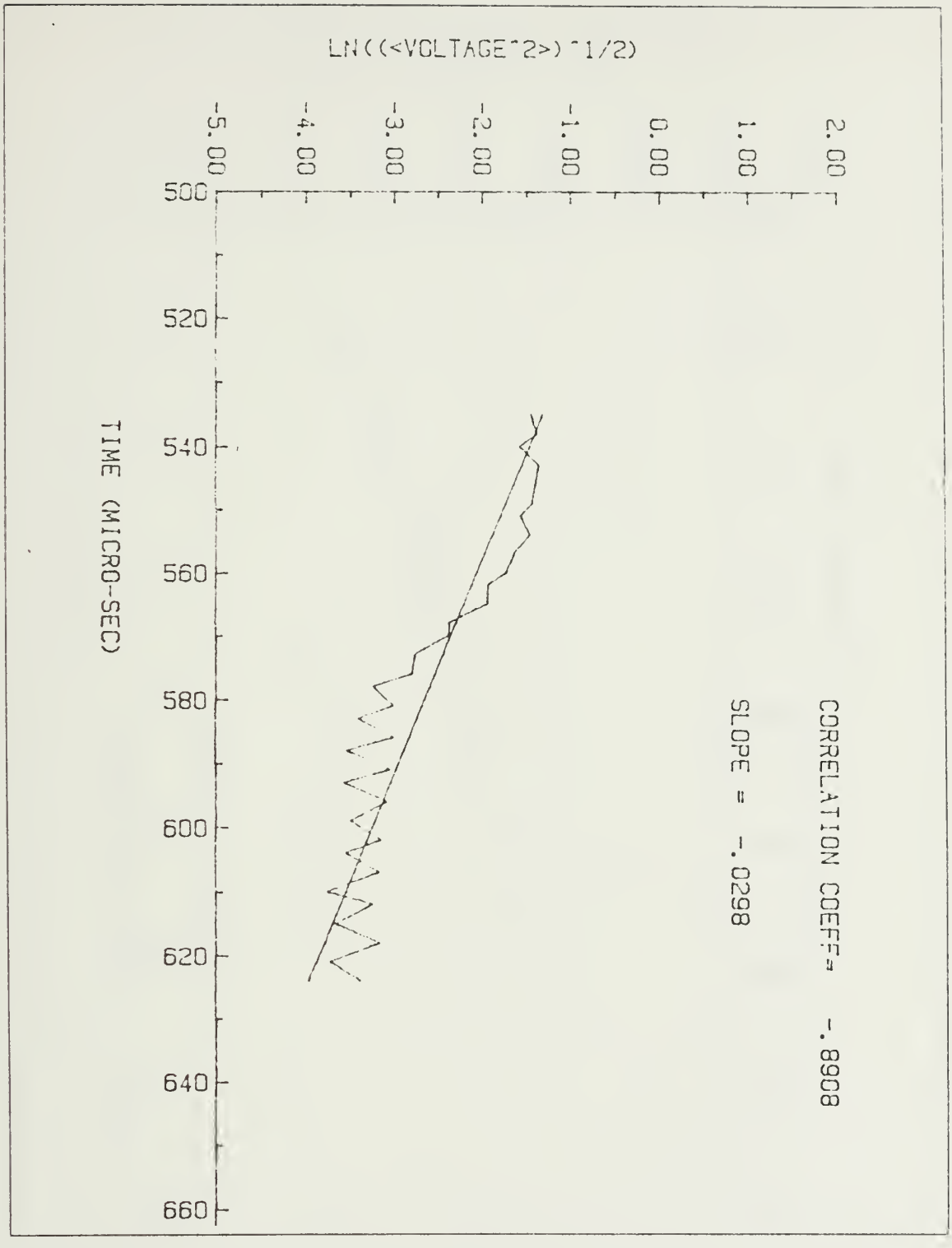

Figure 4.11 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 32).

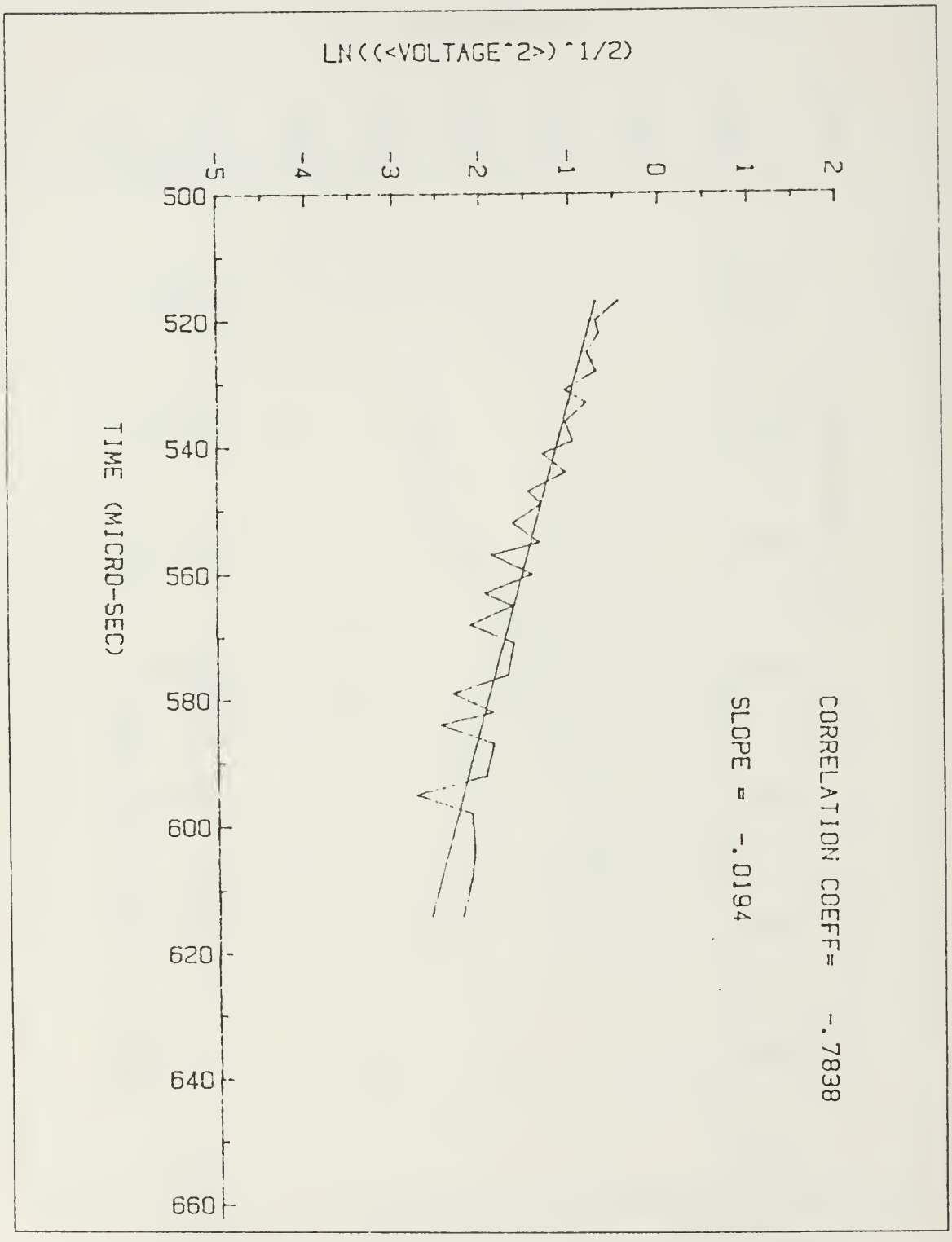

Figure 4.12 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 33).

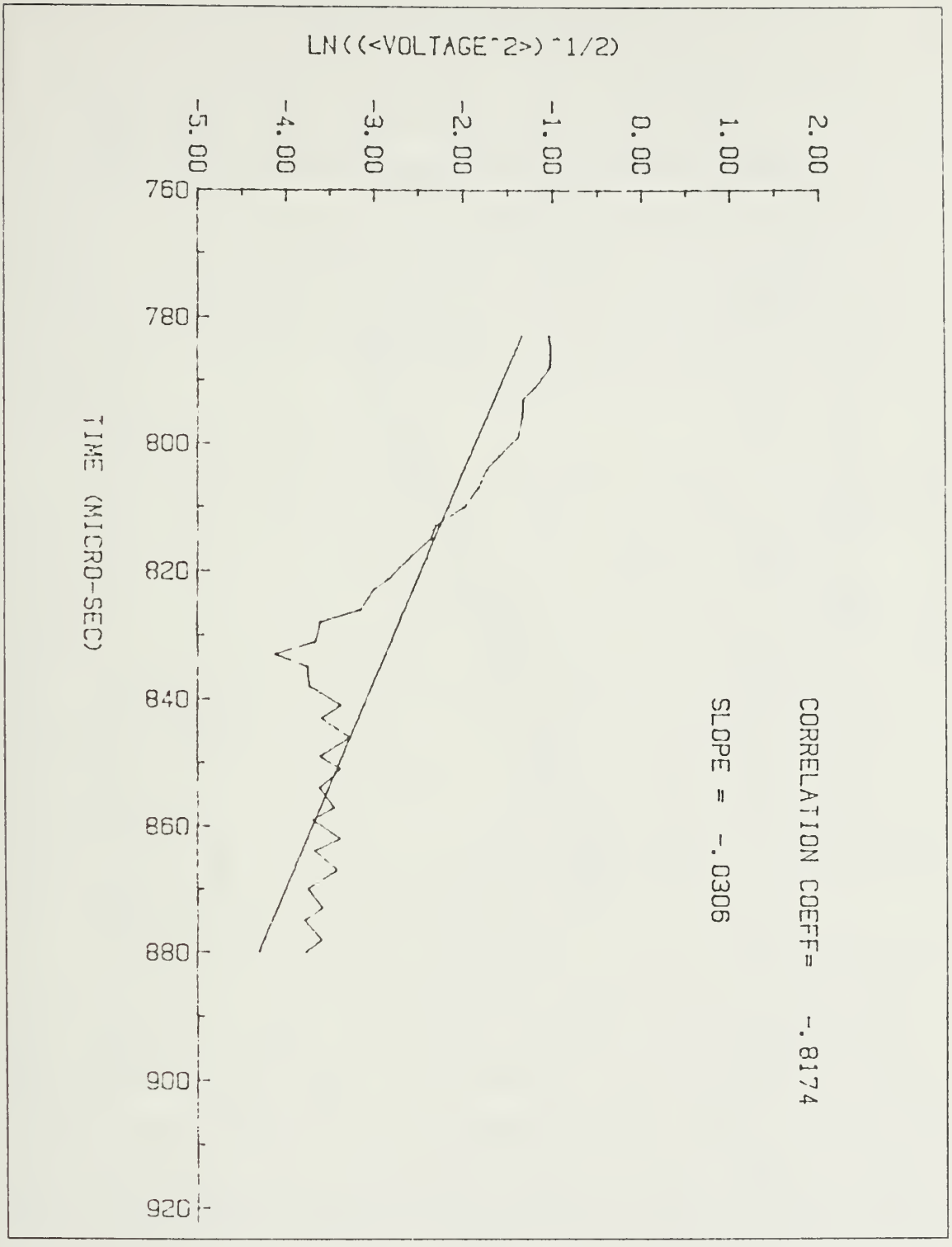

Figure 4.13 Decay envelope for reflection from aggregate/water interface, transducer was 50 cm above surface (data set 34).

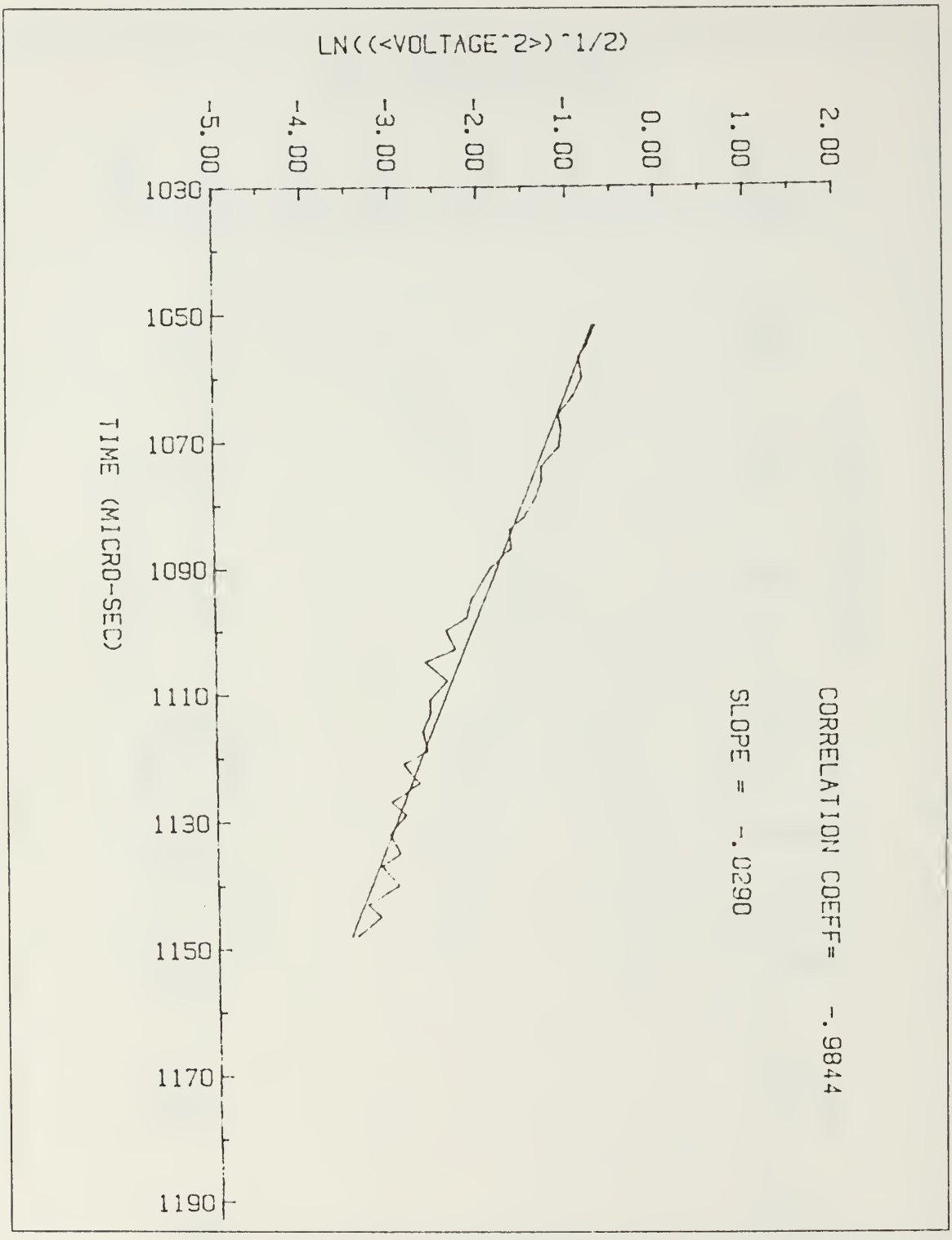

Figure 4.14 Decay envelope for reflection from aggregate/water interface, transducer was 70 cm above surface (data set 35).

the smooth water/air interface should also have the same decay time. Since the purpose of this project was to compare the decay portion of echos reflected from water and sediments, the waveform was sampled for a 100 μs interval from the begining of decay. The sound speed in the aggregate was measured to be 1555 m/s. For the fine sand, Bradshaw (1981) obtained the speed of sound to be 1610 m/s. Combining these sound speeds and the time interval 188 μs, the depth of sediment that contributes to the main echo is 14.6 cm for aggregate and 15.1 cm for fine sand. Interference caused by reflection from the bottom of the tank will not affect the experiment as long as the sand is thicker than 15.1 cm and the aggregate is thicker than 14.6 cm. Throughout our experiments, we kept both sediments more than 24 cm deep in the glass tank to avoid interference.

3. Effects of Near Field Interference

In the near field of a transmitter, the axial pressure exhibits strong interference effects (Kinsler, Frey, Coppens, Sanders, 1982). Thus, the sound field is irregular and does not fall off smoothly with distance as it does in the far field. To avoid measurements in the near field, an experiment was run to find the transition distance which separates the near field and far field. This distance is 20 cm from the transducer center. No problems should occur as long as the target is more than 20 cm from the transducer. In the glass tank, we placed the transducer 30 cm above sediment. The water/air interface measurement also gave a check that 30 cm distance is satisfied. Since a pulse moving in water at 1480 m/s, takes 405 μs to travel the 30 cm to the sediment interface and back, the 30 cm distance is long enough so that the transducer, which is on about 188 μs, stops ringing before the first echo from the sediment arrives.

4. Effects of Water/Air Interface Interference

Ideally, the transducer should be far enough away from all unwanted surfaces to avoid interference. As the transducer faces down and projects a major part of its energy to the sediment surface, some energy is transmitted to the water surface and reflected back toward the sediment. If the transducer is close to the water/air surface, the reflected energy will interfere with the transmitted energy. Restricted by the size of the glass tank, we had to locate the transducer close to the water surface. To test how important this interference could be, the water surface was agitated by fingers. The waveform displayed on both analog and digital oscilloscope was unchanged during the ruffling. It was concluded that this source of interference is negligible for this experiment.

5. Effects of Side Lobe

The half beamwidth (to the first null) for the F-41 transducer was measured to be 10.0°. For a 30 cm distance from sediment to the transducer, the sediment surface ensonified by the major lobe is a circle area with radius 5.3 cm. If the distance is 80 cm, the radius will be 14.1 cm. For both the glass tank and wood tank, if the transducer is located above the center of the tank, the major lobe will not produce interference caused by the sides of the tank.

The glass tank was too small to avoid the interference, if any, caused by the side lobe. To test how much the interference was, sediments outside the center 30 cm x 30 cm square area were disturbed and left in a very irregular surface. Waveforms returned from sediment were measured before and after the disturbance. Data set 51 (Figure 4.15) shows the waveform measured before the sediment was disturbed and data set 52 (Figure 4.16) shows the waveform after disturbance. By comparing the two waveforms, it is found that the F-41 trandsucer gave negligible side lobe interference in this experiment.

6. Effects of Sediment Inhomogeneity

Before the test findings on side lobe effects, we were bothered by the drastic changes on the waveform whenever the transducer was moved parallel to the smoothed aggregate surface. It was assumed that the waveform fluctuation was caused by the inhomogeneities of the aggregate. To prove this, we placed the transducer at a fixed position in the glass tank and repeatedly ensonified the aggregate. After each data set was acquired, the aggregate was disturbed and smoothed again. Ten sets of waveform data were obtained and each of them differed from the others.

It was thought the fine sand would be more homogeneous than aggregate and it might produce more consistant waveforms as the transducer was moved horizontally. Measurements made with the fine sand, however, showed that the waveform still fluctuated. After each data set was obtained from the smoothed fine sand, the transducer was moved horizontally to different position. All the transducer positions were at least 15 cm from the wall to avoid interference caused by reflection from the sides of tank. Also, the positions were at least a length of tranducer diameter from each other to avoid a waveform replication. A metal plate was set on top of the sand and the transducer was moved horizontally. As expected, the waveform on the oscilloscope was unchanged but totally different from sand.

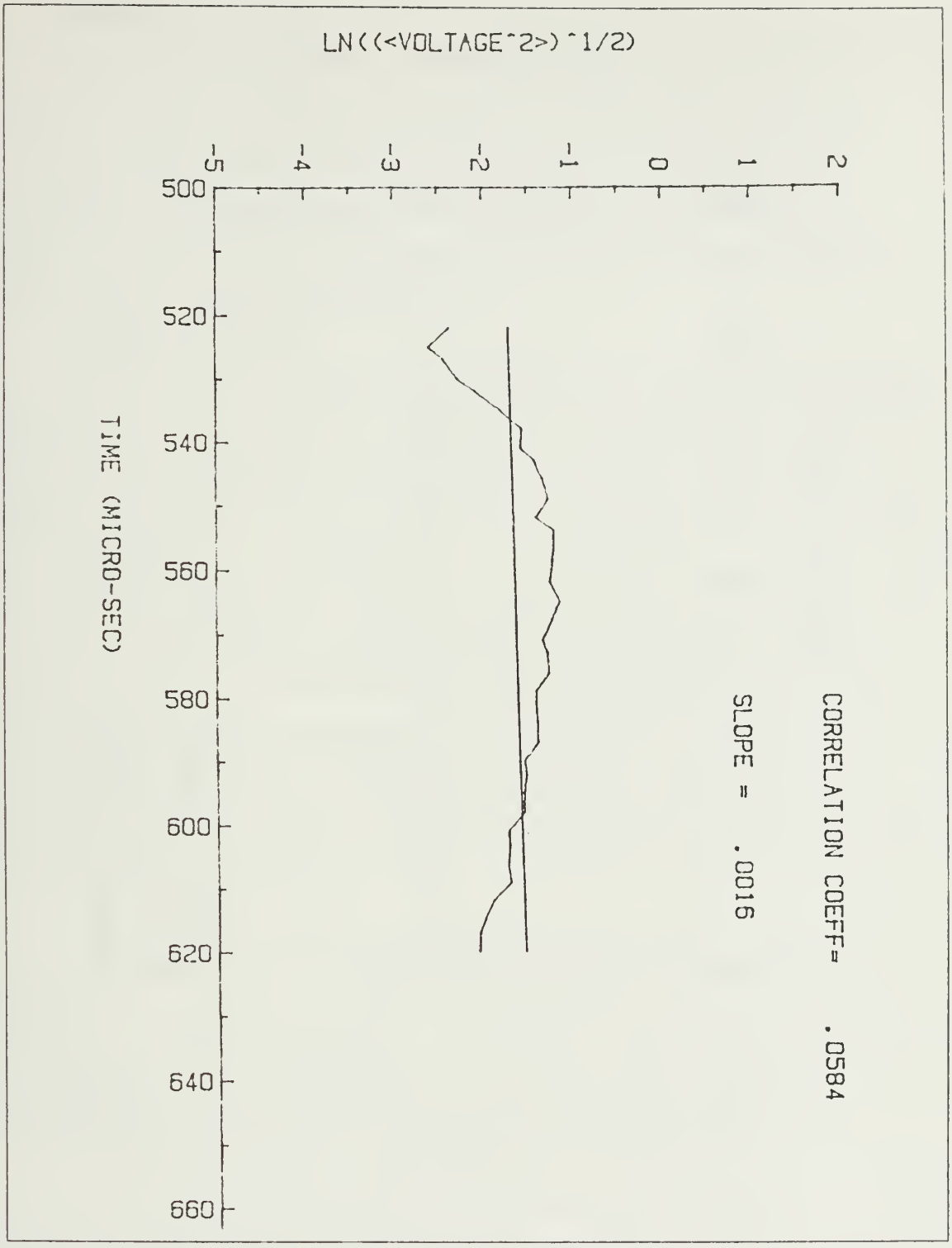

Figure 4.15 Decay envelope for reflection from aggregate/water interface in the glass tank (data det 5f).

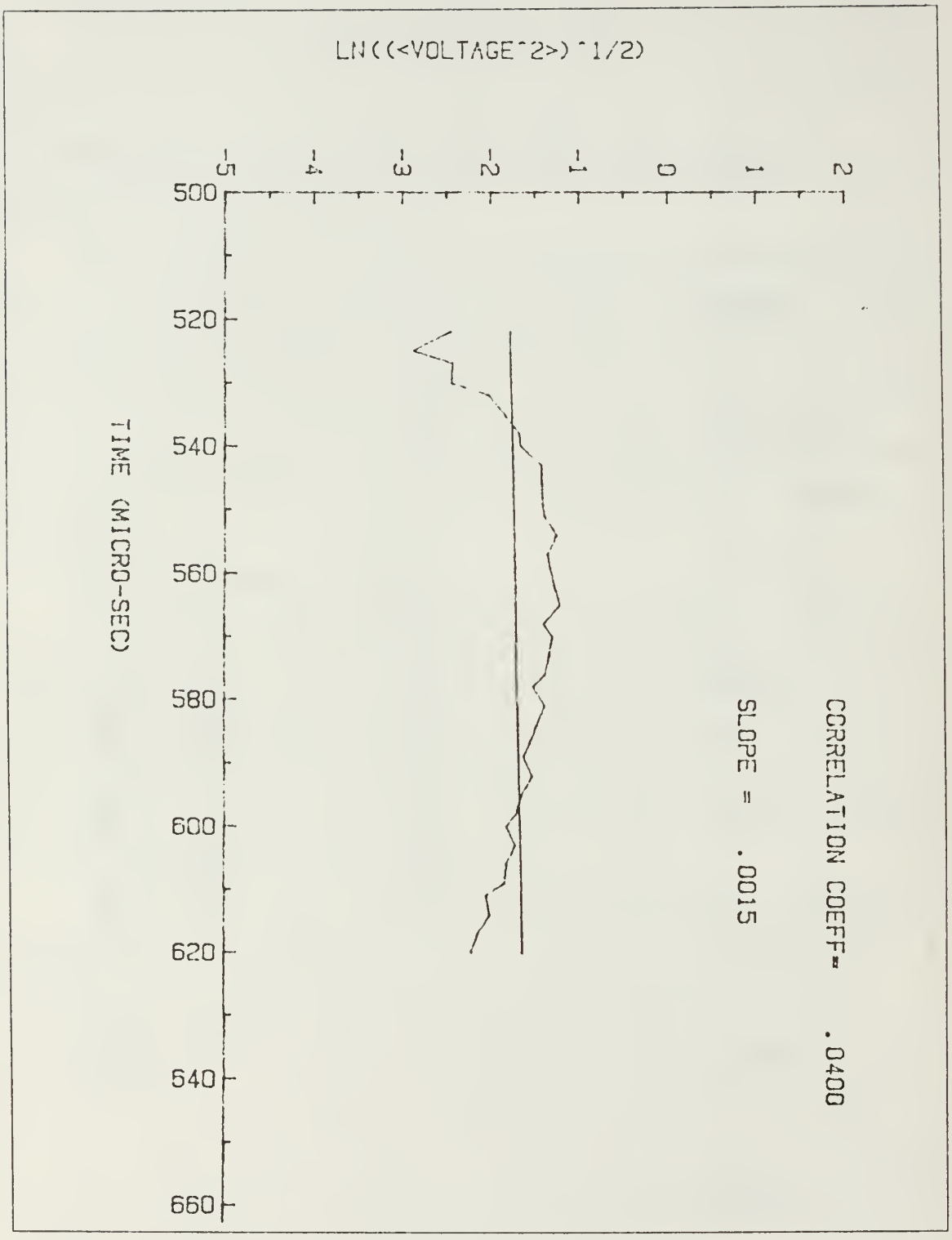

Figure 4.16 Decay envelope for reflection from aggregate/water interface in the glass tank (data set 52).

E. PROGRAMMING

An HP-86 desktop computer was adopted to collect and analyze the waveform data. The computer program was written to be interactive. This enables 1) the collection of data sets with different delay time intervals and 2) the collecting and processing of numerous data sets. The interactive programs allowed essential information to be entered via the key board, eliminating the need to modify the program whenever data sets were changed. The interactive prompts were useful for people unfamiliar with Basic programming.

1. Program "THESIS3"

This program was designed as the initial step in the data collection processing. Before the selected waveform data displayed on the 3091 Nicolet Digital Oscilloscope were output to the computer, it was switched into "freeze" or "store" mode from "live" mode. Through the interface RS-232, the computer received the stored waveform data and then processed them. After processing the waveform data and before receiving the next sampling data, the Nicolet 3091 had to be switched into "live" mode again. An HP-3421A Data acquisition and Control Unit was interfaced between the Nicolet 3091 and HP-86. The HP-3421A reduced the amount of manual operations in the data collection process. A five volts source were input to the HP-3421A. Commands form the HP-86 and 5 volts signal were used to control, by closing and opening the channel in the HP-3421A, the "mode switching" of the oscilloscope. To avoid errors, the oscilloscope should be warmed up enough while entering the inital information. Once this initial information was entered and the oscilloscope was warmed up enough; the whole system runs automatically.

Waveform data output from the oscilloscope were a stream of characters. To obtain the voltage and time value, all these characters needed to be normalized and converted by the computer. A program, listed in the Nicolet 3091 operation manual, was used for data value normalization. A data set, the waveform of the decay portion, was obtained by squaring and averaging 50 samples of waveform data for each transducer position. The running average formula used in the program was

$$< V^2 >_n = ((n-1) < V^2 >_{n-1} + V_n^2) / n$$

where $< V^2 >_n$ is n samples averaged squared-voltage, $< V^2 >_{n-1}$ is n-1 samples averaged squared-voltage and V_n^2 is squared voltage for the nth sample. Note that the average window for the waveform is 100 μs from the beginning of the decay. The above formula was processed for each corresponding time bin.

During each data set processing, some error messages, such as STRING OVF (which stands for the string variable overflow), were displayed on the HP-86 screen. This error messaged could be fatal to the data set if the data has not been stored on the disk. To avoid this problem, the program was designed so that after every 10 samples processed the updated data were stored on the disk over the previous updated data. The program eliminated the problem of the disk being full before the final data set was stored on the disk. This prevention could increase the processing time, but compared to the time wasted from the above problems, it is worthwhile. The final result for this program was 3 data files : one stored the squared voltage, one for time data and one for the number count of the samples.

2. Program "MAXIMUM"

In order to obtained the envelope of the waveform, this program was designed to pick up the local maximum of the voltage data. The voltages, stored in the data file from "THESIS3", were read and compared with the neighboring voltage data to decide the local maximum. The determined local maximums and corresponding time bins were stored in seperated files and printed out. The data files were differentiated by number according to the order they were acquired.

3. Program "PLOT3"

After the local maximums were determined, the decay portion of the waveform can be plotted by program "PLOT3". The experiments, for this project, took place mainly in the glass tank. A decay envelope measured in the glass tank has an interval between 520 and 619 μs starting from transmitting time. Some exceptions existed and gave different time frames.

To determine the decay constant, the voltage data were converted logarithmically and plotted vs. the time

$$V = V_0 e^{-\alpha t}$$

$$LN(V) = -\alpha t + LN(V_0)$$

If the cursor on the oscilloscope was not centered, the resulting envelope showed a "zig-zag" instead of a straight line for a perfect exponential decay.

The least-square method was adopted to calculate the best fit of straight line

$$y = ax + b$$

where a, which is similar to the decay constant, is the slope and b is the intercept on the y-axis. According to Beers (1953),

$$a = \frac{k\sum (x_n y_n) - \sum x_n \sum y_n}{k\sum x_n^2 - (\sum x_n)^2}$$

$$b = \frac{\sum x_n^2 \sum y_n - \sum x_n \sum (x_n y_n)}{k\sum x_n^2 - (\sum x_n)^2}$$

where k is the total number of pairs of (x,y) values, n is the number between 1 and k, $\sum x_n$ is the sum ot the total x value, $\sum y_n$ is the sum of the total y value, $\sum x_n^2$ is the sum of the squared x value, $\sum y_n^2$ is the sum of the squared y value and $\sum (x_n y_n)$ is the sum of the multiples of x_n and y_n.

Note that $\sum x_n^2$ and $\sum (x_n)^2$ are not the same. $\sum x_n^2$ implies that each value of x is squared and then a sum is made of these squares, while $\sum (x_n)^2$ implies that all of the values of x added together and then this sum is squared. There is an analogous distinction between $\sum (x_n y_n)$ and $\sum x_n \sum y_n$. In our case, the x-coordinate is the time value and the y-coordinate is the natural-log of the voltage. To check how close the observed and least-square estimated y-value, compare, a correlation coefficient was calculated (Chatfield, 1984)

$$r = \frac{(x_n - \bar{x})(y_n - \bar{y})}{(\sum (x_n - \bar{x})^2 \sum (y_n - \bar{y})^2)^{1/2}}$$

where r is the correlation coefficient, x is the mean value of x and y is the mean value of y. Slope and correlation coefficient were both printed with the graph.

4. Program "AVERAGE"

The received echo waveform varies from position to position because of the inhomogeneous sediment. To find the decay constant, we have to average out the

inhomogeneities to obtain a mean value of the waveform. This program performs a running average on the original data sets, producing the final averaged waveform of the sediment.

The above four programs are given in Appendix A.

V. RESULTS

The data sets for reflection from aggregate water interface are data 42 to 51, Figure C.1 to Figure C.9, and Figure 4.15. Table 3 shows the slope obtained for each data set varied between data sets. To get a mean value for the slope, the running average method was used to process the data sets. The running average method also shows how fast the average processing became stable. Data sets DAT2 to DAT10, Figure C.10 to Figure C.18, are the results for each average process. The slopes are listed on Table 4. It is evident that the slope becomes stable after 8 sets of data are averaged. The final averged slope is 2.13×10^{-2} Np μs and is quite different from the value reflected from the water air interface. The difference between the two slopes resulted from the effects of volume reverberation in the aggregate, and the scattering is significant.

TABLE 3
ORIGINAL AGGREGATE REFLECTION

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DATA42	-0.94	-0.5278
DATA43	-1.35	-0.5874
DATA44	-2.68	-0.7848
DATA45	-2.64	-0.8509
DATA46	-0.12	-0.1162
DATA47	-1.81	-0.3971
DATA48	-0.95	-0.3990
DATA49	-3.77	-0.8654
DATA50	-2.47	-0.9756
DATA51	-0.16	-0.0584

The data sets for reflection from fine-sand water interface are data 55 to 64, Figure D.1 to Figure D.10. The slope of each data set is listed on Table 5. Evidently,

TABLE 4
AVERAGED AGGREGATE REFLECTION

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DAT2	-1.19	-0.6051
DAT3	-1.97	-0.9720
DAT4	-2.32	-0.9175
DAT5	-2.18	-0.9343
DAT6	-2.10	-0.9914
DAT7	-1.98	-0.9952
DAT8	-2.16	-0.9932
DAT9	-2.20	-0.9943
DAT10	-2.13	-0.9958

the waveform changes very much for different data sets. The same running average method was used to remove the inhomogenities. Data sets DAT12 to DAT20 were produced from the average process. They are listed on Table 6 and plotted from Figure D.11 to Figure D.19. The slope became stable after 6 data sets were averaged. This might suggest that the fine sand has a greater homogeneity. The averaged slope for the fine sand is 2.37 x 10^{-2} Np/μs and is greater than the aggregate. However, the slope difference between them is not as distinguished when compared to the slope difference between the sediment and the water/air surface.

According to Equation 3.1, the decay portion volume scattering, represented in voltage, for the aggregate is

$$V_a = K (e^{-21300t} - e^{-37700t})$$

and for the fine sand is

$$V_s = K (e^{-23700t} - e^{-37700t})$$

The above relations only existed without surface scattering or the surface scattering was negligible.

TABLE 5
ORIGINAL FINE SAND REFLECTION

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DATA55	-1.51	-0.8178
DATA56	-3.03	-0.9581
DATA57	-2.50	-0.8112
DATA58	-0.75	-0.7290
DATA59	-1.00	-0.6776
DATA60	-3.41	-0.9957
DATA61	-3.33	-0.9050
DATA62	-1.42	-0.4922
DATA63	-2.41	-0.9389
DATA64	-1.03	-0.5784

A simplistic model for sediment volume reverberation was developed and is described in Appendix A. Combining the experimental results and the newly developed model, the volume scattering coefficient obtained was 0.0413 $\pm$ 0.007 m^{-3} for fine sand and 0.0624 $\pm$ 0.007 m^{-3} for aggregate. These value are reasonable compared to the difference between the decay constant obtained from the experiment. They are produced as a best fit using the least square method. The correlation coefficients, approximately 0.88, indicate they are quite a good fit. As a first model, the result is promising. However, the discrepancy between the experiment and model might suggest the model is still very crude. Also mentioned in the Appendix A is that this is only a first step to try to obtain a theory to describe the volume scattering effect of the sediment; it need to be improved by further effort.

The ka value for fine sand is 0.12, which is quite small compared to 1. From Equation 2.2, cloud-of-small-spheres model, the volume scattering coefficient for the fine sand is 0.0082 m^{-3} and is not too far from 0.0413 m^{-3}. As mentioned in Chapter 2, Equation 2.2 was derived under various assumptions and does not apply to real sediment. From Equation 2.3, single-small-sphere model, the volume scattering

TABLE 6
AVERAGED FINE SAND REFLECTION

DATA SET	SLOPE ($\times 10^{-2}$)	CORRELATION COEFFICIENT
DAT12	-1.84	-0.9265
DAT13	-2.09	-0.9051
DAT14	-1.46	-0.9309
DAT15	-1.47	-0.9223
DAT16	-2.36	-0.9912
DAT17	-2.39	-0.9904
DAT18	-2.39	-0.9902
DAT19	-2.38	-0.9903
DAT20	-2.37	-0.9916

coefficient is 0.34 m^{-3} which is an order of magnitude different from the the measured value 0.0413 m^{-3}. These values suggest that the cloud-of-small-spheres model is closer to the newly developed model than the single-small-sphere model.

The scattering coefficient obtained from Equation 2.2 is 9456 m^{-3} and from Equation 2.3 is 1134 m^{-3}. Obviously the two values deviate considerably from the true value. The ka value is equal to 2.1, which is outside the Rayleigh scattering limit. Thus Equations 2.2 and 2.3 can not be applied to the aggregate.

VI. CONCLUSION AND RECOMMENDATION

The following conclusions are possible:

1. The inhomogenities within the sediment caused the reflected waveform to change considerably for various transducer positions. The changes can be removed by averaging over the inhomogeneities and the averaging yields a mean decay constant.
2. The glass tank works very well, and therefore a bigger tank to contain the sediment is not necessary.
3. The laboratory procedure to measure the volume reverberation, using off-the-shelf equipment and a high pass filter in a water-over-sediment system, is workable.
4. The basic program, written for a HP-86 desktop computer, is sufficient for this experiment.
5. Although Equations 2.2 and 2.3 can not be applied to aggregate since it has a ka greater than 1, the aggregate does have a higher volume reverberation than fine sand. The aggregate has a larger size than the fine sand; this might suggest that the larger size sediment causes more volume reverberation.
6. From the scattering coefficient 0.0413 $\pm$ 0.007 m^{-3} for the fine sand and 0.0624 $\pm$ 0.007 m^{-3} for the aggregate, the scattered energy received by transducer is quite small compared to the incident energy.
7. For fine sand sediment, the cloud-of-small-spheres model works better than the single-small-sphere model.
8. The simplistic model, derived from the true acoustical pulse and described in Appendix A, gives a crude formulated volume scattering relationship. Combining with the experiment result, the sediment's volume scattering coefficient can be estimated.

Further study of the volume reverberation from ocean sediment is recommended. Future experimentation should include further variation of the sediment size and of the acoustic frequency to find a relationship combining the ka value and volume reverberation. The developed model should be improved to obtain a better result

coincident with the experimental result. The absorption coefficient of different sediment with the frequency used should be measured to compare the value obtained from Urick's formula described in appendix A. Equations 2.2 and 2.3 should be improved to obtain the scattering coefficient, which can be used to check the above model. Continued use of the experimental procedure, equipment and computer programs, written for this project on the HP-86, is highly recommended.

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APPENDIX A
DERIVATION OF SCATTERING FROM THE SEDIMENT

The generated electrical pulse can be described by the step unit function, H, as follows:

$$I(t) = I_0 (H(t) - H(t-\tau)) \qquad (A.1)$$

where I(t) is the intensity at time t, I_0 is the intensity amplitude, τ is the pulse length,

$$H(t) = \begin{cases} 0 & t < 0 \\ 1 & t \geq 0 \end{cases}$$

and

$$H(t-\tau) = \begin{cases} 0 & t-\tau < 0 \\ 1 & t-\tau \geq 0 \end{cases}$$

Since the transducer is a resonant system with damping, the square electrical pulse was transformed into an acoustic pulse with an exponential rise, an approximately flattened top and exponential decay. The shape of the acoustic waveform can be described, (Sanders and Coppens, 1986), as

$$f(t) = (1 - e^{-\alpha t}) H(t) + (1 - e^{-\alpha \tau}) H(t-\tau) \qquad (A.2)$$

where t is the delay time and α is the decay constant.

Let a transducer, located in the water, send out a sound pulse to a smoothed sediment surface. To assure the surface scattering is negligible and the volume scattering is only single scattering, reflected pulse received, by the same transducer, should have an intensity (Sanders and Coppens, 1986)

$$I = .(\int T_i^2 s_v e^{-\beta\xi} I_0 f(t-2\xi/c)d\xi/(r+\xi)^2 + R_i I(t)/r^2) / r^2 \qquad (A.3)$$

Where T_i is the intensity transmission coefficient, s_v is the volume scattering coefficient, β is the absorption coefficient in the sediment, ξ is the affected sediment depth, R_i is the intensity reflection coefficient and r is the distance between the transducer and sediment. From above equation, the intensity contributed by scattering is

$$I_s = \int T_i^2 s_v e^{-\beta\xi} I_o f(t-2\xi/c) d\xi / (r+\xi)^2 r^2 \qquad (A.4)$$

and the intensity contributed by the reflection is

$$I_r = R_i I_o f(t) / r^4 \qquad (A.5)$$

If $r >> \xi$, then

$$I_s = (T_i^2 s_v I_o / r^4) \int e^{-\beta\xi} f(t-2\xi/c) d\xi \qquad (A.6)$$

where

$$f(t-2\xi/c) = (1 - e^{-\alpha(t-2\xi/c)}) H(t-2\xi/c) - (1 - e^{-\alpha(t-\tau-2\xi/c)}) H(t-\tau-2\xi/c) \qquad (A.7)$$

During the integration, the lower boundary of ξ is zero; the upper boundary is $ct/2$ for $H(t-2\xi/c)$ and $c(t-\tau)/2$ for $H(t-\tau-2\xi/c)$. Note that only the decay portion, $t > \tau$, was interested. After the integration,

$$I_s = A (-(e^{-c\beta t/2} - 1)/\beta - (e^{-c\beta t/2} - e^{-\alpha t})/(-\beta + 2\alpha/c) \qquad (A.8)$$

$$+ (e^{-c\beta(t-\tau)} - 1)/\beta + (e^{-c\beta(t-\tau)/2} - e^{-\alpha(t-\tau)})/(-\beta + 2\alpha/c))$$

where

$$A = T_i^2 s_v I_o / r^4 \qquad (A.9)$$

From the experimental formula $\beta = 0.25f$ (Urick, 1979) and f is 182 kHz, the absorption coefficient

$$\beta = 45.5 \text{ dB/m} = 5.2 \text{ Np/m},$$

$c\beta/2$ is 4030 Np/s for aggregate and is 4186 Np/s for the fine sand. The intensity decay constant α is twice the pressure decay constant δ. From the experiment, δ is 37700 Np/s and it gives an α equal to 75400 Np/s; $2\alpha/c$ is 97.2 Np/m for the aggregate and is 93.6 Np/m for the fine sand. After plugging in the above values for the aggregate, Equation A.8 becomes

$$I_s = A(e^{-4030t}/11.6) - A(8.3\, e^{-75400t}) \qquad (A.10)$$

For the fine sand, Equation A.7 becomes

$$I_s = A(e^{-4186t}/11.0) - A(8.6\, e^{-75400t}) \qquad (A.11)$$

$$R_i = R^2$$
$$R_i + T_i = 1$$

The pressure reflection coefficient R is 0.356 for the aggregate (Diaz, 1986) and 0.36 for the fine sand (Bradshaw, 1981). For the aggregate,

$$R_i = 0.1270$$
$$T_i = 0.8730$$

For the fine sand,

$$R_i = 0.1296$$
$$T_i = 0.8704$$

The pulse length is 88 μs and from equation A.5,

$$I_r = I_o R_i (e^{-\alpha\tau} - 1)\, e^{-75400t}/r^4 \qquad (A.12)$$

Using the above values, the reflected intensity for the aggregate becomes

$$I_r = 96.6\, e^{-75400t}\, I_o/r^4 \qquad (A.13)$$

and for the fine sand

$$I_r = 98.5\, e^{-75400t}\, I_o/r^4 \qquad (A.14)$$

The intensity contributed by the scattering for the aggregate is

$$I_s = (s_v I_o r^4)(e^{-4030t}/15.2 - 6.3 e^{-75400t}) \quad (A.15)$$

and for the fine sand,

$$I_s = (s_v I_o r^4)(e^{-4186t}/14.5 - 6.5 e^{-75400t}) \quad (A.16)$$

Combining the above equations, the reflected intensity from the aggregate received by the transducer is:

$$I = (I_o r^4) B \quad (A.17)$$

where

$$B = (s_v e^{-4030t} 15.2 - 6.3 s_v e^{-75400t} + 96.6 e^{-75400t}) \quad (A.18)$$

For the fine sand,

$$I = (I_o r^4) D \quad (A.19)$$

where

$$D = (s_v e^{-4186t}/14.5 - 6.5 s_v e^{-75400t} + 98.5 e^{-75400t}) \quad (A.20)$$

By inputting a series of scattering coefficients and computing the Log $(B)^{1/2}$ and Log $(D)^{1/2}$, the theoretical envelope was determined. A least-square-fit slope was obtained for each envelope. The scattering coefficient for each sediment can be estimated by the value of s_v, for which the slope of the theoretical envelope is equal to the slope of experiment data. For the fine sand, measured the decay constant 23700 Np/s gave a scattering coefficient of 0.0413 m^{-3}. For the aggregate, the scattering coefficient 0.0624 m^{-3} was obtained from the measured decay constant 21300 Np/s.

Figure A.1 and Figure A.2 show the envelopes determined theoretically from the above values of s_v for the aggregate and fine sand respectively. The theoretical

envelope is plotted by normalizing the left end of the best fit slope line to the same value obtained from the experiment and then applying this normalization to the whole theoretical envelope.

Results from the fine sand were selected to find the uncertainty of scattering coefficient obtained from the above method. By comparing a series of envelope plots for different scattering coefficient, the uncertainty $\pm$ 0.007 was determined. Figure A.3 and A.4 show the envelopes for scattering coefficients $\pm$ 0.007 different from 0.0413 m^{-3}. The slope changes as the scattering coefficient changes. In the beginning of decay, the dominant term in equation A.20 is the reflection term which is independent on s_v, and the scattering term which depends on s_v is negligible. The theoretical value will not change much in the beginning of decay as the scattering coefficient changes. The normalization, described previously, still gave a good approximation to the plot of the theoretical envelope vs. the experimental envelope for different scattering coefficients.

Note that the model derived and described in this appendix is crude. A later improvement on this model is suggested.

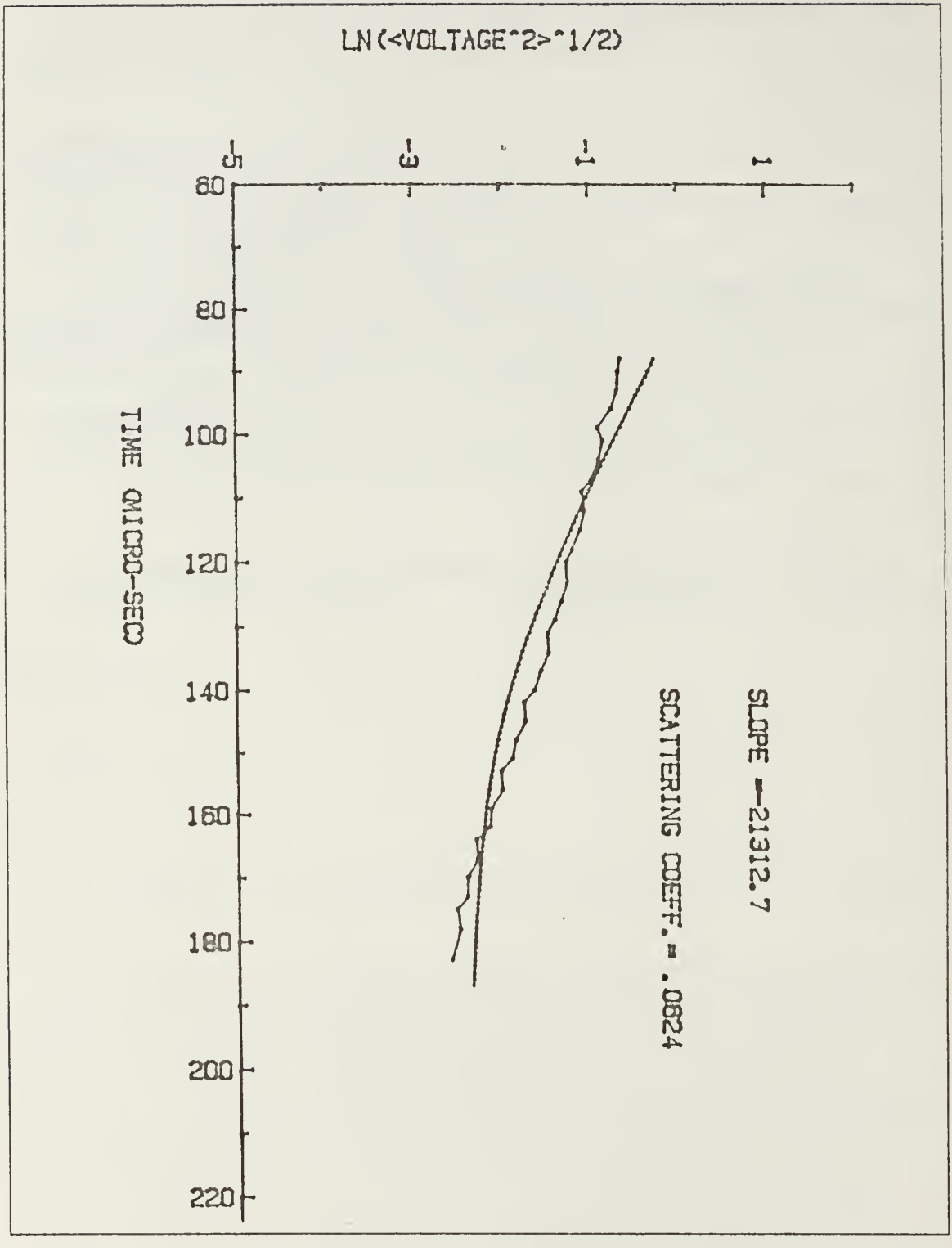

Figure A.1 For the aggregate, the decay envelope obtained from the model vs. the decay envelope obtained from the experiment.

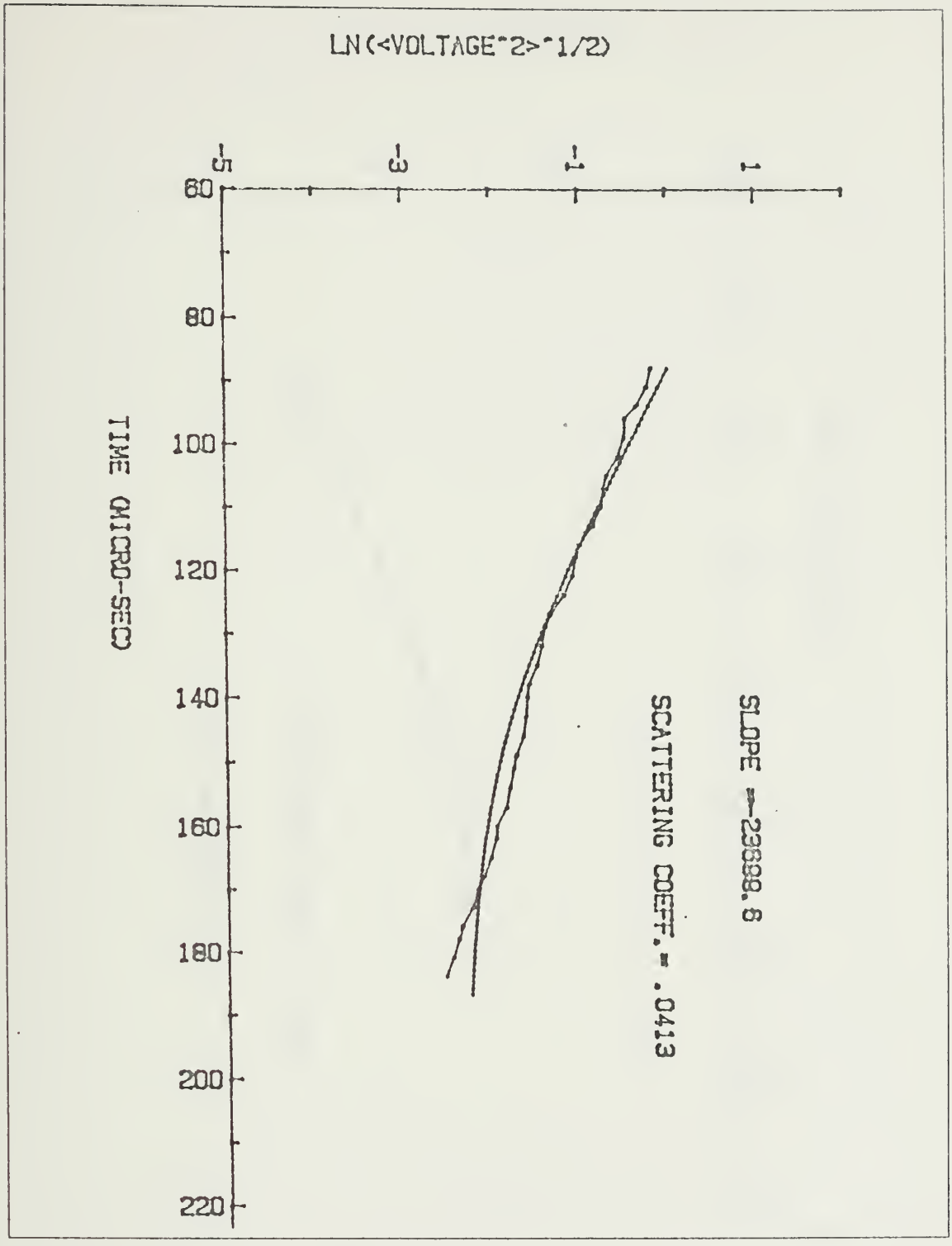

Figure A.2 For the fine sand, the decay envelope obtained from the model vs. the decay envelope obtained from the experiment.

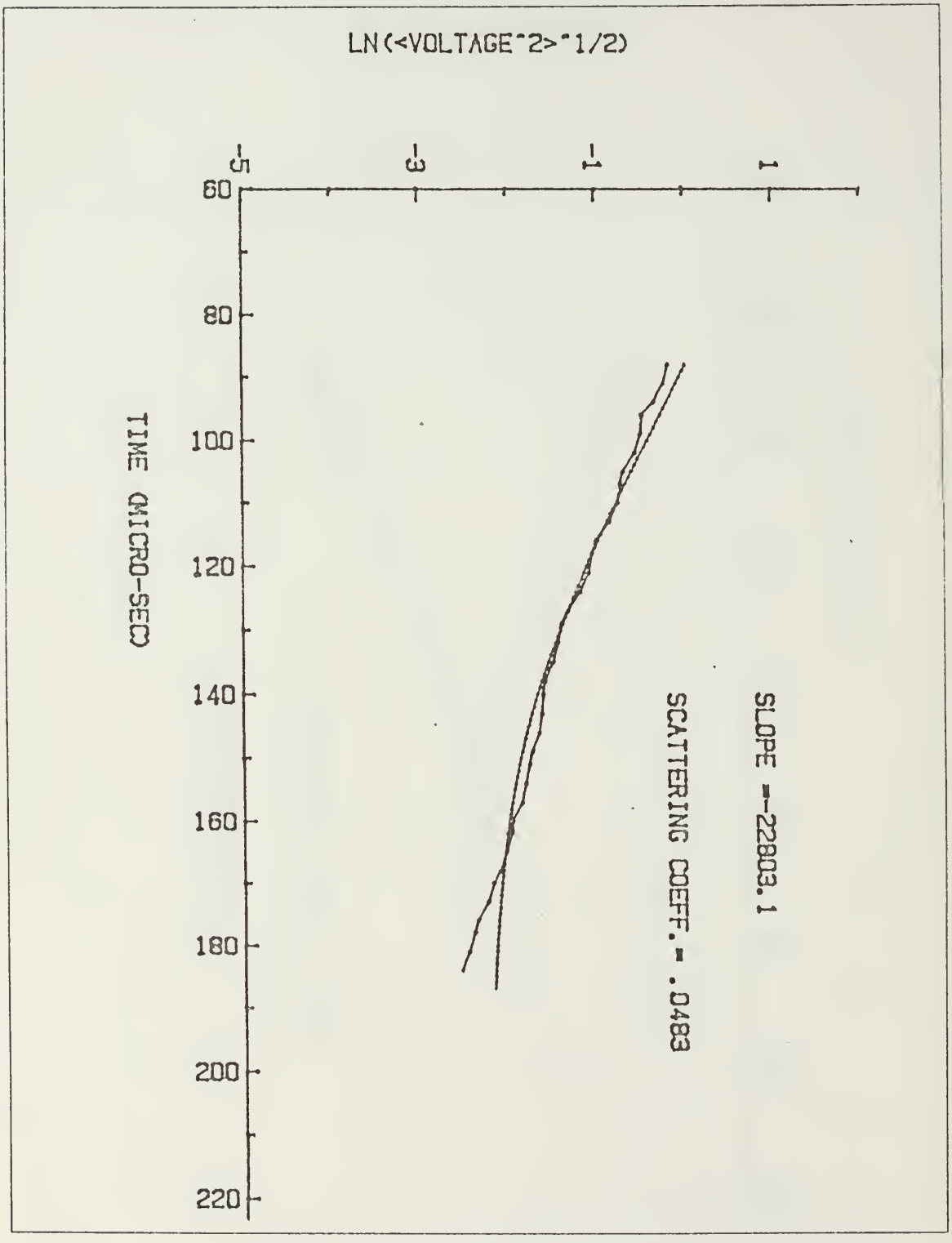

Figure A.3 For the fine sand, the decay envelope obtained from the model vs. the decay envelope obtained from the experiment.

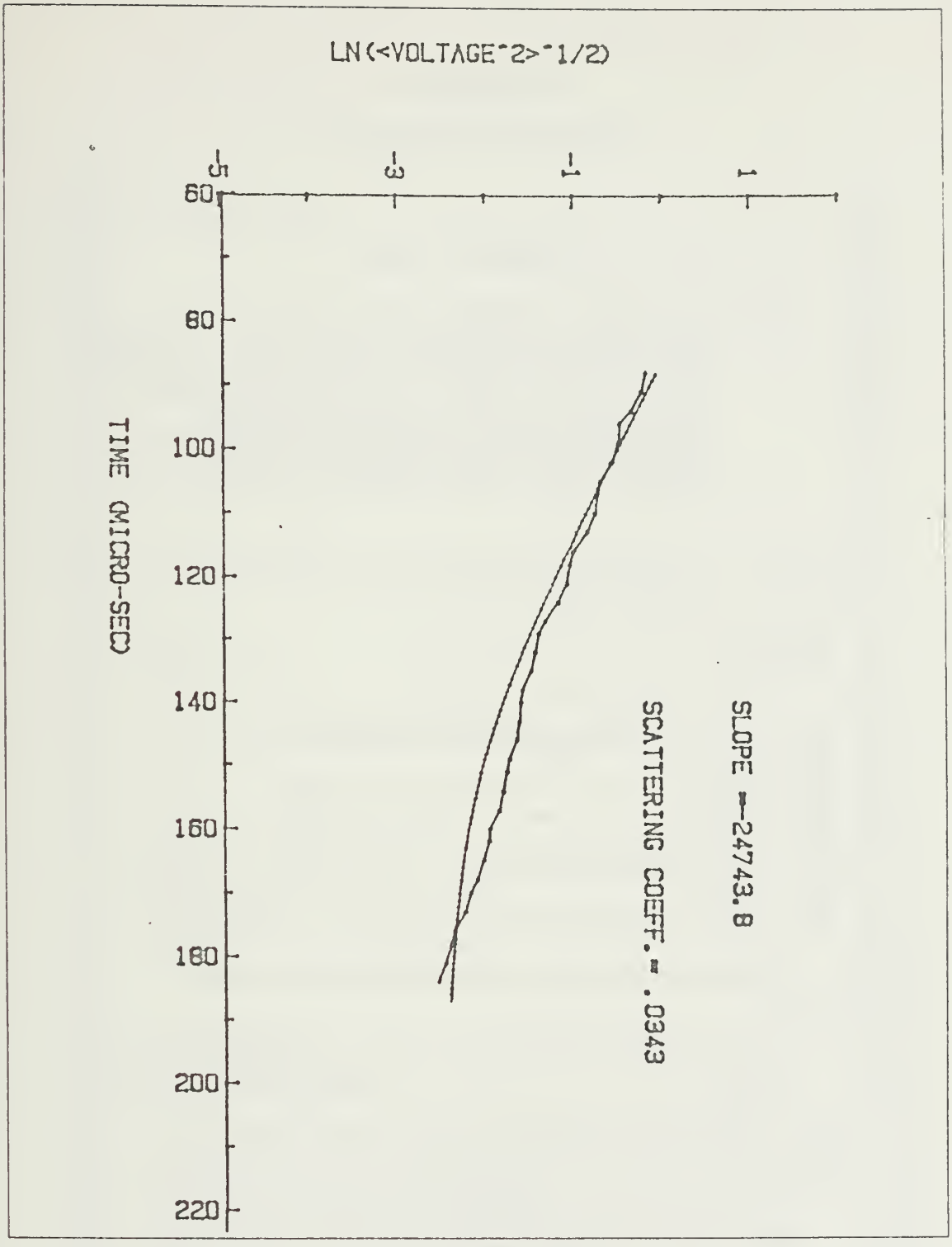

Figure A.4 For the fine sand, the decay envelope obtained from the model vs. the decay envelope obtained from the experiment.

APPENDIX B

COMPUTER PROGRAM

```
1000  ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
1010  ! !                                                                          !!
1020  ! !                                                                          !!
1030  ! !                       PROGRAM :  THESIS3                                 !!
1040  ! !                                                                          !!
1050  ! !                                                                          !!
1060  ! !        THIS PROGRAM IS DESIGNED TO CONVERT AND NORMALIZE THE             !!
1070  ! !        THE WAVEFORM DATA VALUE AND POINT LOCATION, TRANSFERED            !!
1080  ! !        FROM THE NICOLET 3091 DIGITAL OSCILLASCOPE, TO THE                !!
1090  ! !        VOLTAGE AND TIME VALUE.  THE NICOLET IS COTROLED BY               !!
1100  ! !        THE HP-3041 DATA ACQUISITION AND CONTROL UNIT.                    !!
1110  ! !        THE PROGRAM SQUARE THE VOLTAGE VALUE AND THEN TAKE                !!
1120  ! !        THE RUNNING AVERAGE FOR FIFTY SET OF READING.  TO                 !!
1130  ! !        INSURE THE DATA IS NOT LOSSED DURING COMPUTER ERROR.              !!
1140  ! !        THE DATA IS BEING STORE IN THE DISK AFTER EVERY 10                !!
1150  ! !        SET CALCULATION.                                                  !!
1160  ! !                                                                          !!
1170  ! !                                                                          !!
1180  ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
1181  !
1182  !
2000  DIM D(1501),T(1501),S(1501)
2010  DIM VDATA$[20],VTIME$[20],VCOUNT$[20]
2020  INTEGER N,I
2021  !
2022  !     INPUT THE FILE NAME TO STORE DATA
2023  !
2024  DISP "WHAT IS THE FILE NAME FOR VOLTAGE DATA ?"
2025  INPUT VDATA$
2026  DISP "WHAT IS THE FILE NAME FOR TIME DATA ?"
2027  INPUT VTIME$
2028  DISP "WHAT IS THE FILE NAME OF THE COUNT DATA ?"
2029  INPUT VCOUNT$
2030  DISP "YOUR INTEREST TIME INTERVAL IS FROM [START] TO [ENDT] "
2031  DISP "WHAT IS THE STARTING TIME OF MEASURING IN MICRO-SEC) ?"
2032  INPUT START
2033  DISP "WHAT IS THE ENDING TIME OF MEASURING ( IN MICRO-SEC) ?"
2034  INPUT ENDT
2035  !
2036  !   CHECKING THE INTERESTED TIME INTERVAL FROM CRT SCREEN
2037  !
2040  LET N=1
2060  !
2061  !    IF THIS IS NOT THE FIRST SET OF DATA, THE COMPUTER IS GOING
2062  !    TO READ THE DISK FOR PREVIOUS DAT INFORMATION, AND CARRY ON
2063  !    THE JOB
2064  !
2080  DISP "IS THIS YOUR FIRST DATA SET OUT OF THE 50 DATA SET?"
2100  DISP "PRESS 0 IF YES ; PRESS 1 IF NO"
2120  INPUT ANS
2140   IF ANS=1 THEN GOSUB READ_DATA
2219  !
2220  !    FOLLOWING IS THE COMPUTER RECEIVE THE DATA FROM 3091 AND
2221  !    THEN CALCULATE THE VOLTAGE AND TIME VALUE.
2222  !
2240  DIM I$[5],D$[20000],N$[40]
2260  CONTROL 10,3 : 15
2280  CONTROL 10,4 ; 58
2290  CONTROL 10,2 : 1
```

```
2292  !
2300  !
2301  OUTPUT 709 ;"OPN4"
2302  !
2303  !   ABOVE STATEMENT IS LET THE CRT TO "LIVE" CONDITION
2304  !
2305  !
2306  !  FOLLOWING ONE IS TO LET THE CRT IN "STORE" CONDITION
2307  !
2308  !
2310  OUTPUT 709 ;"CLS5"
2311    WAIT 1000
2312  !
2313  !   PRESS BOTTOM ONLY USED WITHOUT THE HP-3421 UNIT
2314  ! DISP "PRESS 3091 BUTTON"
2315  !
2316  !   LET THE DATA TRASMIT TO THE COMPUTER THROUGHR RS-232
2320  !
2321  OUTPUT 709 ;"CLS2"
2322  !
2323  !  ABOVE STATEMENT LET THE WAVEFORM INFORMATION BE TRANSFERED
2324  !  FROM CRT TO COMPUTER THROUGH RS-232 INTERFACE
2325  !
2340  ENTER 10 ; I$
2360  ENTER 10 ; D$
2380  ENTER 10 ; N$
2390  !
2400  H0=VAL (N$[16,20])
2420  V1=(VAL (N$[21,25])-5)*10^(VAL (N$[26,30])-12)
2440  H1=(VAL (N$[31,35])-5)*10^(VAL (N$[36,40])-12)
2441  !
2443  OUTPUT 709 ;"OPN5"
2445  OUTPUT 709 ;"OPN2"
2446  !  LET THE CRT IN LIVE MODE
2447  OUTPUT 709 ;"CLS4"
2460  J=1
2480  K=5
2500  PRINT "N=",N
2520  FOR I=0 TO ENDT
2525  IF I<START OR I>ENDT THEN 2780
2530  !
2531  !    NORMALIZE THE VOLTAGE VALUE AND TIME FOR THE INTEREST INTERVAL
2532  !
2540  D(I)=VAL (D$[J,K])*V1
2560  T(I)=(I-H0)*H1
2580  D(I)=D(I)^2
2600  IF N=1 THEN GOTO 2640
2620  S(I)=((N-1)*S(I)+D(I))/N
2621  !
2640  IF N=1 THEN S(I)=D(I)
2660  IF I=START THEN 2760 ELSE 2680
2680  IF I=START+20 THEN 2760 ELSE 2700
2700  IF I=START+30 THEN 2760 ELSE 2720
2720  IF I=START+50 THEN 2760 ELSE 2740
2740  IF I=ENDT THEN 2760 ELSE 2780
2760  DISP T(I);"SEC    ";D(I);"VOLT    ";S(I)
2770  PRINT T(I);"SEC    ";D(I);"VOLT    ";S(I)
2771  !
2780  J=J+5
2800  K=K+5
```

```
2820  NEXT I
2840  N=N+1
2850  !
2851  !  LET THE DATA BEING STORE AFTER EVERY 10 SET OF CALCULATION
2852  !
2860  IF N MOD 10=1 THEN 2965 ELSE 2240
2965  IF N=11 THEN 2970 ELSE 2980
2970    CREATE VDATA#,200,8
2971   CREATE VCOUNT#,1,8
2972   CREATE VTIME#,200,8
2980  GOSUB WRITE_DISK
2990  IF N=51 THEN 3000 ELSE 2240
3000  END
3305  !
3306  !
3307  !
3308  !    FOLLOWING SUBROUTINE IS USED TO WRITE THE DATA TO THE DISK
3309  !
3310  !
3500  WRITE_DISK:
3510   PURGE VDATA#
3520  CREATE VDATA#,200,8
3540  ASSIGN# 1 TO  VDATA#
3550  PURGE VCOUNT#
3560  CREATE VCOUNT#,1,8
3580  ASSIGN# 2 TO  VCOUNT#
3590  PURGE VTIME#
3600  CREATE VTIME#,200,8
3620  ASSIGN# 3 TO  VTIME#
3640  PRINT# 2 ; N
3660  FOR I=START TO ENDT
3680  PRINT# 3 ; T(I)
3700  PRINT# 1 ; S(I)
3720  NEXT I
3740  ASSIGN# 1 TO  *
3760  ASSIGN# 2 TO  *
3780  ASSIGN# 3 TO  *
3800  RETURN
3900  !
3910  !
3920  !  FOLLOWING SUBROUTINE IS USED TO READ THE DATA FROM PREVIOUS
3930  !  WRITTEN DISK
3940  !
3950  !
4000  READ_DATA:
4020  ASSIGN# 2 TO  VCOUNT#
4040  ASSIGN# 1 TO  VDATA#
4060  READ# 2 ; N
4061  PRINT N
4080  FOR I=START TO ENDT
4100  READ# 1 ; S(I)
4120  IF I=START THEN 4220 ELSE 4140
4140  IF I=START+20 THEN 4220 ELSE 4160
4160  IF I=START+30 THEN 4220 ELSE 4180
4180  IF I=START+50 THEN 4220 ELSE 4200
4200  IF I=ENDT THEN 4220 ELSE 4240
4220  PRINT S(I)
4240  NEXT I
4260  ASSIGN# 1 TO  *
4280  ASSIGN# 2 TO  *
4380  RETURN
```

```
800  ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
801  ! !                                                                        !!
802  ! !                                                                        !!
803  ! !                          PROGRAM : MAXIMUM                             !!
804  ! !                                                                        !!
805  ! !                                                                        !!
806  ! !          THIS PROGRAM IS DESIGNED TO READ THE SQUARED                  !!
807  ! !          WAVEFORM VOLTAGE DATA AND TIME DATA STORED                    !!
808  ! !          IN THE DISK AND THEN CHOOSE THE LOCAL MAXIMUM                 !!
809  ! !          (WAVEFORM ENSEMBLE). THE CHOOSED MAXIMUMS WILL                !!
810  ! !          BE TAKEN SUARE-ROOT AND STORE THE FINAL RESULT                !!
811  ! !          ON THE DISK                                                   !!
812  ! !                                                                        !!
813  ! !                                                                        !!
814  ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
815  !
816  !
880  DIM VDATA$[20],VTIME$[20],VNUMBER$[20],VTIME_MAX$[20],VMAXIMUMS$[20]
900  DISP "WHAT IS THE NAME FOR VOLTAGE DATA FILE ?"
910  INPUT VDATA$
920  DISP "WHAT IS THE NAME FOR TIME DATA FILE ?"
930  INPUT VTIME$
940  DISP "WHAT IS THE NAME FOR FILE TO STORE THE NUMBER$ NO. ?"
950  INPUT VNUMBER$
960  DISP "WHAT IS THE NAME FOR FILE TO STORE THE TIME_MAX$ DATA ?"
970  INPUT VTIME_MAX$
980  DISP "WHAT IS THE NAME FOR FILE TO STORE THE MAXIMUMS$?"
990  INPUT VMAXIMUMS$
991  DISP "WHAT IS THE STARTING TIME OF YOUR DATA COLLECING ?"
992  INPUT START
993  DISP "WHAT IS THE ENDING TIME OF THE DATA COLLECTING ?"
994  INPUT ENDT
996  !
1000 ASSIGN# 1 TO  VDATA$
1020 ASSIGN# 3 TO  VTIME$
1040 CREATE VNUMBER$,1,8
1060 ASSIGN# 4 TO  VNUMBER$
1080 CREATE VTIME_MAX$,100,8
1100 ASSIGN# 5 TO  VTIME_MAX$
1120 CREATE VMAXIMUMS$,100,8
1140 ASSIGN# 6 TO  VMAXIMUMS$
1141 !
1144 INTEGER PRINTTER
1146 DISP "WHAT IS THE PRINTER DEVICE ADDRESS NO. ?"
1148 !  INPUT THE PRINTER NO.  SCREEN IS 1
1150 INPUT PRINTTER
1152 PRINTER IS PRINTTER
1154 !
1160 DIM S(1501),T(1501),TIM(100),MAXS(100)
1165 PRINT USING 1170 : "TIME (SEC.)","VOLT"
1170 IMAGE 25X,11A,12X,4A
1180 INTEGER I,J
1200 FOR I=START TO ENDT
1220 READ# 3 : T(I)
1240 READ# 1 : S(I)
1260 NEXT I
1280 LET J=0
1290 !
1291 !  IF THE FIRST DATA BEING READ IS GREAT THAN THE SECOND ONE,
```

```
1292  !  THE FIRST ONE IS TREATED AS A LOCAL MAXIMUM.
1293  !
1300  IF S(START)>= S(START+1) THEN 1320 ELSE 1500
1320     TIM(J)=T(START)
1340     MAXS(J)=SQR (S(START))
1360  PRINT# 5 ; TIM(J)
1380  PRINT# 6 ; MAXS(J)
1400  PRINT USING 1410 ; "J=";J,TIM(J),MAXS(J)
1410  IMAGE 12X,3A,DDD,7X,D.DDDDDD,11X,D.DDDDDDDD
1420  ! PRINT TIM(J)
1440  ! PRINT MAXS(J)
1460     J=J+1
1480  !
1500  FOR I=START+1 TO ENDT-1
1520     IF S(I)>= S(I-1) AND S(I)>= S(I+1) THEN 1540 ELSE 1720
1540         TIM(J)=T(I)
1560         MAXS(J)=SQR (S(I))
1580  !
1600  PRINT USING 1610 ; "J=",J,TIM(J),MAXS(J)
1610  IMAGE 12X,3A,DDD,7X,D.DDDDDD,11X,D.DDDDDDDD
1620  ! PRINT TIM(J)
1640  ! PRINT MAXS(J)
1660  PRINT# 5 ; TIM(J)
1680  PRINT# 6 ; MAXS(J)
1700  J=J+1
1720  NEXT I
1730  J=J-1
1740  PRINT# 4 ; J
1760  ASSIGN# 4 TO  *
1800  ASSIGN# 5 TO  *
1820  ASSIGN# 6 TO  *
1840  ASSIGN# 1 TO  *
1880  ASSIGN# 3 TO  *
1900  END
```

```
900  !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
901  ! !                                                            !!
903  ! !                                                            !!
904  ! !                       PROGRAM : PLOT3                      !!
905  ! !                                                            !!
906  ! !                                                            !!
907  ! !     THIS PROGRAM IS DESIGNED TO PLOT THE ENVELOP           !!
908  ! !     OF WAVEFORM BY READING DATA FROM DATA DISK.            !!
909  ! !     AFTER READING, VOLTAGE DATA IS CONVERTED TO LOG        !!
910  ! !     VALUE, THEN BE PLOTTED.  AFTER PLOTING, A LEAST-       !!
911  ! !     SQUARE METHOD IS USED TO FIND THE BEST FIT STRAIGHT    !!
912  ! !     LINE FOR THE LOG-ENSEMBLE, PLOT THE LINE, PRINT        !!
913  ! !     OUT THE SLOPE OF THE LINE AND THE CORRELATION          !!
914  ! !     COEFFICIENT.                                           !!
915  ! !                                                            !!
916  ! !                                                            !!
917  !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
918  !
919  !
1000  CLEAR
1020  GCLEAR
1022  INTEGER PLOTER
1024  DISP "WHAT IS YOUR POLTTER DEVICE ADDRESS NO. ?"
1025  !  INPUT THE PLOTTE NO.  SCREEN IS 1
1026  INPUT PLOTER
1028  PLOTTER IS PLOTER
1040  FRAME
1041  !
1042  !  THIS PLOT SIZE IS TO FIT THE REQUIREMENT FOR THE NPS THESIS
1043  !
1060  LOCATE 30,125,30,85
1080  CSIZE 3
1100  MOVE 50,20
1120  LABEL "TIME (MICRO-SEC)"
1140  PEN UP
1160  MOVE 18,40
1180  DEG
1200  LDIR 90
1220  LABEL "LN((<VOLTAGE^2>)^1/2)"
1240  PEN UP
1241  !
1242  !   DEFAULT SET-UP IS TO FIX THE PLOTING COORDINATION AS
1243  !   X-AXIS IS FROM 500 TO 670 (MICRO-SEC), Y-AXIS IS FROM
1244  !   -5 TO 2
1245  !
1250  DISP "DO YOU WANT TO USE DEFAULT SET-UP ? YES=0"
1251  INPUT BULL
1252  IF BULL=0 THEN 1253 ELSE 1260
1253  SCALE 500,670,-5,2
1255  LAXES 10,.5,500,-5,2,2
1256  XMIN=500
1257  GOTO 1710
1259  !
1260  DISP "ENTER THE XMIN OF SCALE"
1280  INPUT XMIN
1300  DISP "ENTER XMAX OF SCALE"
1320  INPUT XMAX
1340  DISP "ENTER THE YMIN OF SCALE"
1360  INPUT YMIN
```

```
1380  DISP "ENTER THE YMAX OF SCALE "
1400  INPUT YMAX
1420  SCALE XMIN,XMAX,YMIN,YMAX
1440  FXD 0,2
1460  DISP "ENTER THE X-TICKING SPACE"
1480  INPUT XT
1500  DISP "ENTER THE Y-TICKING SPACE"
1520  INPUT YT
1540  DISP "ENTER THE X INTERSECTION"
1560  INPUT XI
1580  DISP "ENTER THE Y INTER SECTION"
1600  INPUT YI
1620  DISP "ENTER THE X-MAJOR COUNT"
1640  INPUT XMC
1660  DISP "ENTER THE Y-MAJOR COUNT"
1661  !
1680  INPUT YMC
1700  LAXES XT,YT,XI,YI,XMC,YMC
1710  GRAPH
1720   PEN 1
1721  !
1740  DIM TIM(100),MAXS(100)
1741  DIM TIMEMAX$[20],MAXIMUM$[20]
1742  DISP "WHAT IS YOUR FILE NAME FOR TIMEMAX$ ?"
1744  INPUT TIMEMAX$
1746  DISP "WHAT IS YOUR FILE NAME FOR MAXIMUM$ ?"
1748  INPUT MAXIMUM$
1749  PRINT "THE DATA FILES ARE",TIMEMAX$,"AND",MAXIMUM$
1750  DISP "WHAT IS THE HIGHEST ORDER OF ARRAY NUMBER?"
1751  ! THIS GIVES A CHOOICE TO CHOOSE THE END POINT OF PLOT
1752  INPUT JK
1759  !
1760  ASSIGN# 5 TO  TIMEMAX$
1780  ASSIGN# 6 TO  MAXIMUM$
1781  DISP "PRESS 0 IF THE FIRST LOCAL MAXIMUM IS BEING SAVED ?"
1782  INPUT OK
1790  FOR I=0 TO JK
1800  READ# 5 ; TIM(I)
1802  !
1803  !   CONVERT THE TIME UNIT FROM SEC TO MICRO_SEC
1804  !
1810  TIM(I)=TIM(I)*1000000
1820  READ# 6 ; MAXS(I)
1821  MAXS(I)=LOG (MAXS(I))
1822  !  CONVERT THE VOLTAGE TO NATURE LOG VALUE
1823  NEXT I
1825  K=JK+1
1826  IF OK=0 THEN GOTO 1835
1828  FOR I=1 TO JK
1831  TIM(I-1)=TIM(I)
1832  MAXS(I-1)=MAXS(I)
1833  NEXT I
1834  K=JK
1835  ! DISP "WHICH CHARACTER YOU PREFER TO USING IN PLOTTING THE DATA?"
1837  ! INPUT C$
1839  MOVE TIM(0),MAXS(0)
1840  FOR I=0 TO K-1
1920  DRAW TIM(I),MAXS(I)
1930  ! LABEL C$
1940  NEXT I
```

```
1960  PEN UP
1961  !
1962  GOSUB LEASTSQR
1980  ASSIGN# 5 TO  *
2000  ASSIGN# 6 TO  *
2020  END
2900  !
2910  !
2920  !      FOLLOWING SUBROUTINE IS DESIGNED TO APPLY THE LEAST
2922  !      SQUARE METHOD IN THE ABOVE DATA AND THE PLOT THE
2924  !      BEST FIT STRAIGHT LINE, PRINT OUT THE SLOPE AND
2926  !      THE CORRELATION COEFFICIENT ON THE PLOT.
2928  !      FORMULA USED PLEASE
2930  !
3000  LEASTSQR:
3040  REAL Y,XY,X1,X2,TAVE,YAVE,VARX,VARY,COVXY
3060  LET Y=0
3080  !        Y IS THE SUMMATION OF Y(I) VALUE
3100  LET XY=0
3120  !        XY IS THE SUMMATION OF X(I)*Y(I)
3140  LET X1=0
3160  !        X1 IS THE SUMMATION OF X(I)
3180  LET X2=0
3200  !        X2 IS THE SUMMATION OF X(I) 2
3220  FOR I=0 TO K-1
3240  Y=Y+MAXS(I)
3260  XY=XY+TIM(I)*MAXS(I)
3280  X1=X1+TIM(I)
3300  X2=X2+TIM(I)^2
3320  NEXT I
3340  B=(X2*Y-X1*XY)/(K*X2-X1^2)
3350  !
3351  !
3352  !       A IS THE SLOPE OF THE FITTED STRAIGHT LIGHT
3360  A=(K*XY-X1*Y)/(K*X2-X1^2)
3370  !
3371  !
3372  !       B IS THE INTERCEPT TO Y AXIS
3380  PRINT "THE SLOPE A=";A
3400  PRINT "THE Y-INTERCEPT B=";B
3420  YAVE=(MAXS(0)+MAXS(K-1))/2
3421  !
3422  !       YAVE IS THE AVERAGE VALUE FOR THE LOG VOLTAGE
3423  !
3440  TAVE=(TIM(0)+TIM(K-1))/2
3441  !
3442  !       TAVE IS THE AVERAGE VALUE FOR THE TIME VARIABLE
3443  !
3460  COVXY=0
3461  !
3480  !       COVXY IS THE COVARIANCE OF  TIME AND VOLTAGE (LN)
3481  !
3500  VARX=0
3520  !       VARX IS THE VARIANCE OF TIME VARIABLE
3521  !
3540  VARY=0
3560  !       VARY IS THE VARIANCE OF VOLTAGE(LN) VARIABLE
3561  !
3562  DIM YL(100)
3580  FOR I=0 TO K-1
```

```
3600  !
3620  COVXY=COVXY+(TIM(I)-TAVE)*(MAXS(I)-YAVE)
3640  !
3660  VARX=VARX+(TIM(I)-TAVE)^2
3680  !
3700  VARY=VARY+(MAXS(I)-YAVE)^2
3720  !
3740  YL(I)=A*TIM(I)+B
3760  !       YL IS THE VALUE FITTED ON THE STRAIGHT LINE
3761  !
3780  NEXT I
3800  PEN 2
3820  MOVE TIM(0),YL(0)
3840  FOR I=0 TO K-1
3860  DRAW TIM(I),YL(I)
3880  NEXT I
3900  CORCOE=COVXY/SQR (VARX*VARY)
3910  !
3920  !       CORCOE IS THE CORRELATION COEFFICIENT
3940  !
3960  PRINT "CORRELATION COEFFICIENT IS ";CORCOE
3980  PEN 1
3990  DEG
3991  LDIR 0
3994  !
3996  !     FOLLOWING PRINT OUT THE SLOPE AND COORELATION COEFFICIENT
3998  !     ON THE PLOT
3999  !
4000  MOVE XMIN+80,1
4002  !
4004  !     LABLE ALWAYS STARTS FROM THE XMIN+80 IN X COORDINATES
4006  !
4020  LABEL USING 4021 ; "SLOPE =",A
4021  IMAGE 7A,DDD.DDDD
4040  MOVE XMIN+80,2
4060  LABEL USING 4061 ; "CORRELATION COEFF=",CORCOE
4061  IMAGE 19A,DDD.DDDD
4062  PEN UP
4080  RETURN
```

```
800   ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
810   ! !                                                        !!
820   ! !                                                        !!
830   ! !               PROGRAM : AVERAGE                        !!
840   ! !                                                        !!
850   ! !      THIS PROGRAM IS DESIGNED TO AVERAGE               !!
860   ! !      THE DATA SETS TO GET A AVERAGED                   !!
870   ! !      WAVEFORM DATA.                                    !!
880   ! !                                                        !!
890   ! !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
1000  DIM VDAT$[25],VDATA$[25],VDAT1$[25]
1020  DIM V1(1500),V2(1500),V3(1500)
1040  DISP "WHAT IS THE ORIGINAL DATA FILE ?  DAT#"
1060  INPUT VDAT$
1080  DISP "WHAT IS THE NEW DATA FILE ?  DATA#"
1100  INPUT VDATA$
1120  DISP "WHAT IS THE AVERAGED DATA FILE ? DAT1#"
1140  INPUT VDAT1$
1160  ASSIGN# 1 TO  VDAT$
1180  ASSIGN# 2 TO  VDATA$
1200  CREATE VDAT1$,8,110
1220  ASSIGN# 3 TO  VDAT1$
1230  !
1231  !    N IS THE NUMBER HOW MANY DATA SET BEING AVERGED
1232  !
1240  DISP "WHAT IS  YOUR AVERAGE No. N ?"
1260  INPUT N
1261  !
1262  !   AVERAGE ONLY APPLY TO THE SAME ARRAY NO.
1263  !
1270  FOR I=522 TO 621
1271  READ# 1 ; V1(I)
1272  NEXT I
1274  FOR I=522 TO 621
1275  READ# 2 ; V2(I)
1276  NEXT I
1280  FOR I=522 TO 621
1300  !
1301  !   RUNNING AVERAGE IS ADOPTED
1302  !
1340  V3(I)=((N-1)*V1(I)+V2(I))/N
1360  PRINT# 3 ; V3(I)
1371  !
1372  !    PRINT OUT FOLLOWING VALUE AS A CHECKING PURPOSE
1373  !
1380  IF I=522 THEN 1500 ELSE 1400
1400  IF I=553 THEN 1500 ELSE 1420
1420  IF I=600 THEN 1500 ELSE 1440
1440  IF I=621 THEN 1500 ELSE 1520
1500  PRINT V1(I),V2(I),V3(I)
1520  NEXT I
1540  END
```

APPENDIX C

DECAY ENVELOPE GRAPHS FOR AGGREGATE

This appendix includes the graphs of the decay envelopes for reflection from aggregate water interface within the glass tank. Figure C.1 to C.9 show the original decay envelopes obtained from different transducer positions. The decay envelopes are also described as following data sets:

data set 42
data set 43
data set 44
data set 45
data set 46
data set 47
data set 48
data set 49
data set 50

Figures C.10 to C.18 are the decay envelopes resulted from the running average method. They are also described as following data sets:

data set DAT2
data set DAT3
data set DAT4
data set DAT5
data set DAT6
data set DAT7
data set DAT8
data set DAT9
data set DAT10

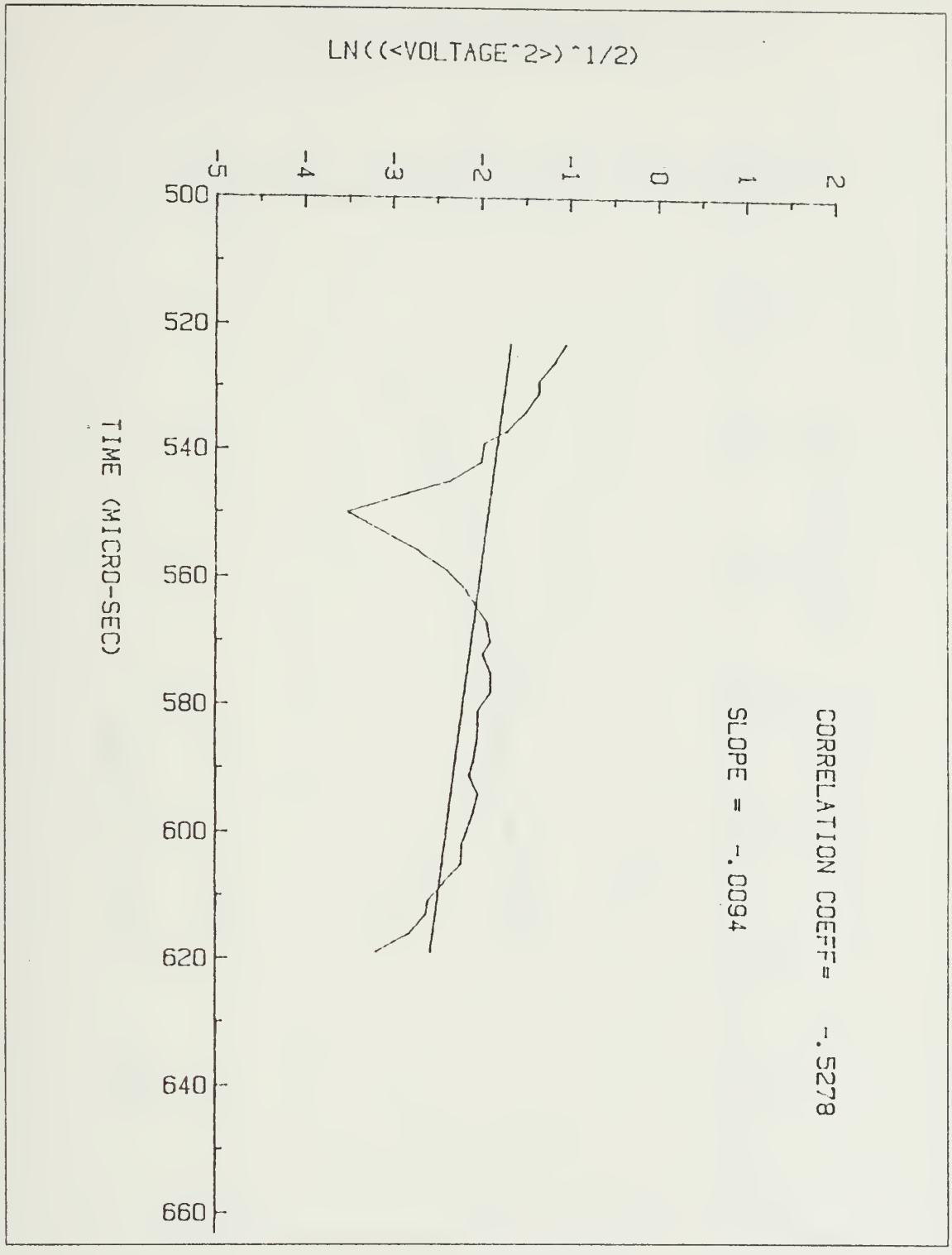

Figure C.1 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 42).

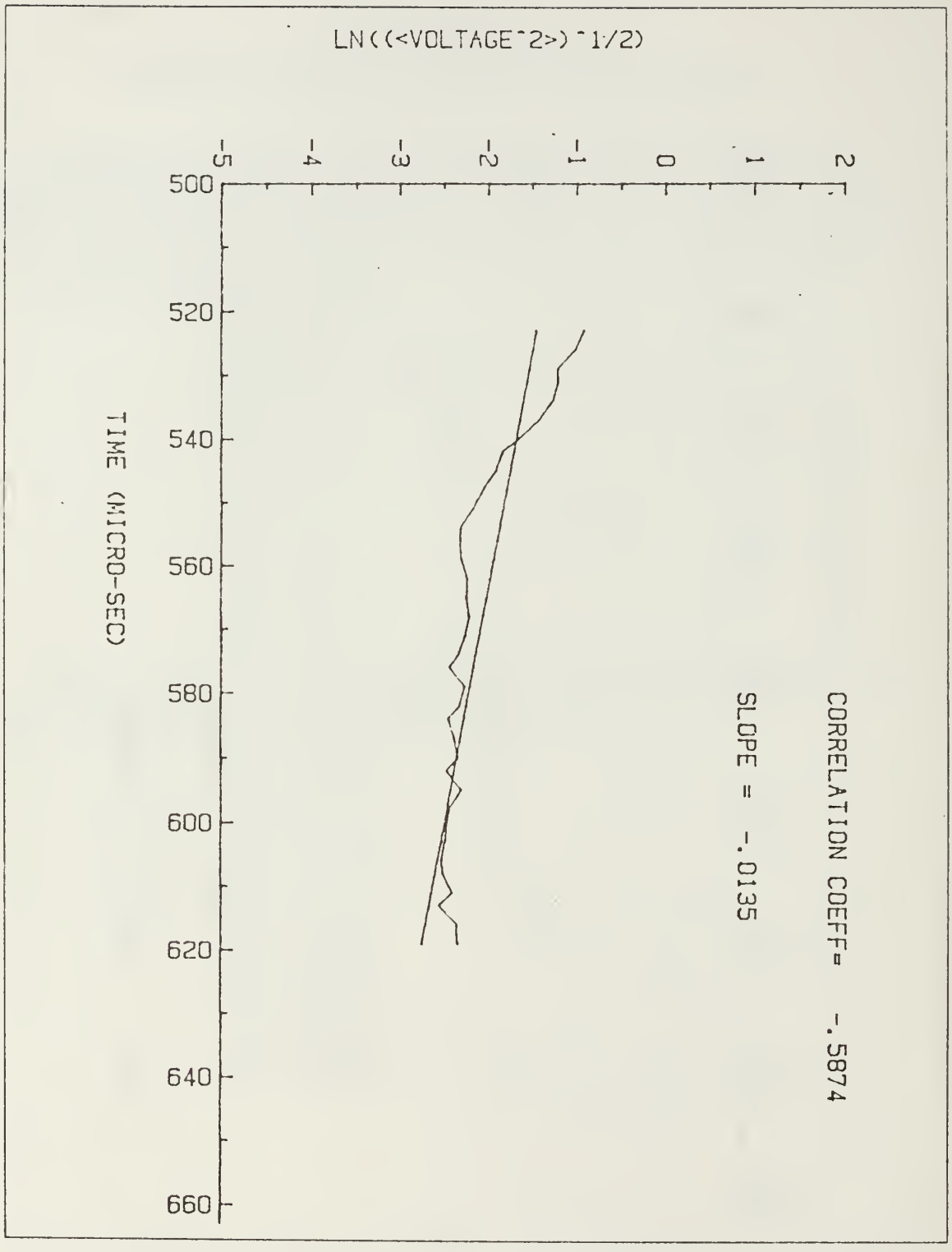

Figure C.2 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 43).

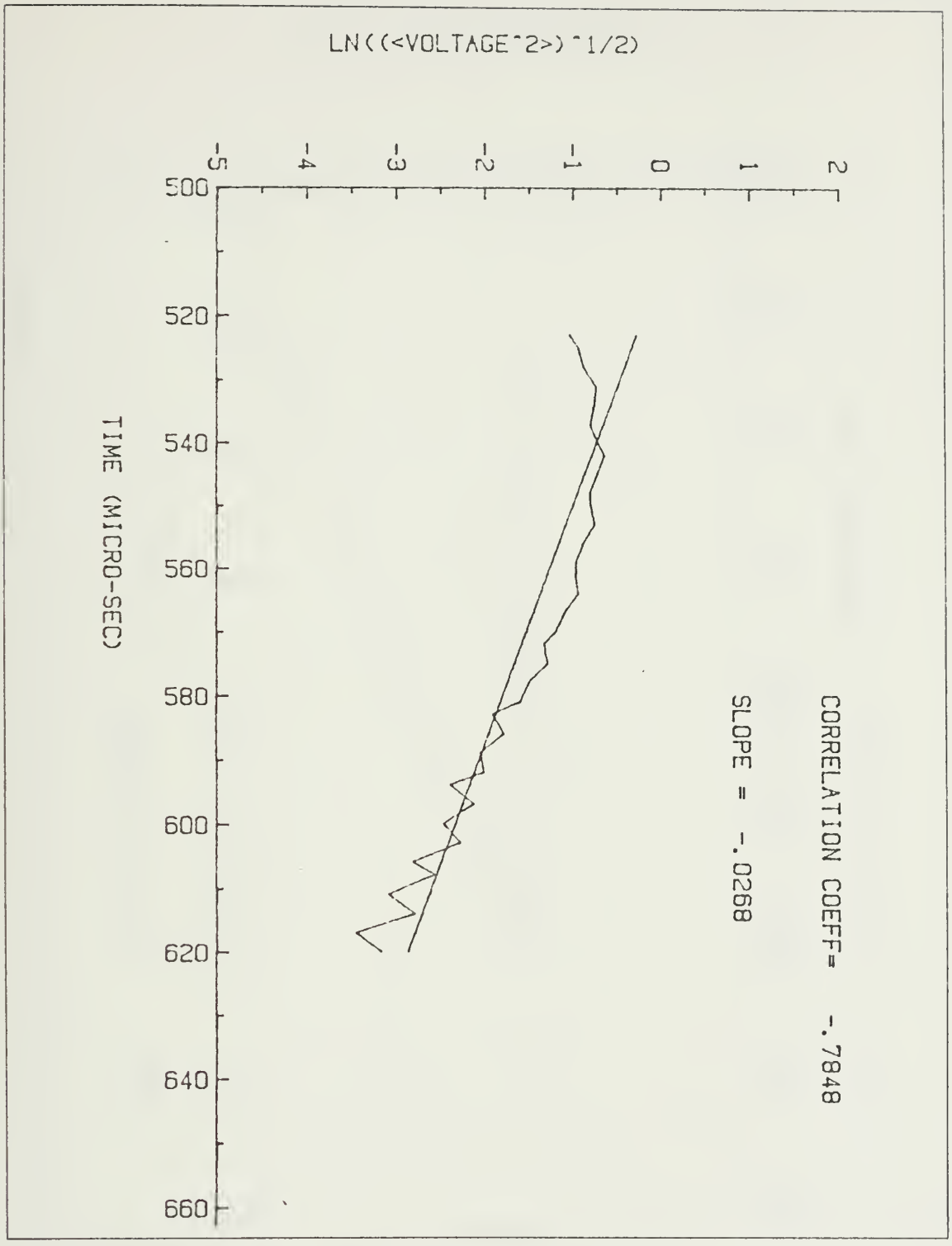

Figure C.3 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 44).

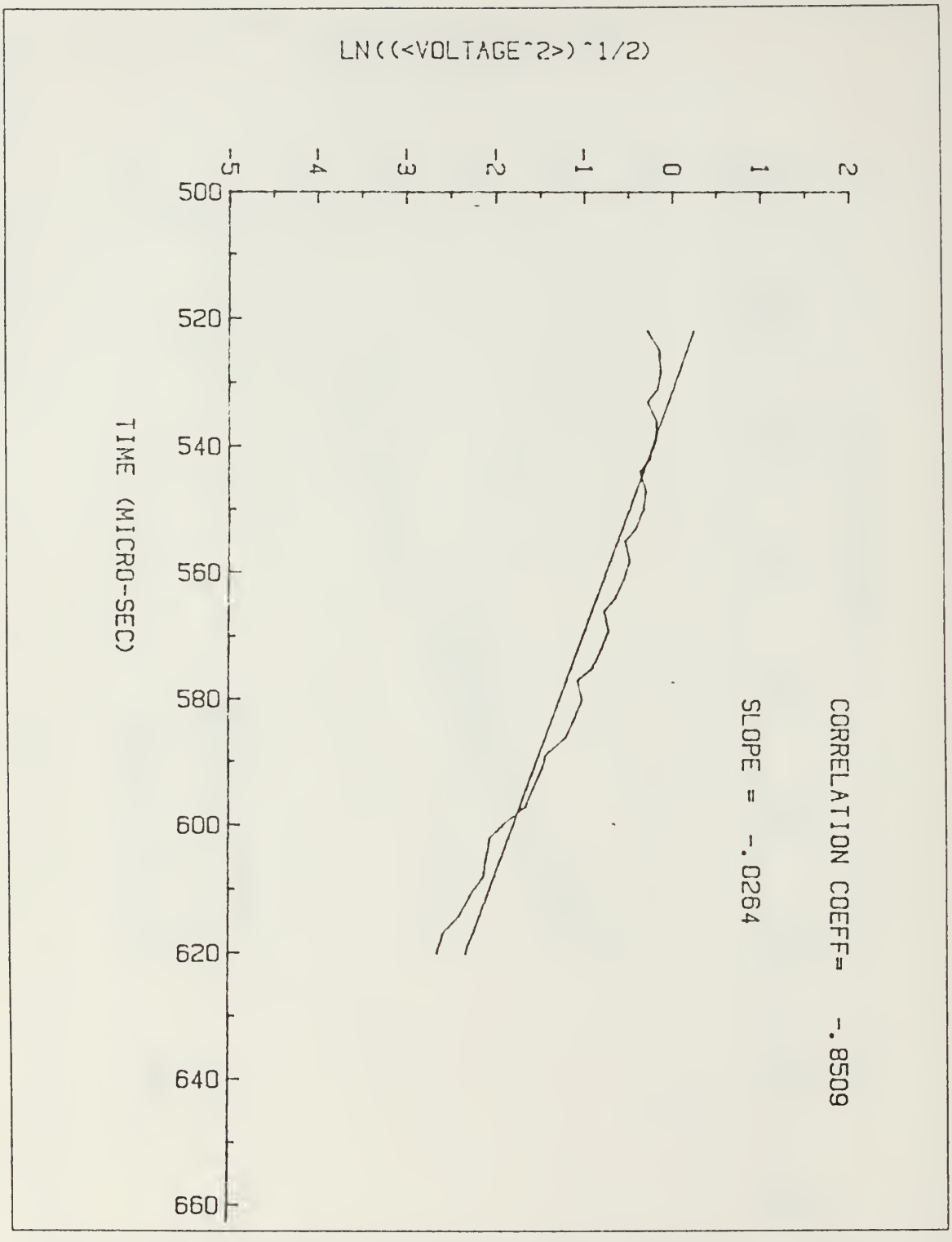

Figure C.4 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 45).

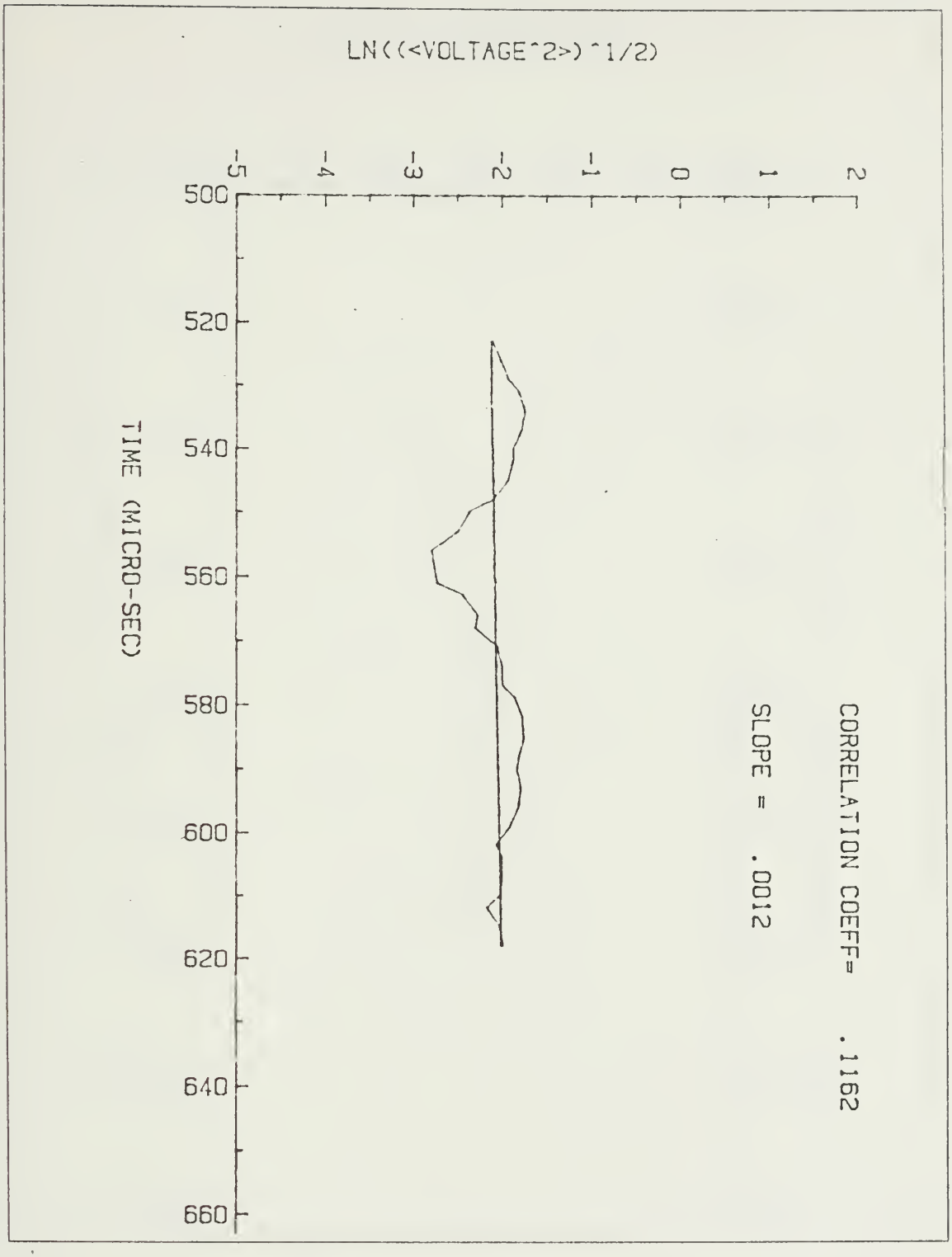

Figure C.5 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 46).

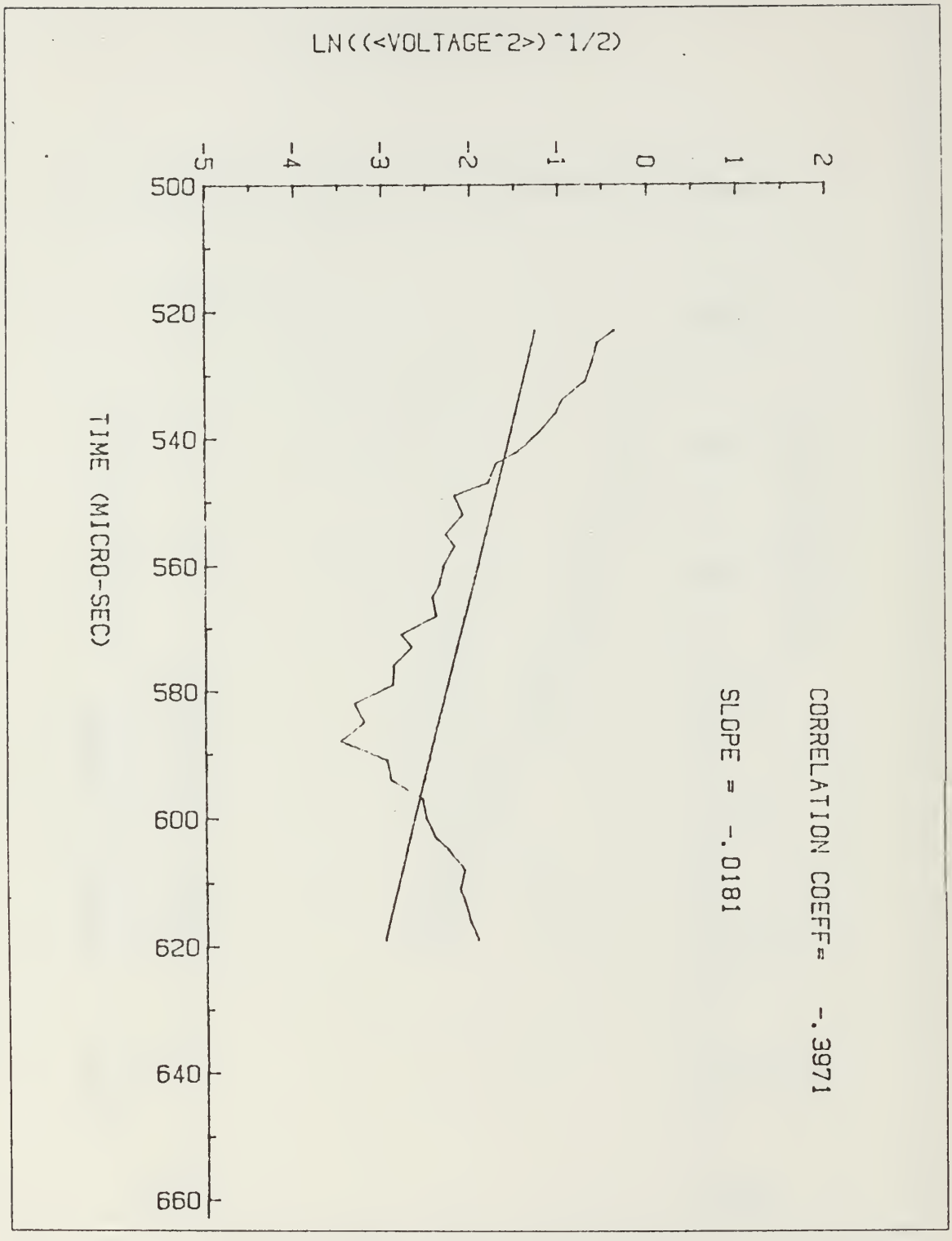

Figure C.6 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 47).

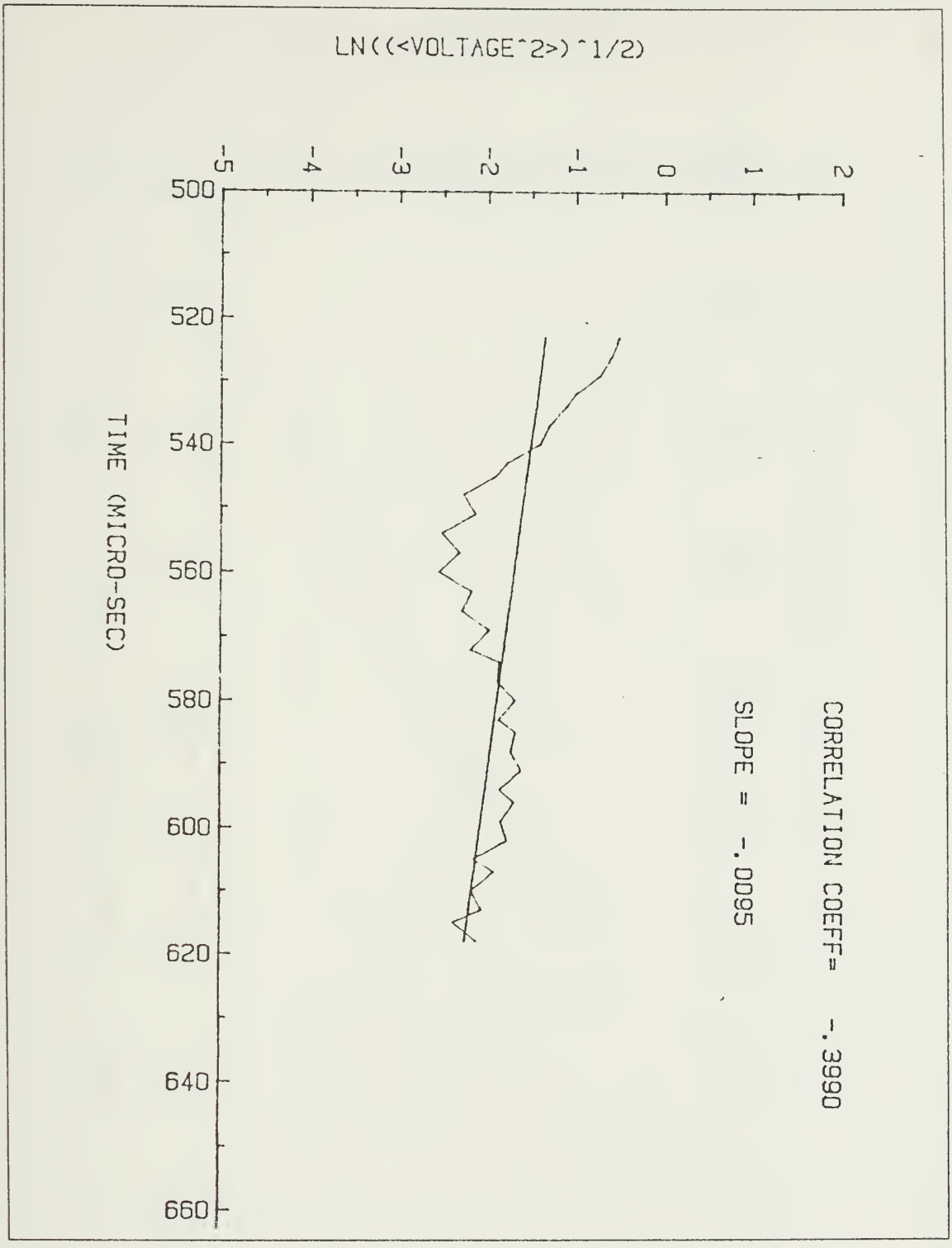

Figure C.7 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 48).

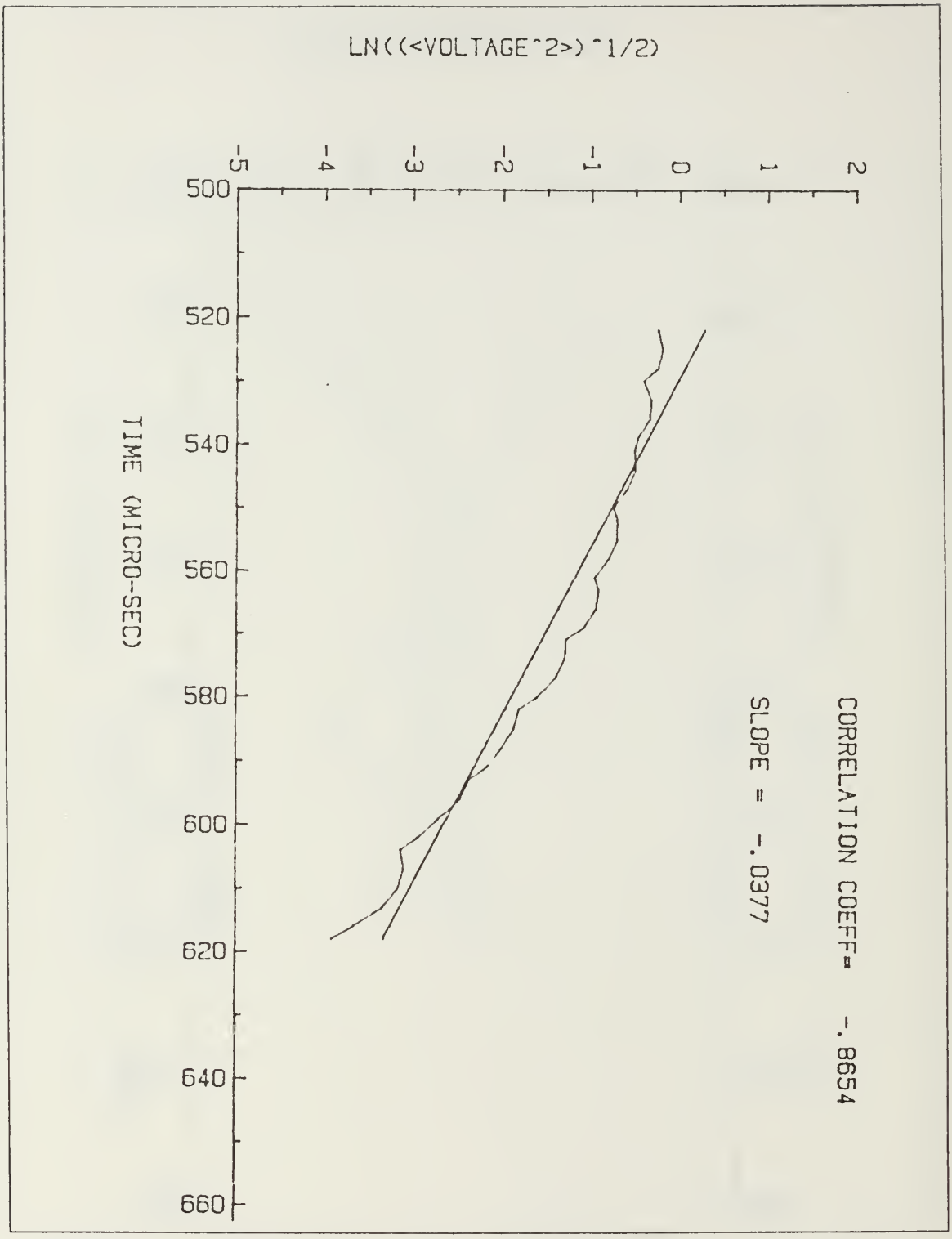

Figure C.8 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 49).

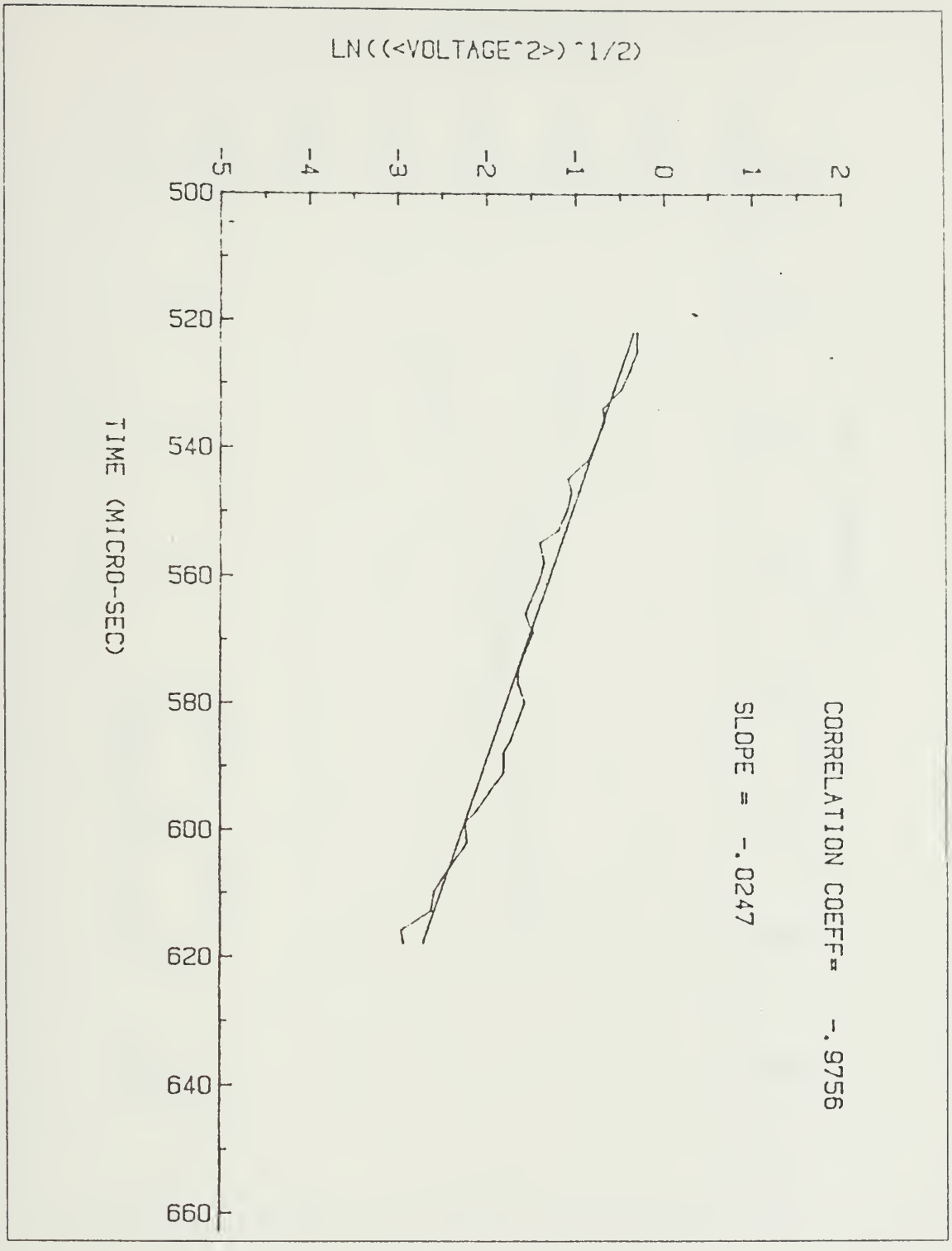

Figure C.9 Decay envelope for reflection from aggregate/water interface, transducer was 30 cm above surface (data set 50).

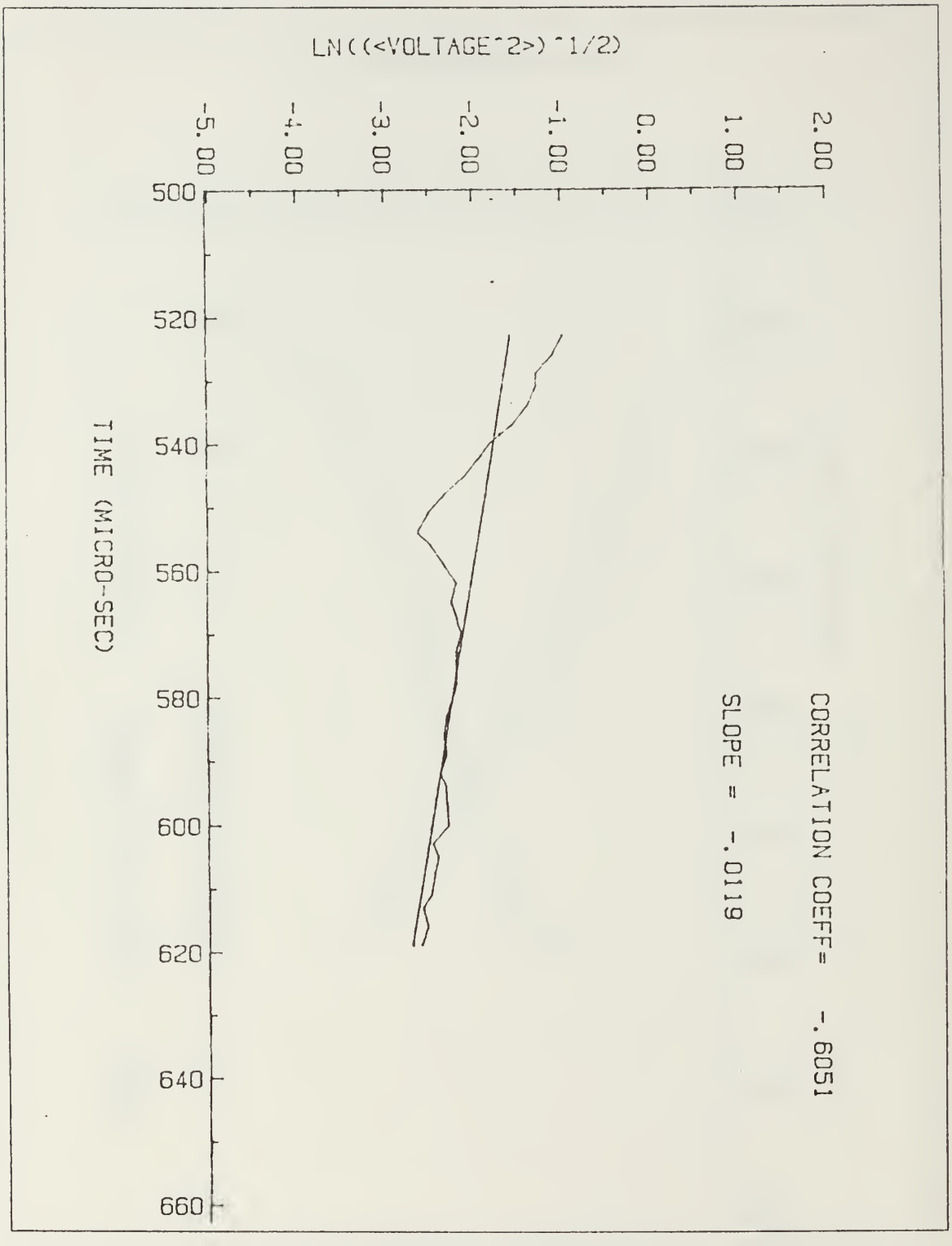

Figure C.10 Decay envelope resulted from the average of data set 42 and 43 for the aggregate/water surface (data set DAT2).

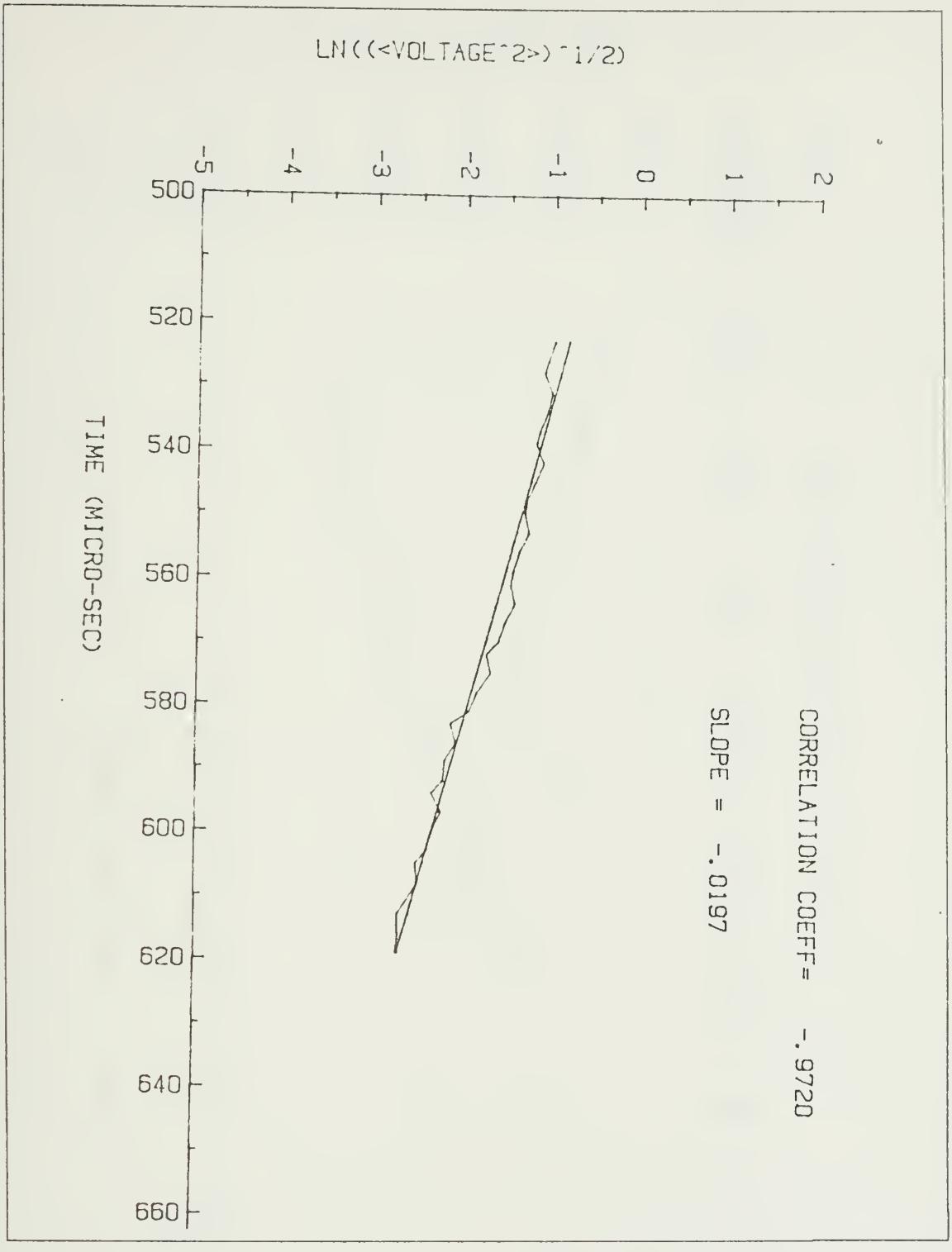

Figure C.11 Decay envelope resulted from the average from data set 42 to 44 for the aggregate/water surface (data set DAT3).

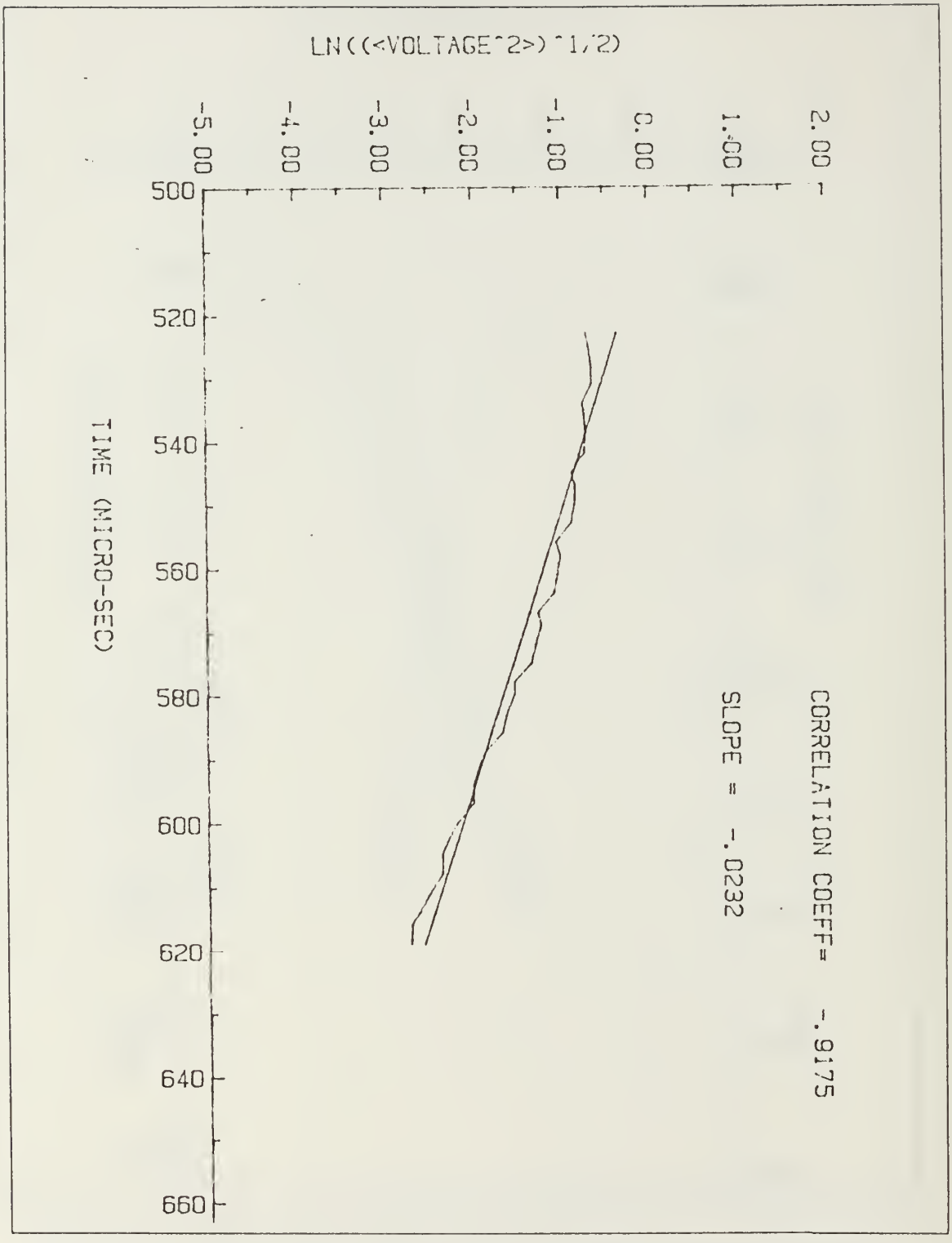

Figure C.12 Decay envelope resulted from the average from data set42 to 45 for the aggregate/water surface (data set DAT4).

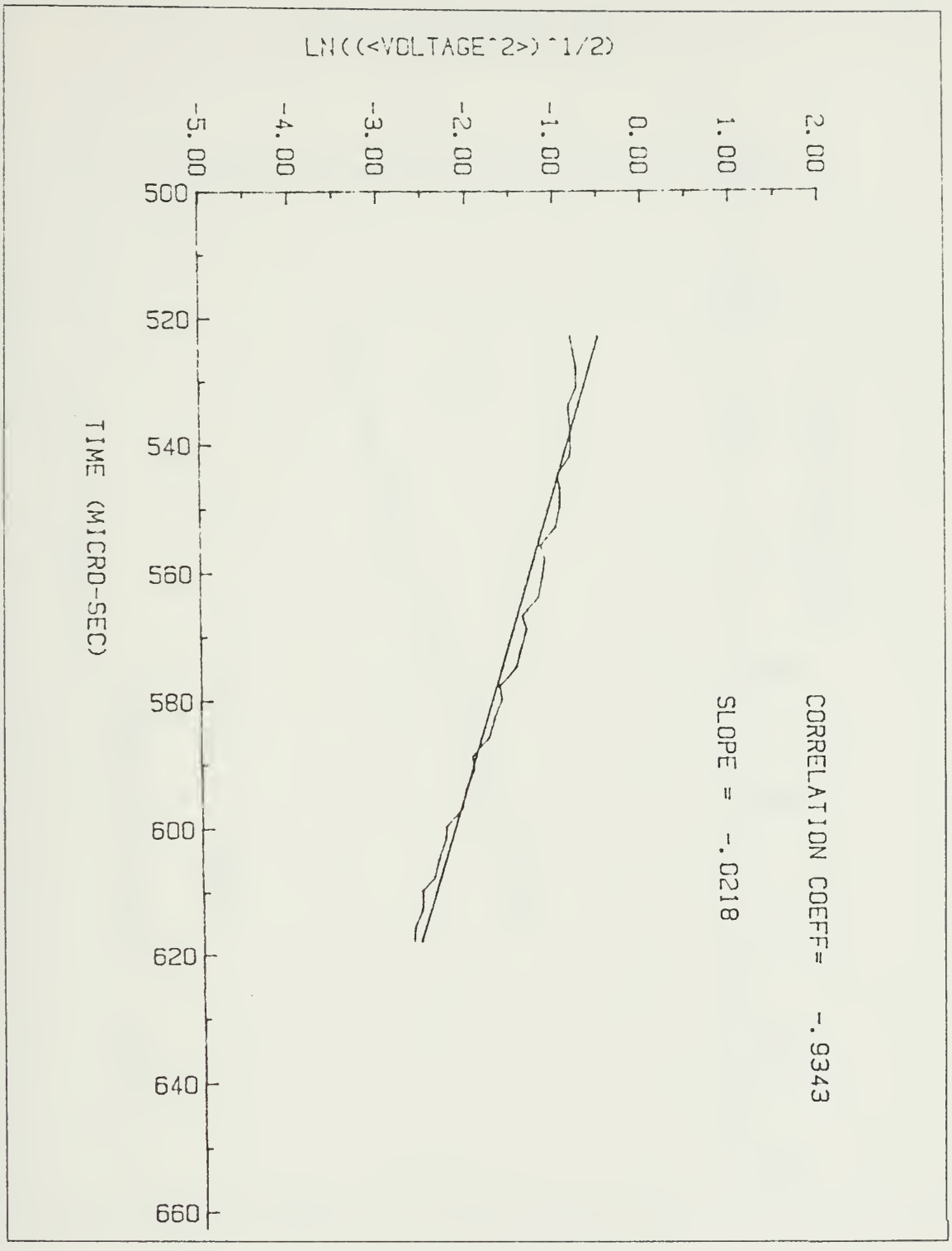

Figure C.13 Decay envelope resulted from the average from data set 42 to 46 for the aggregate/water surface (data set DAT5).

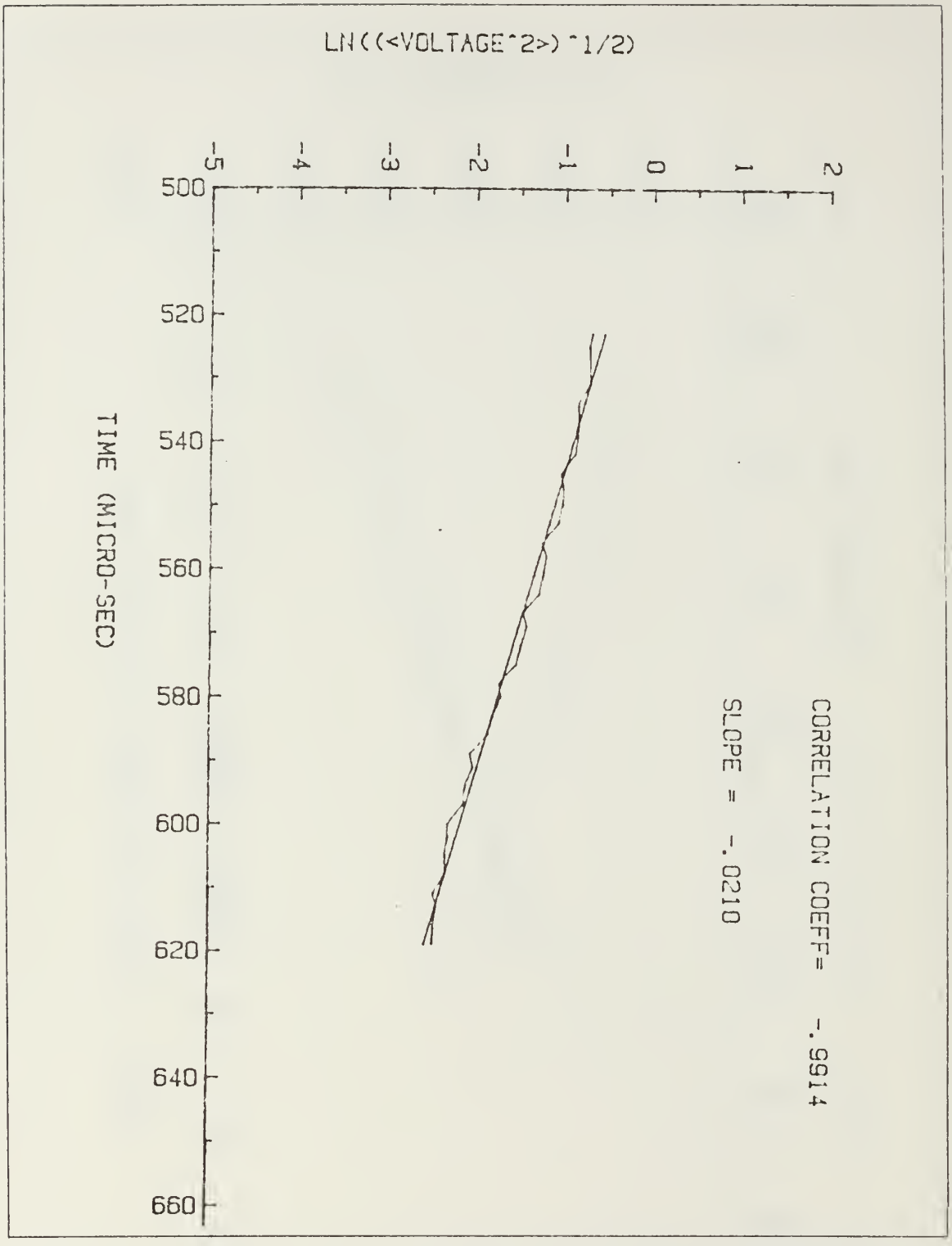

Figure C.14 Decay envelope resulted from the average from data set 42 to 47 for the aggregate/water surface (data set DAT6).

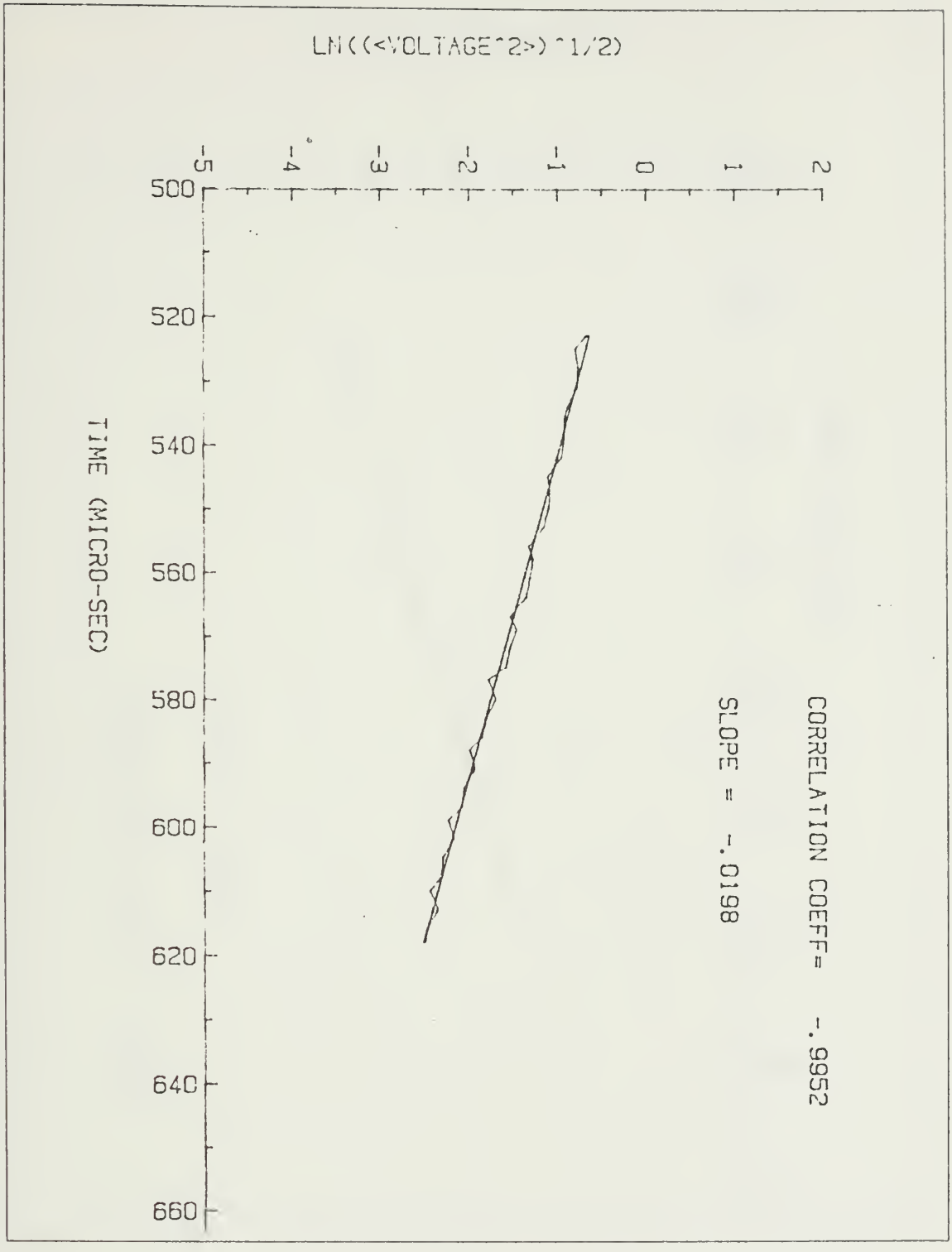

Figure C.15 Decay envelope resulted from the average from data set 42 to 48 for the aggregate/water surface (data set DAT7).

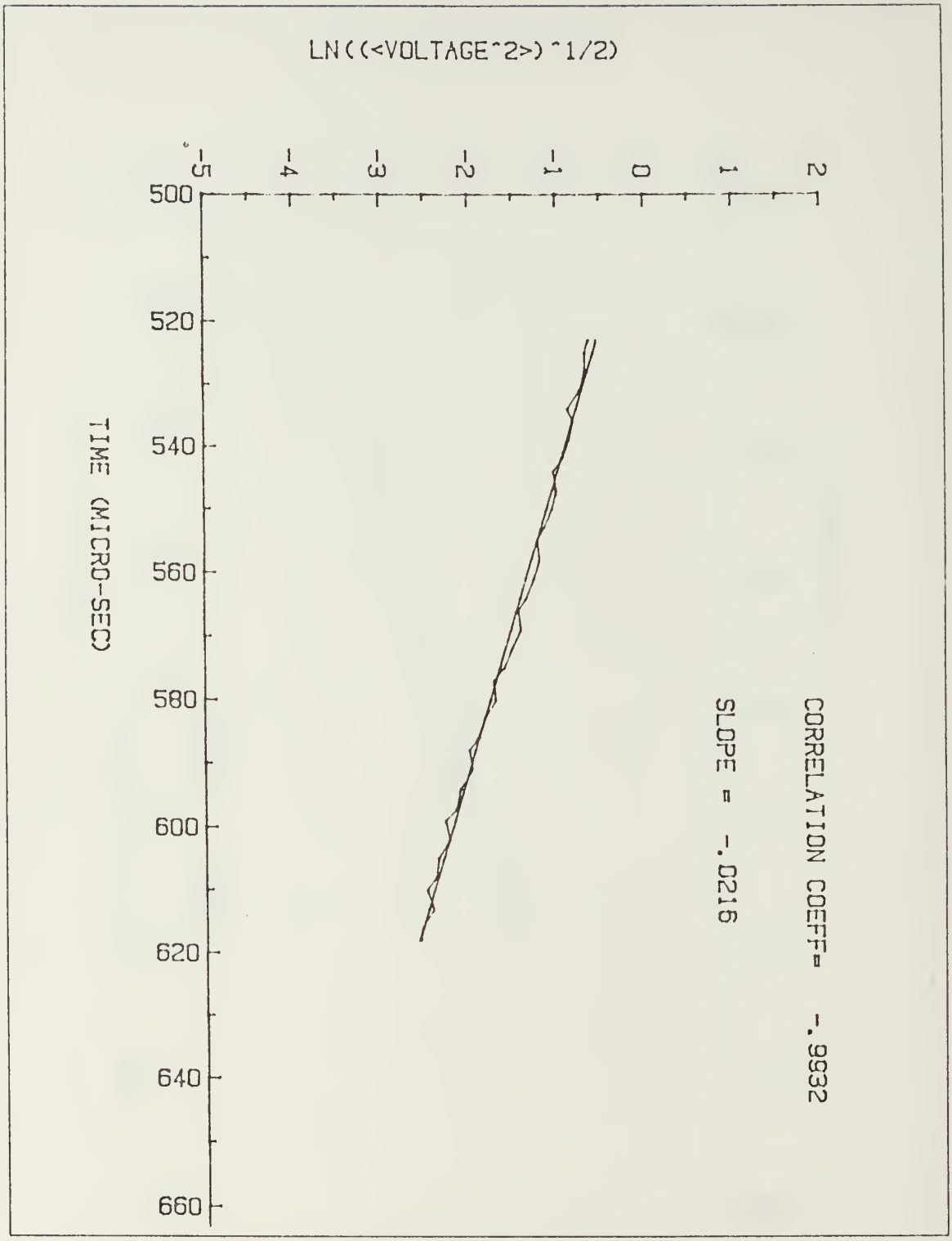

Figure C.16 Decay envelope resulted from the average from data set 42 to 49 for the aggregate/water surface (data set DAT8).

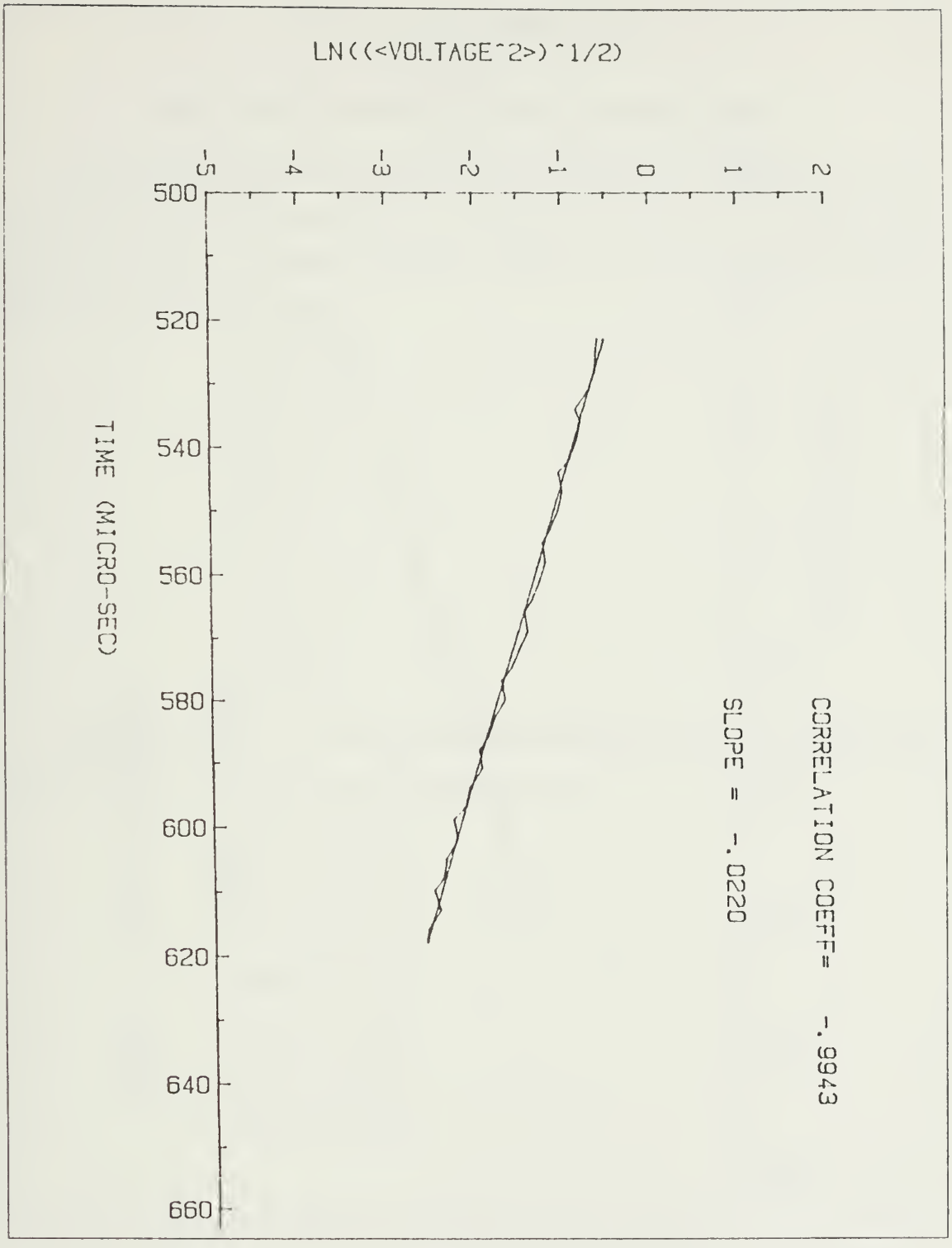

Figure C.17 Decay envelope resulted from the average from data set 42 to 50 for the aggregate/water surface (data set DA19).

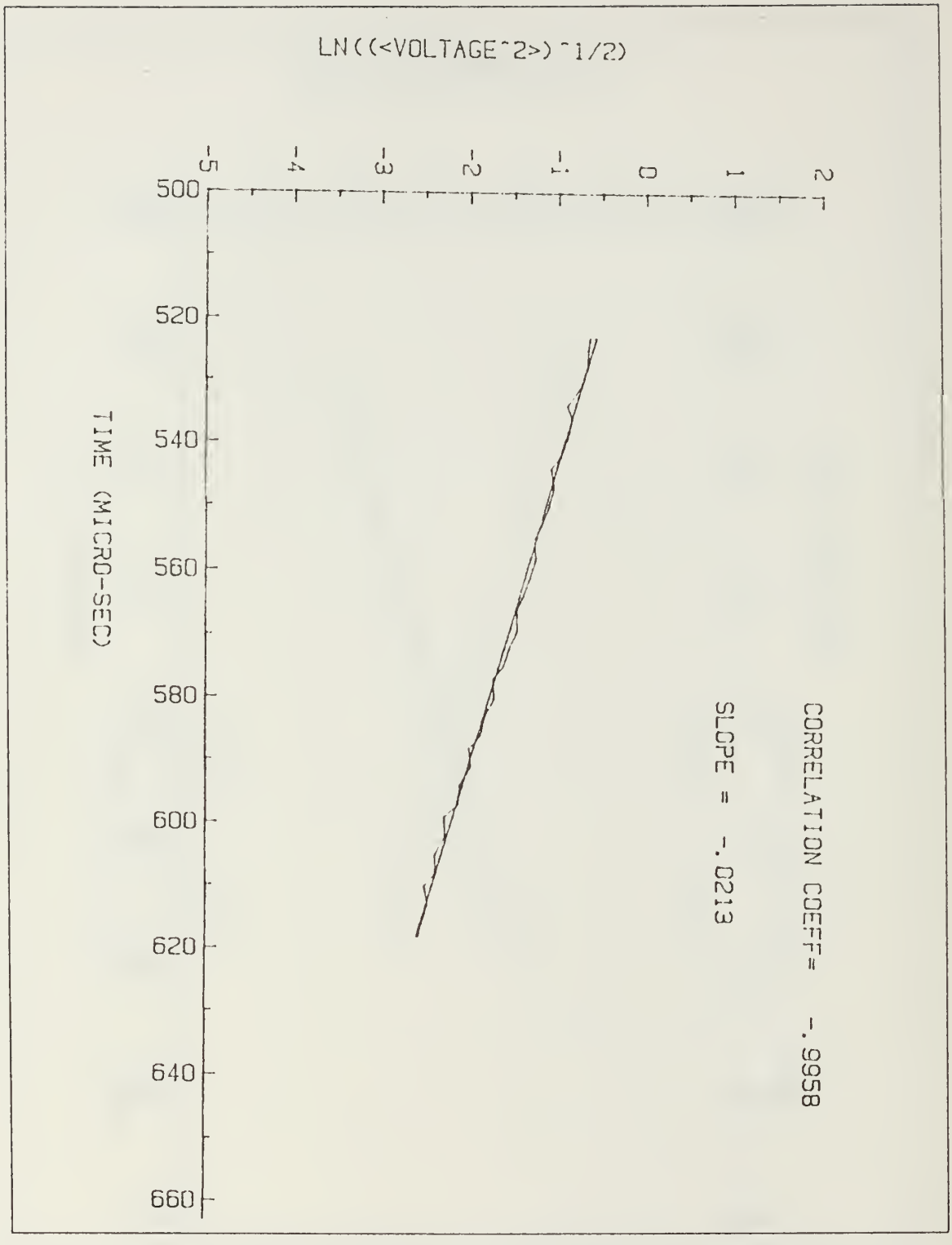

Figure C.18 Decay envelope resulted from the average from data set 42 to 51 for the aggregate/water surface (data set DAT10).

APPENDIX D

DECAY ENVELOPE GRAPHS FOR FINE SAND

This appendix includes the graphs of the decay envelopes for reflection from fine-sand, water interface within the glass tank. Figure D.1 to D.10 show the original decay envelopes obtained from different transducer positions. The decay envelopes are also described as following data sets:

data set 55
data set 56
data set 57
data set 58
data set 59
data set 60
data set 61
data set 62
data set 63
data set 64

Figures D.11 to D.19 are the decay envelopes resulted from the running average method. They are also described as following data sets:

data set DAT12
data set DAT13
data set DAT14
data set DAT15
data set DAT16
data set DAT17
data set DAT18
data set DAT19
data set DAT20

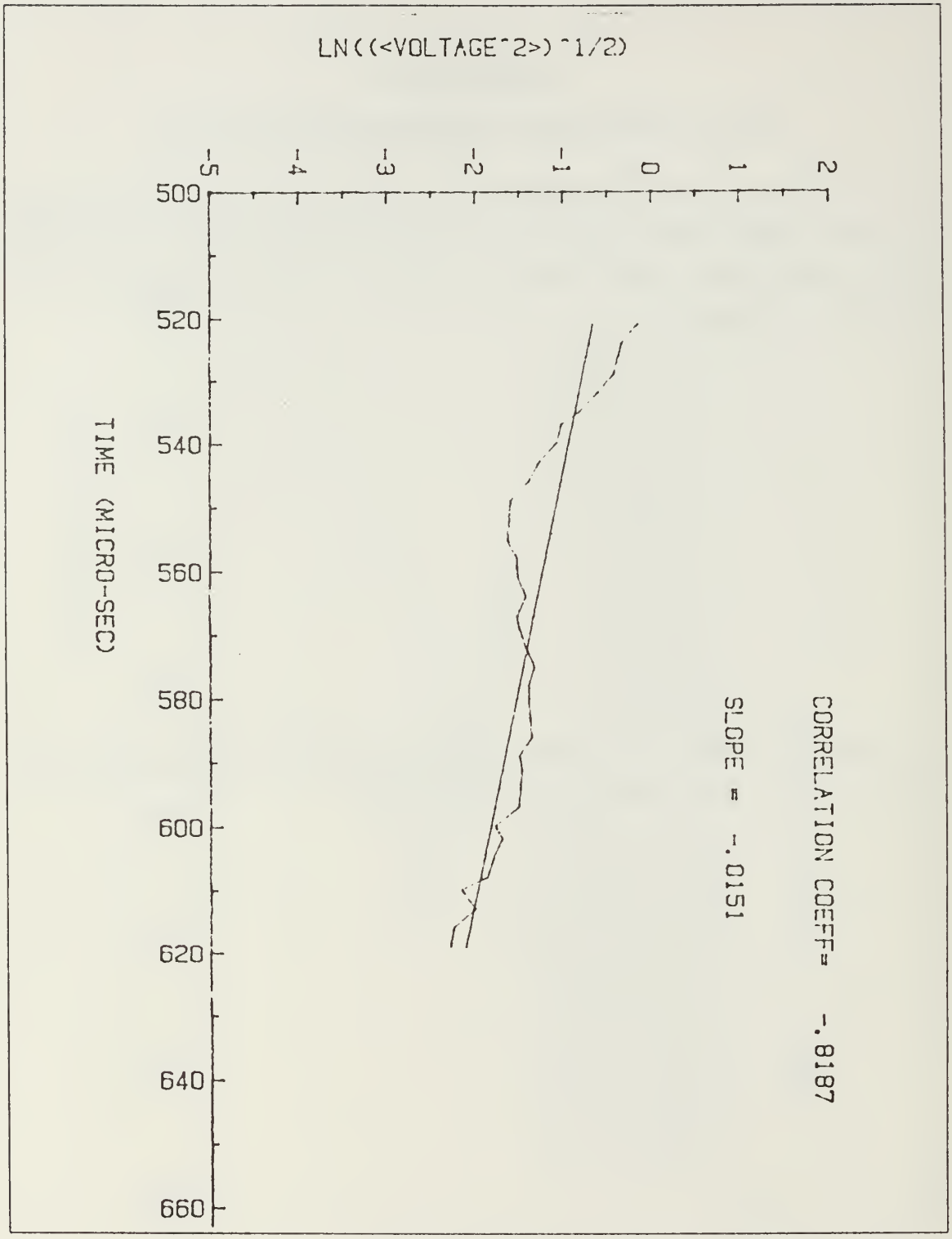

Figure D.1 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 55).

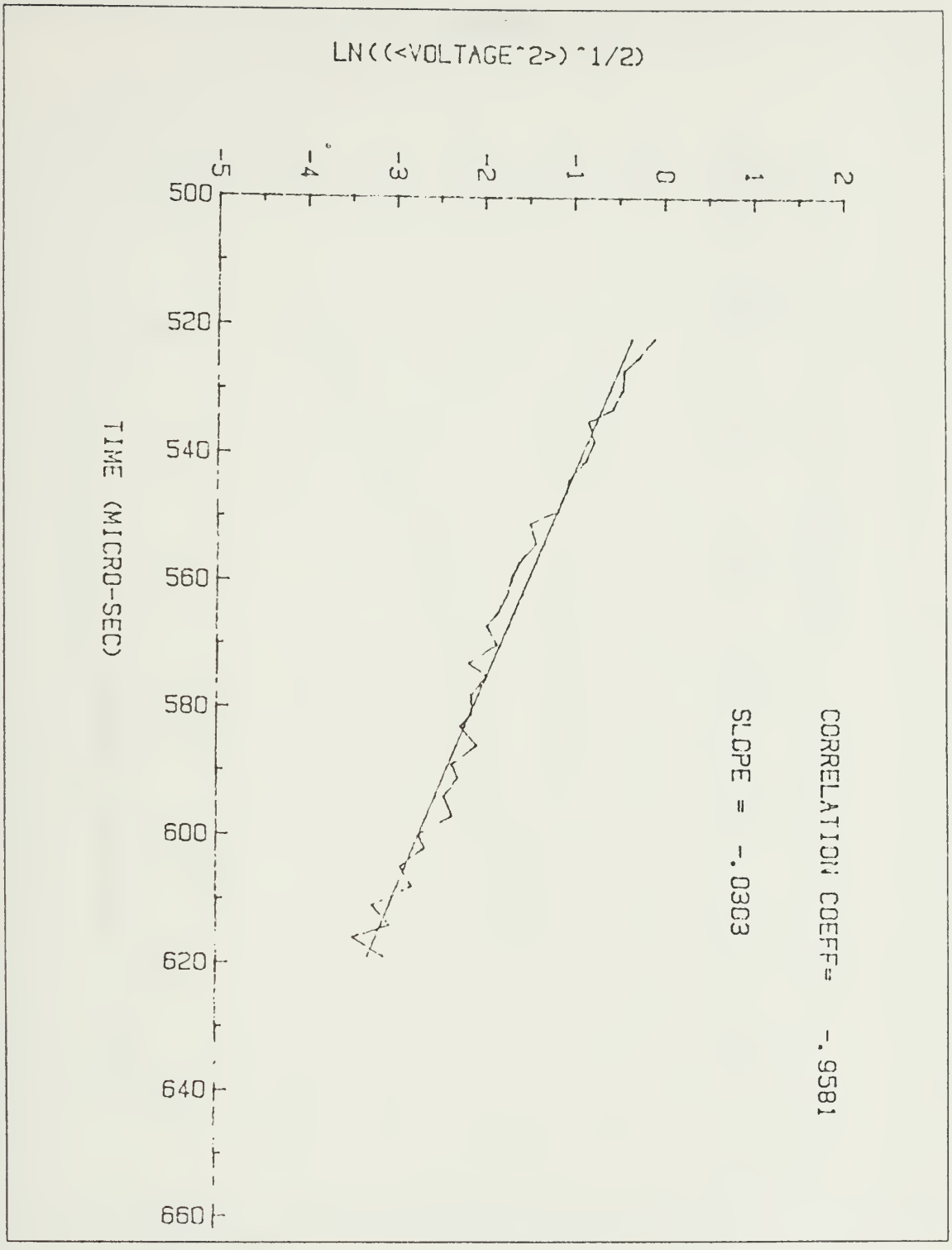

Figure D.2 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 56).

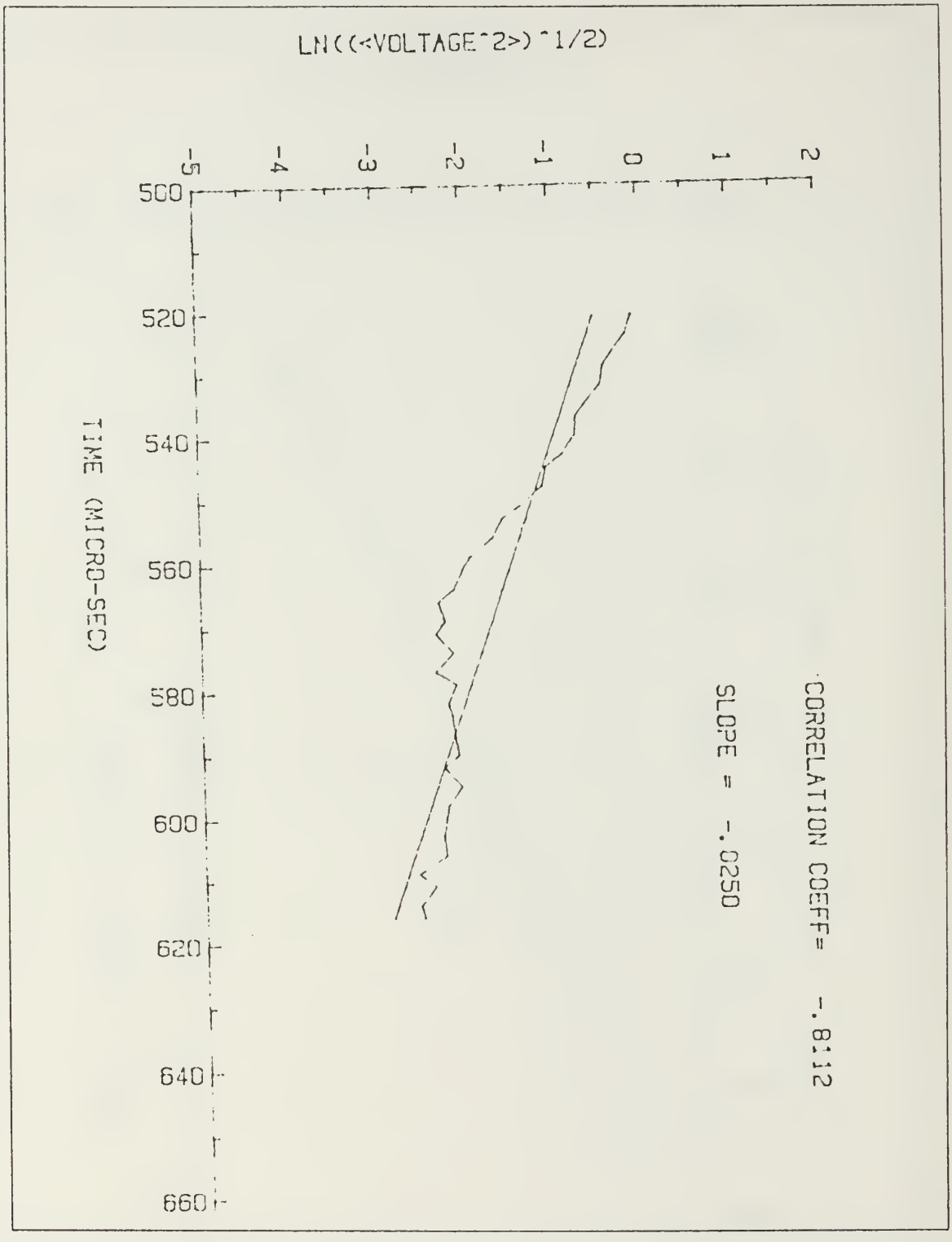

Figure D.3 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 57).

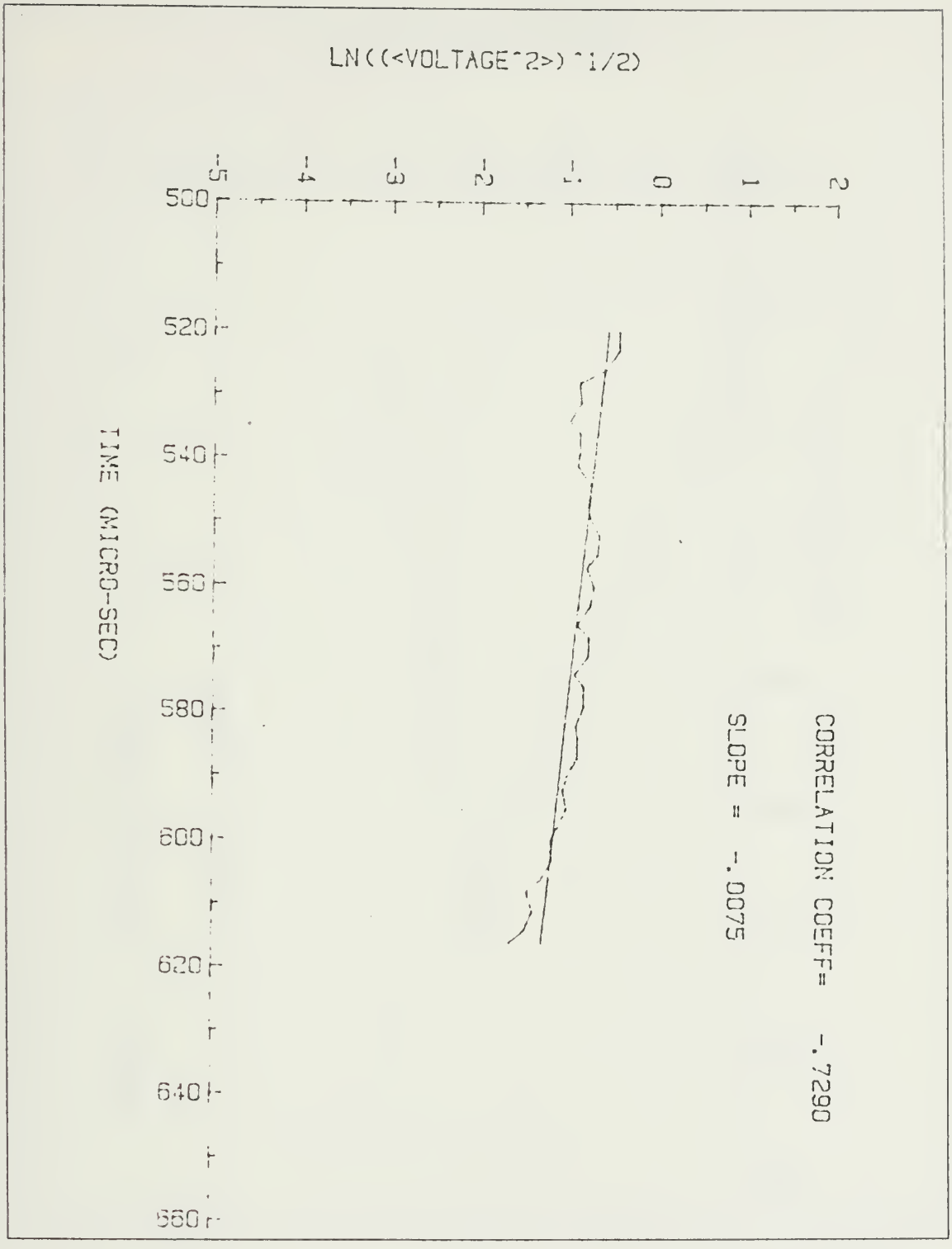

Figure D.4 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 58).

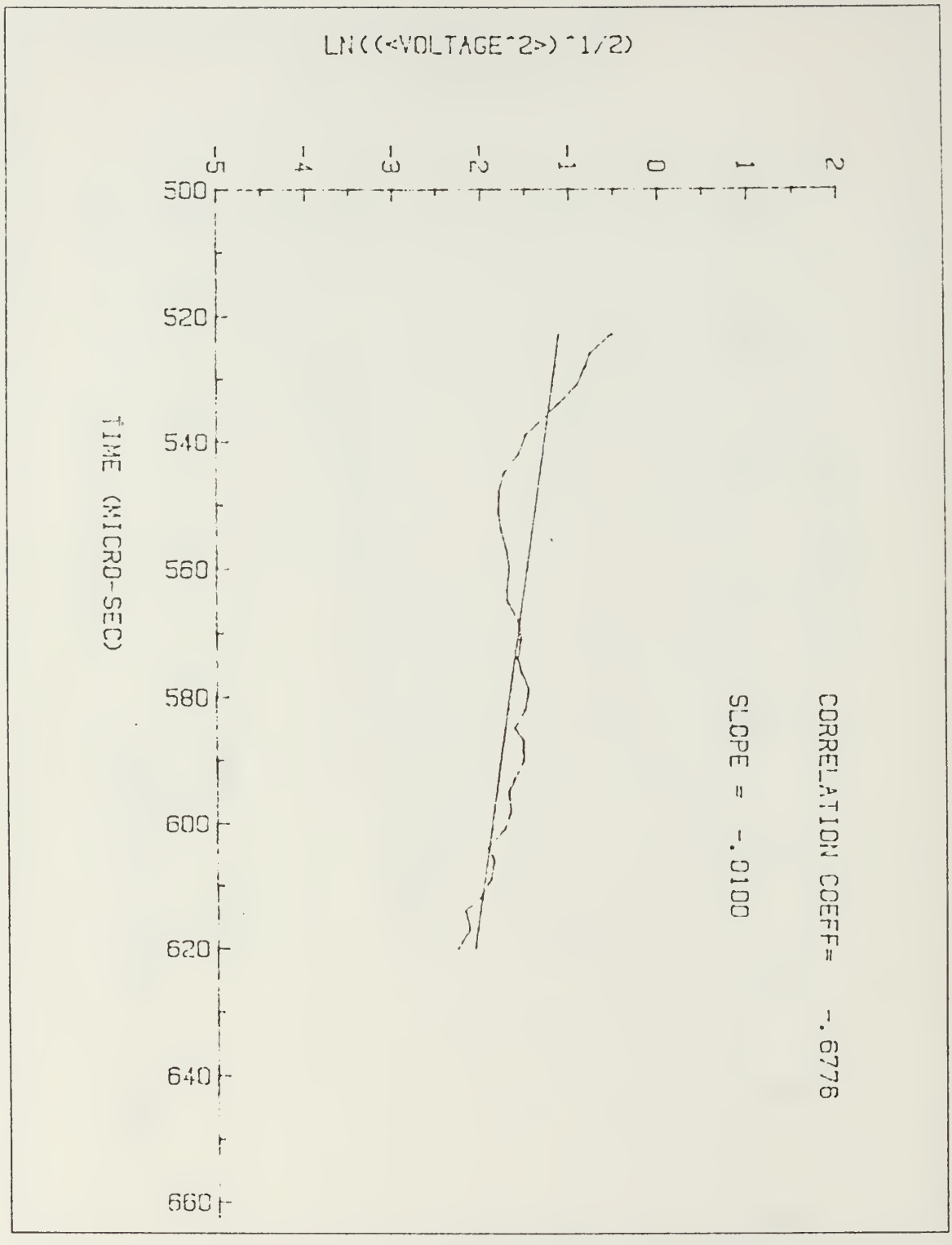

Figure D.5 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 59).

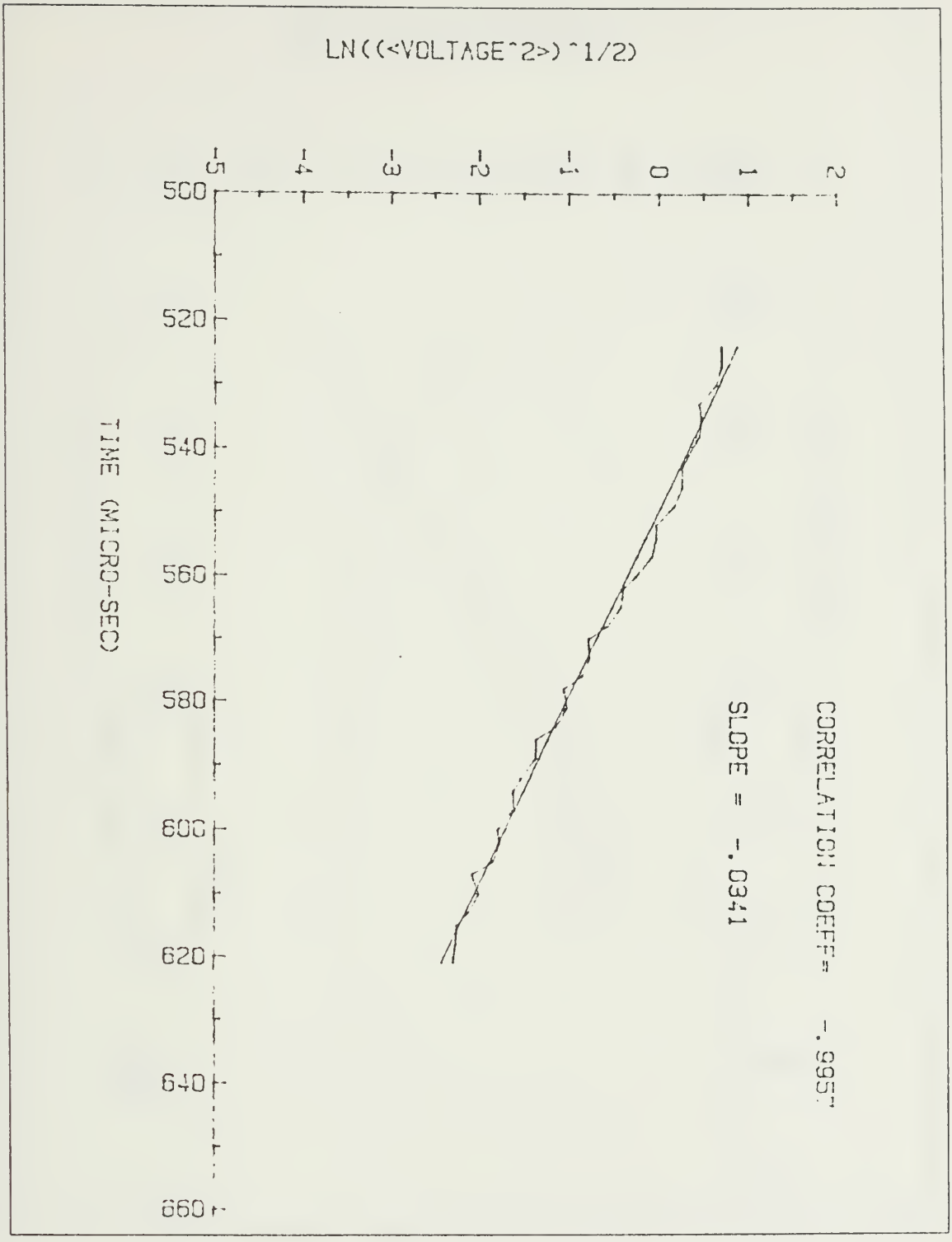

Figure D.6 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 60).

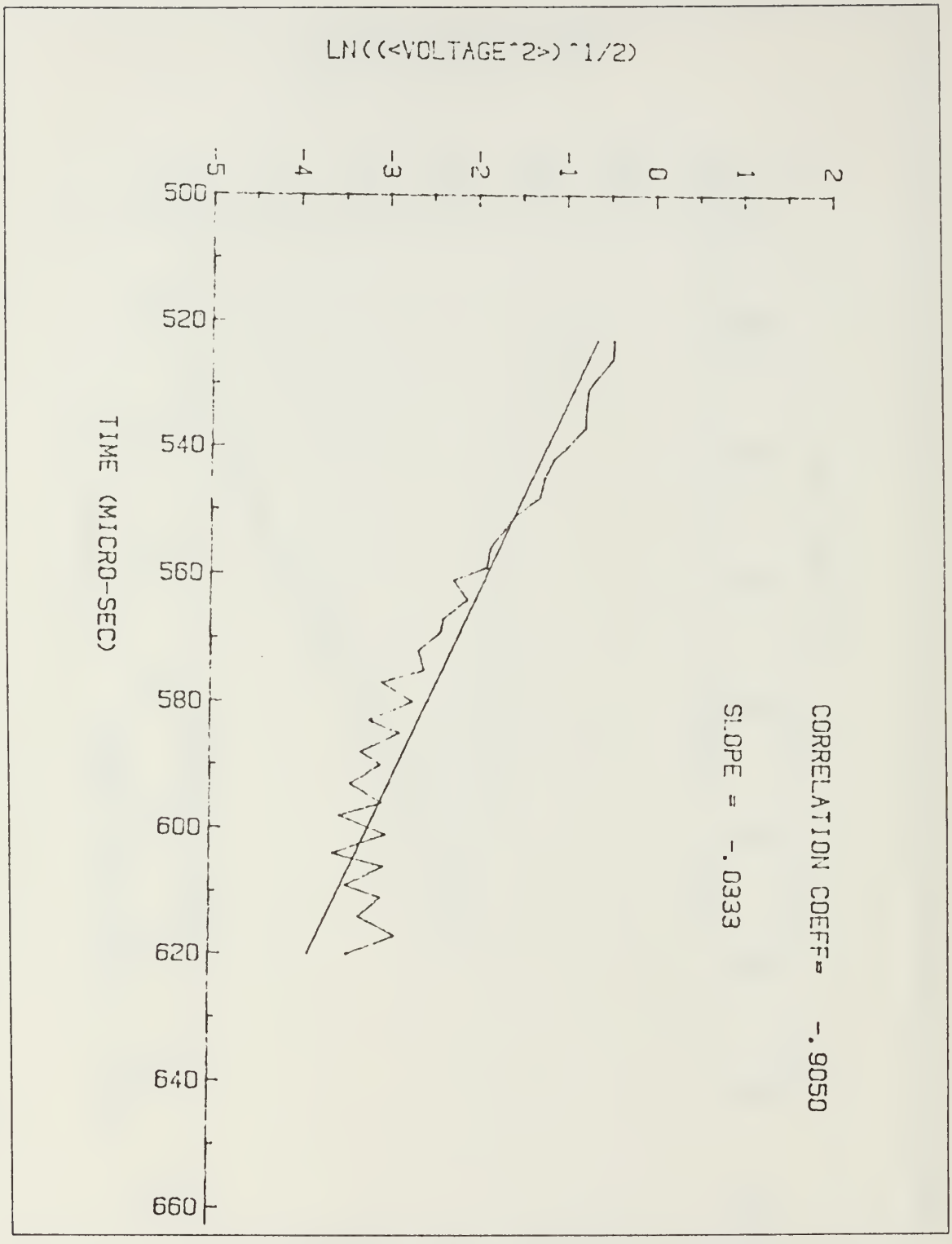

Figure D.7 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 61).

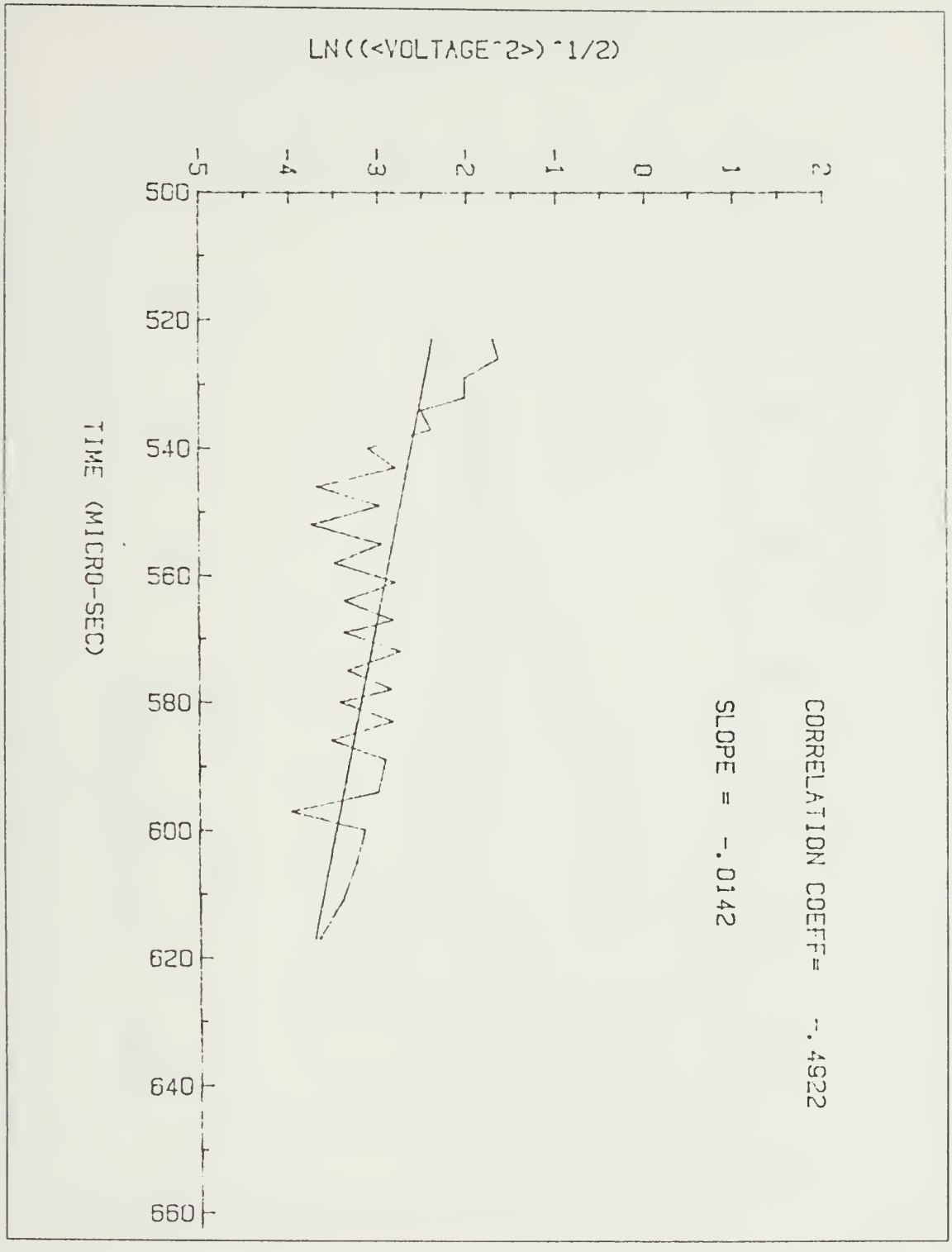

Figure D.8 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 62).

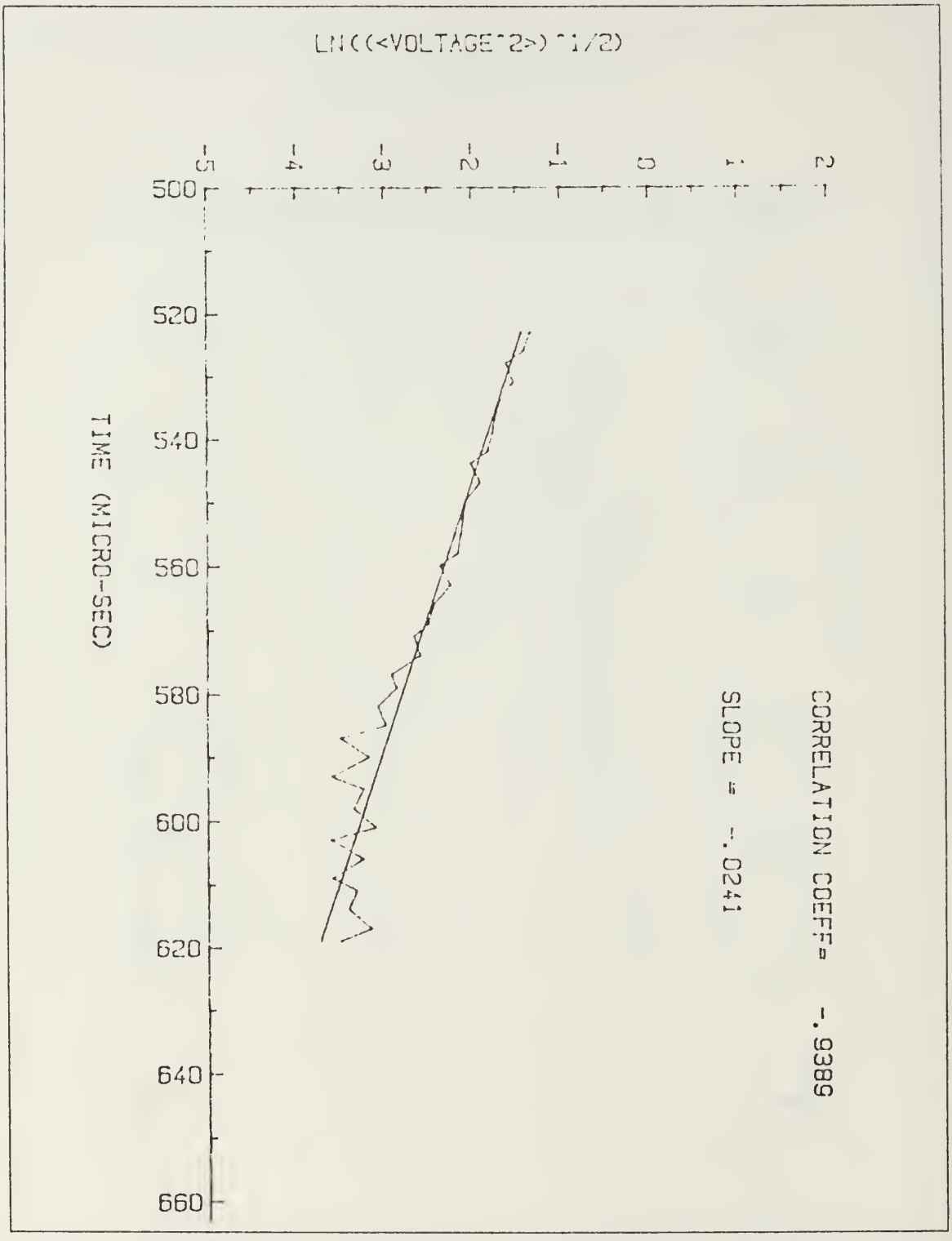

Figure D.9 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 63).

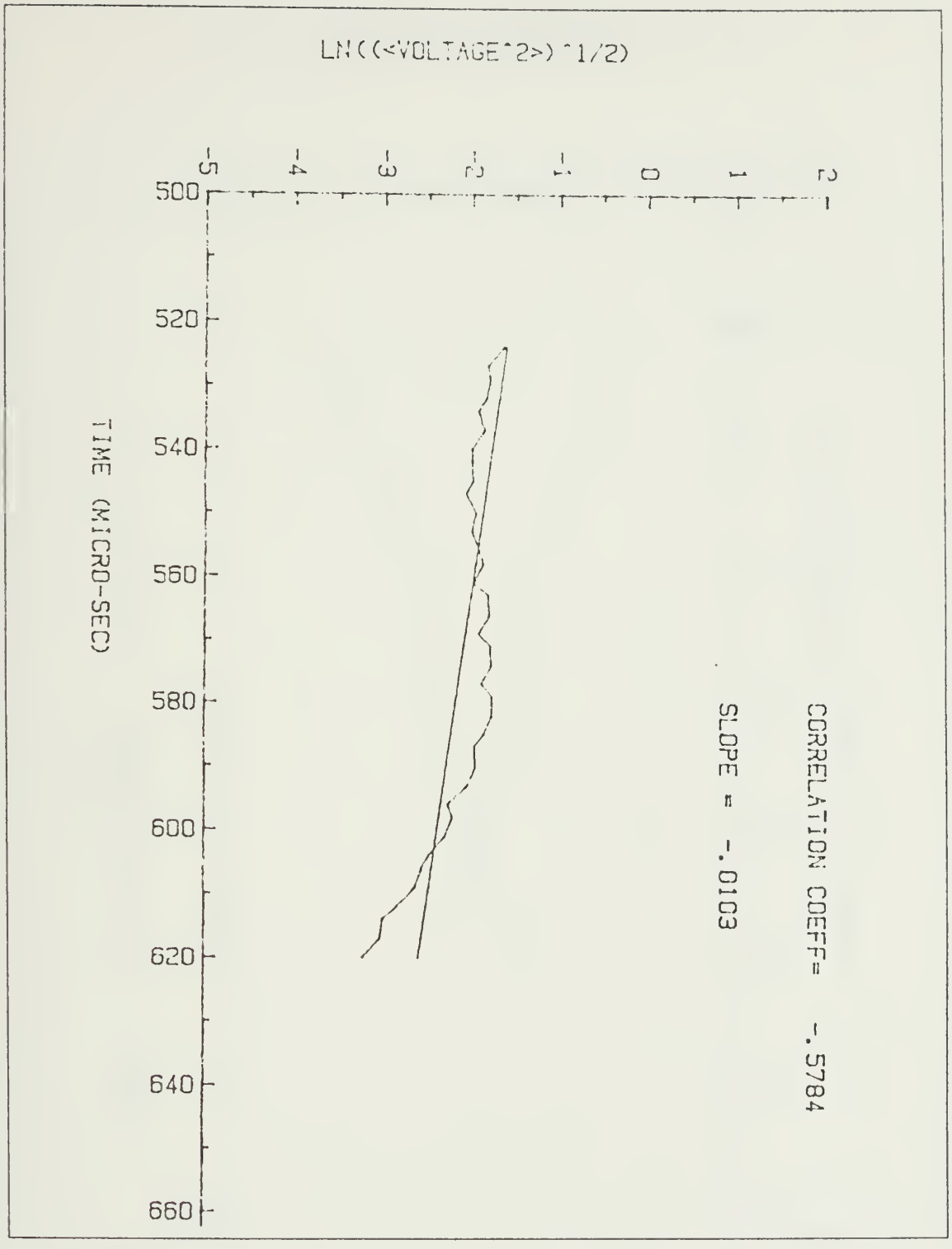

Figure D.10 Decay envelope for reflection from fine-sand/water interface, transducer was 30 cm above surface (data set 64).

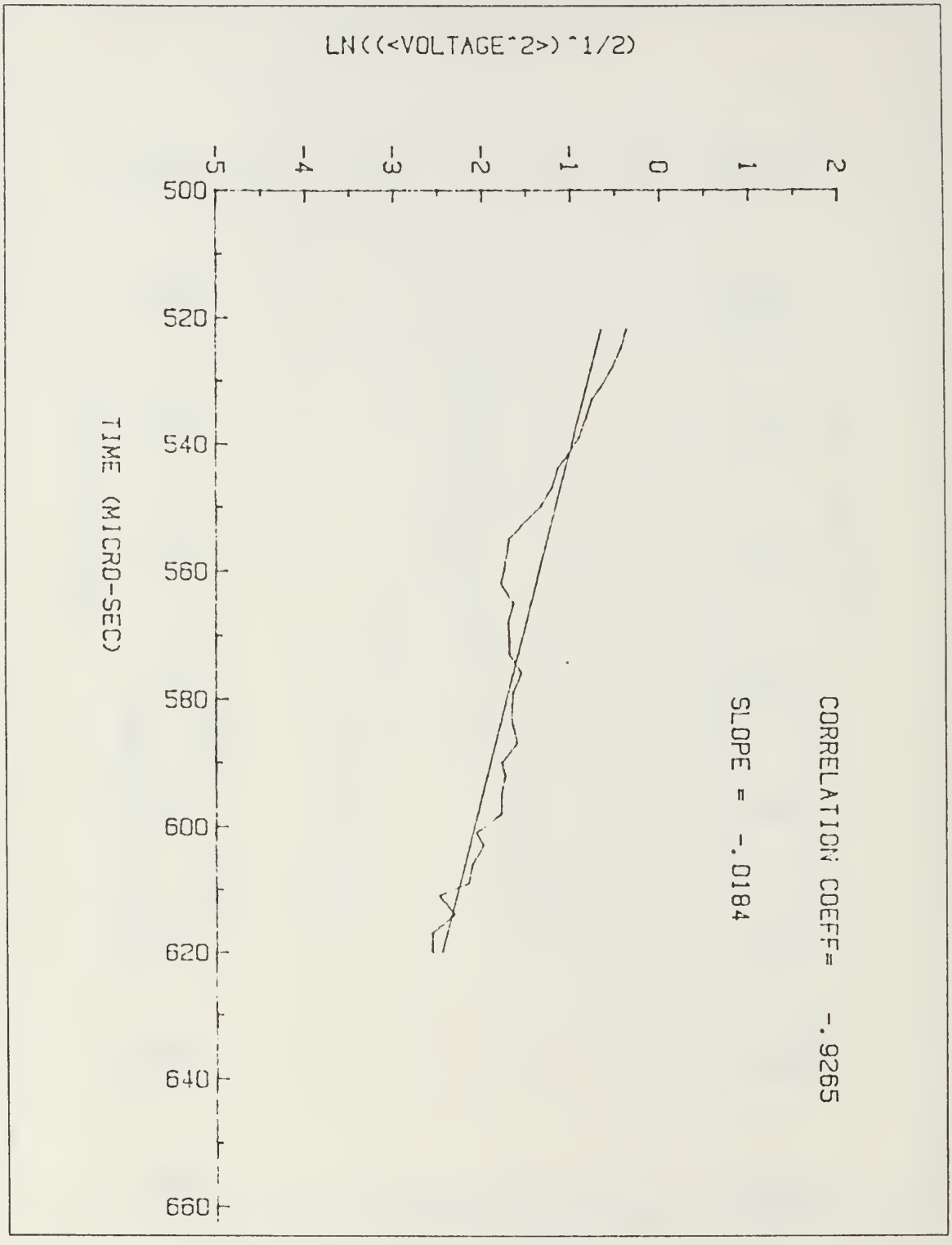

Figure D.11 Decay envelope resulted from the average of data set 55 and 56 for the fine-sand/water surface (data set DAT12).

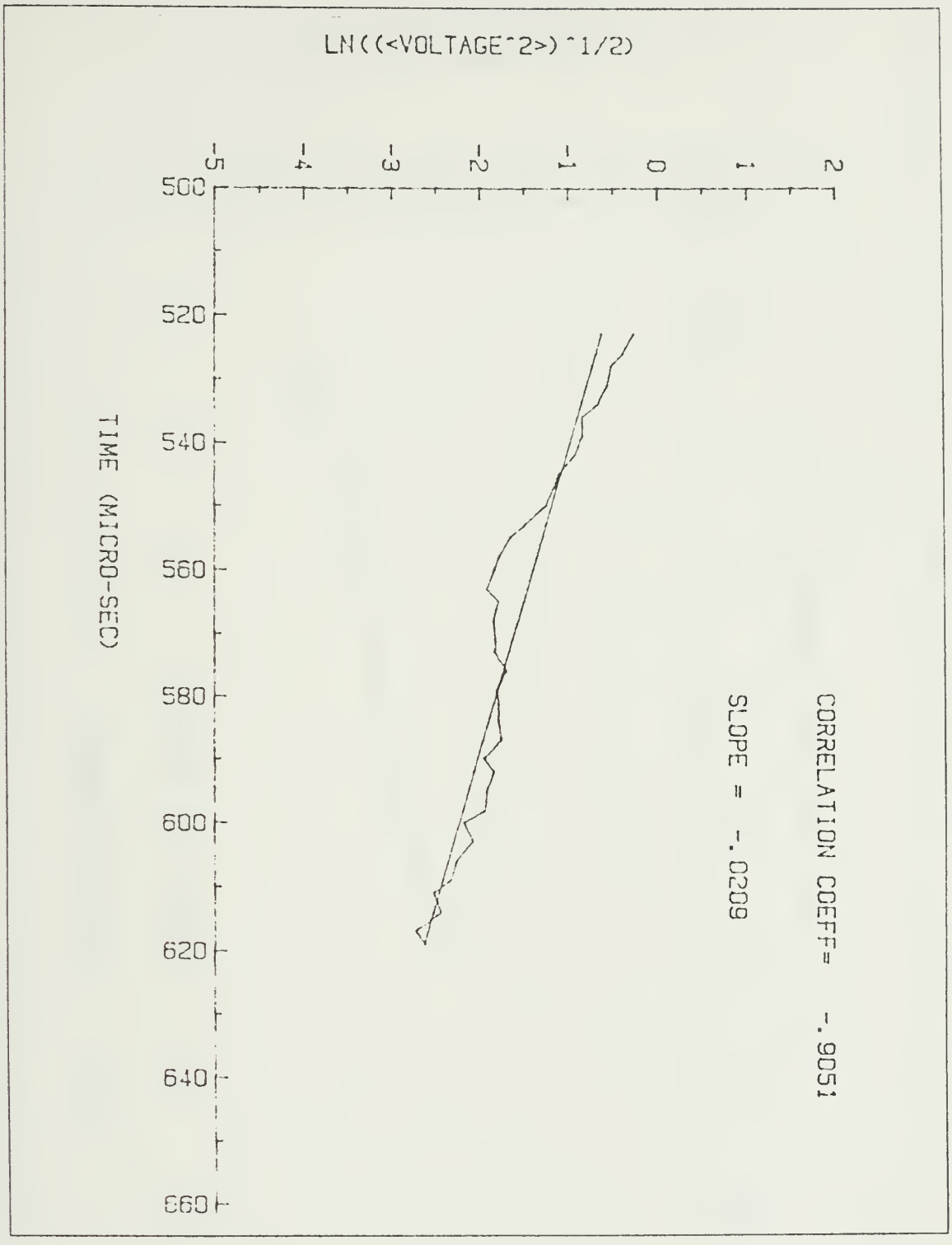

Figure D.12 Decay envelope resulted from the average from data set 55 to 57 for the fine-sand/water surface (data set DAT13).

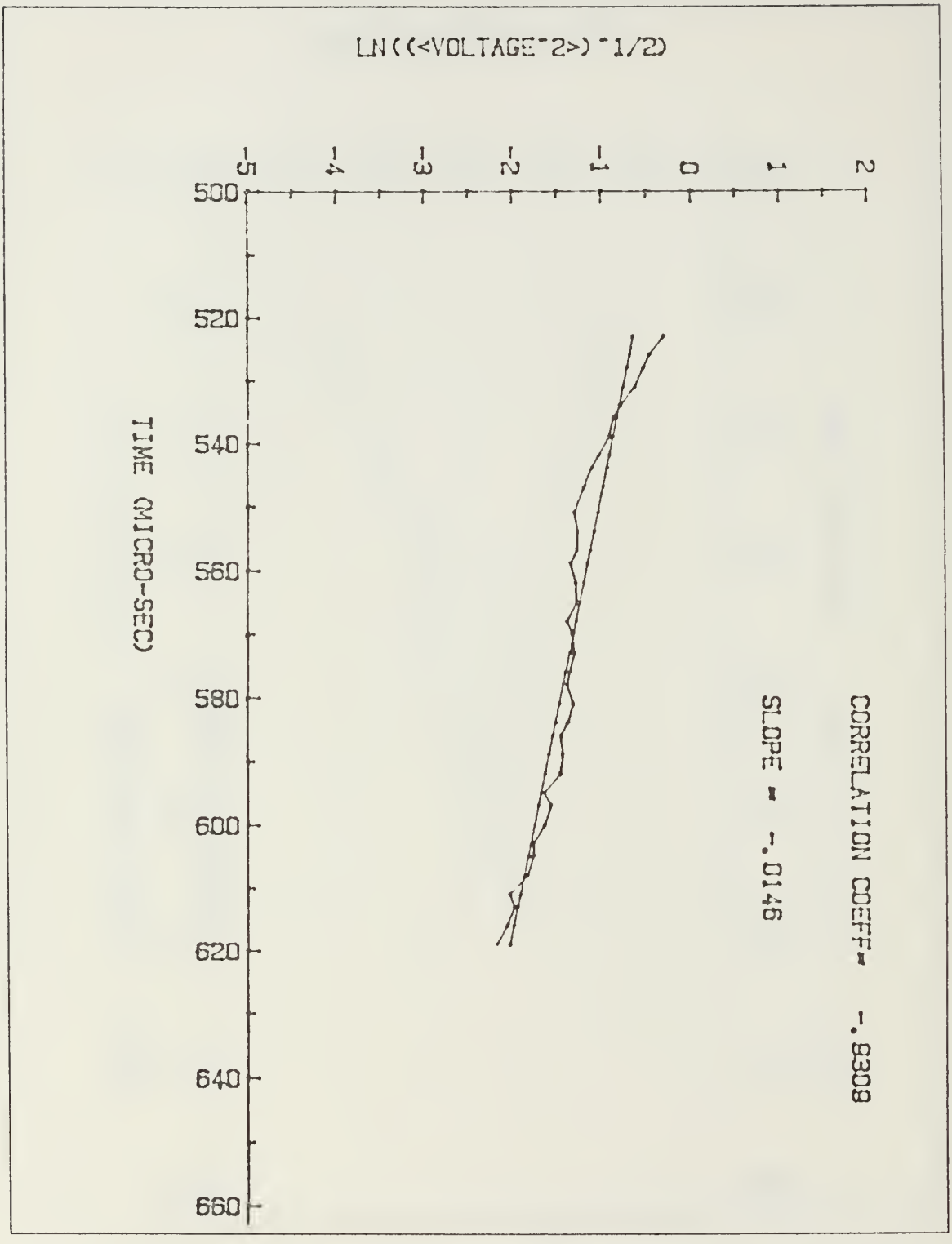

Figure D.13 Decay envelope resulted from the average from data set 55 to 58 for the fine-sand/water surface (data set DAT14).

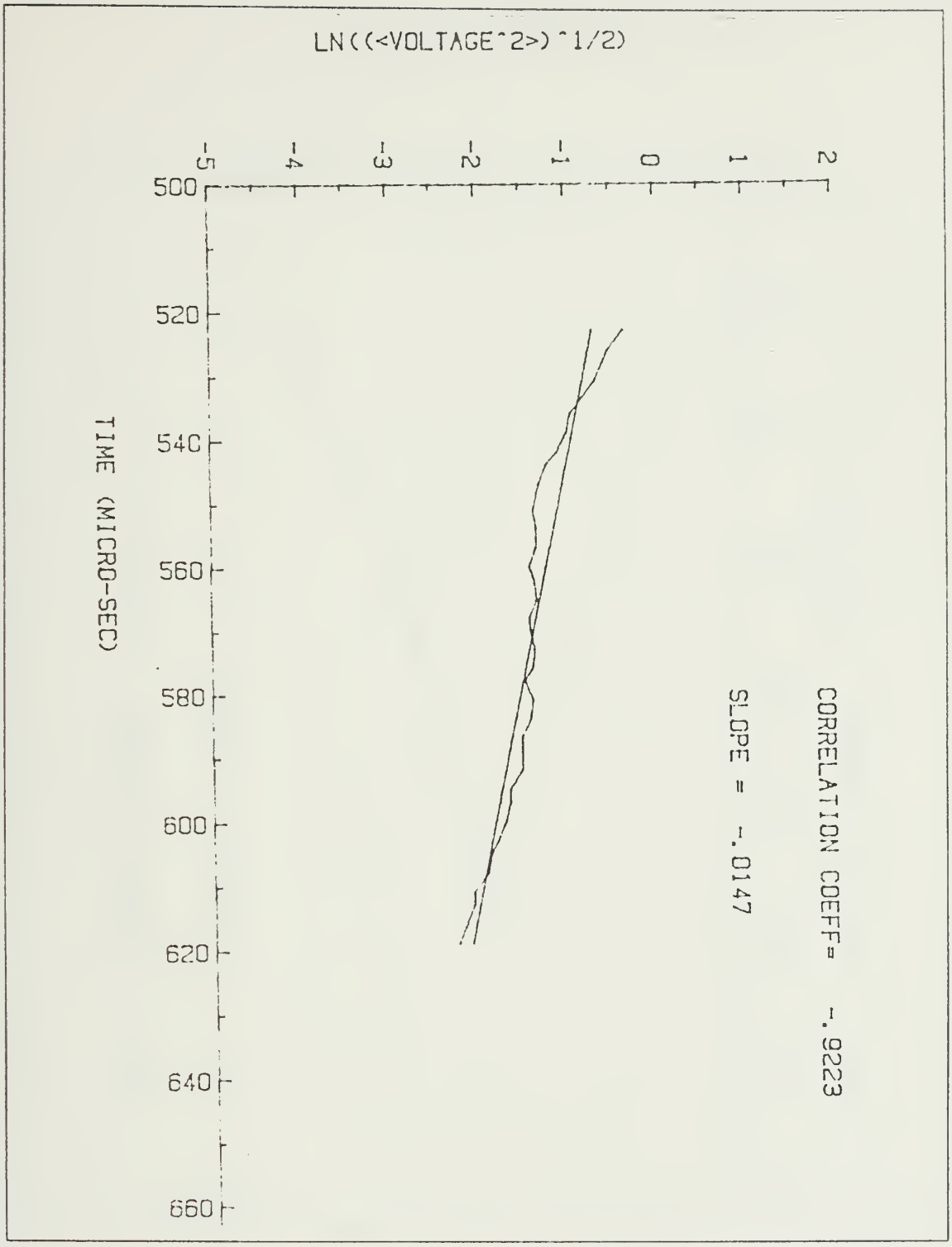

Figure D.14 Decay envelope resulted from the average from data set 55 to 59 for the fine-sand/water surface (data set DAT15).

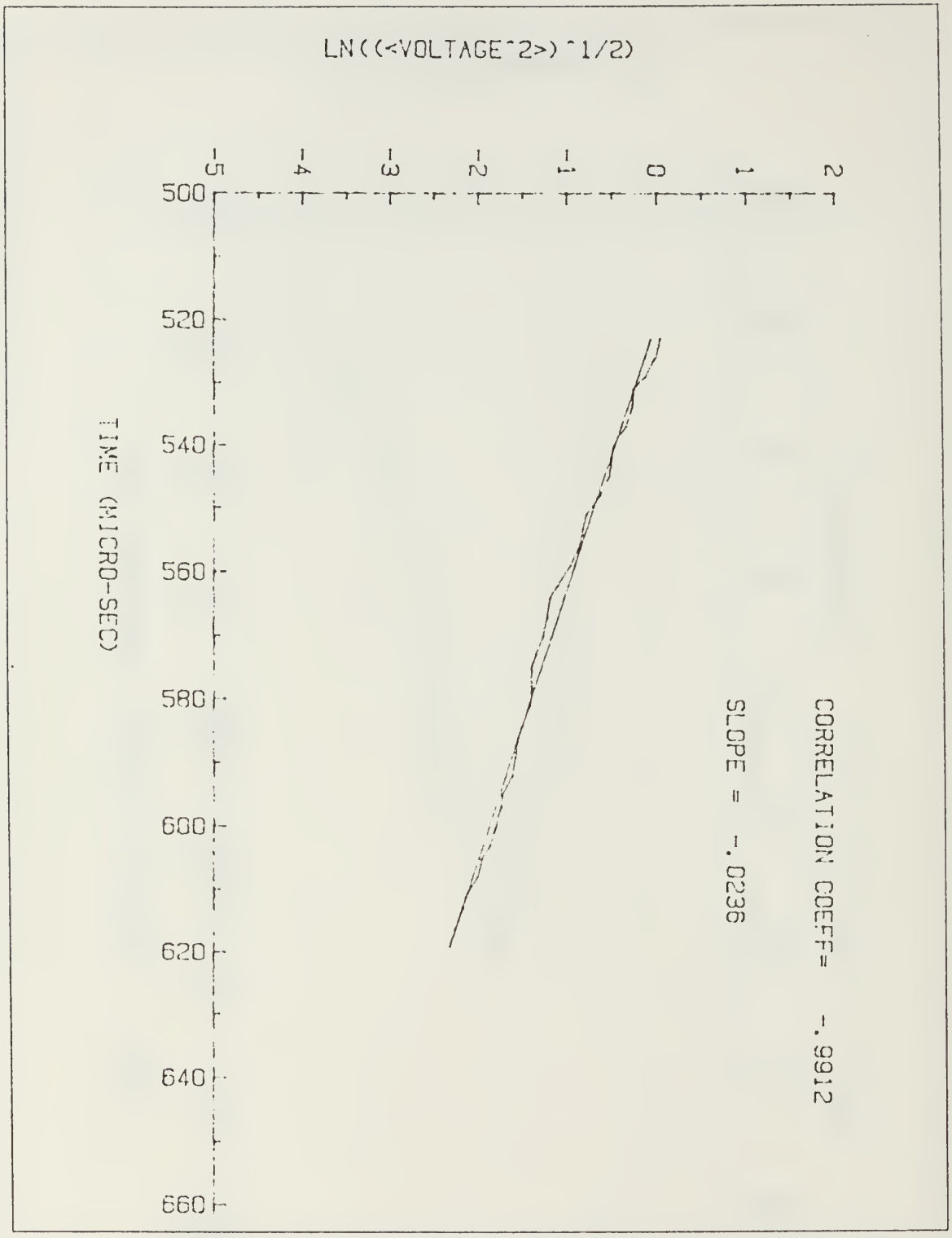

Figure D.15 Decay envelope resulted from the average from data set 55 to 60 for the fine-sand/water surface (data set DAT16).

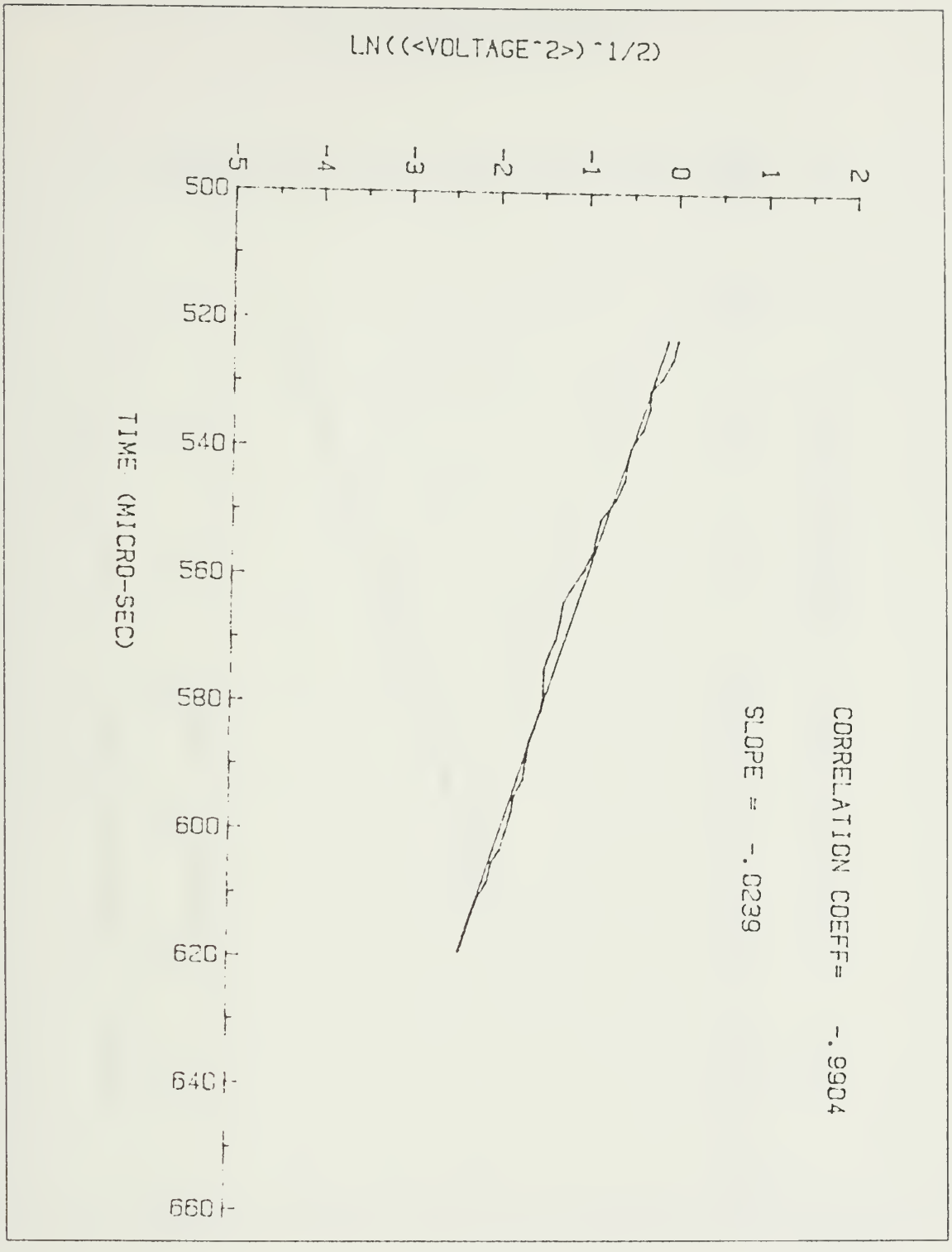

Figure D.16 Decay envelope resulted from the average from data set 55 to 61 for the fine-sand/water surface (data set DAT17).

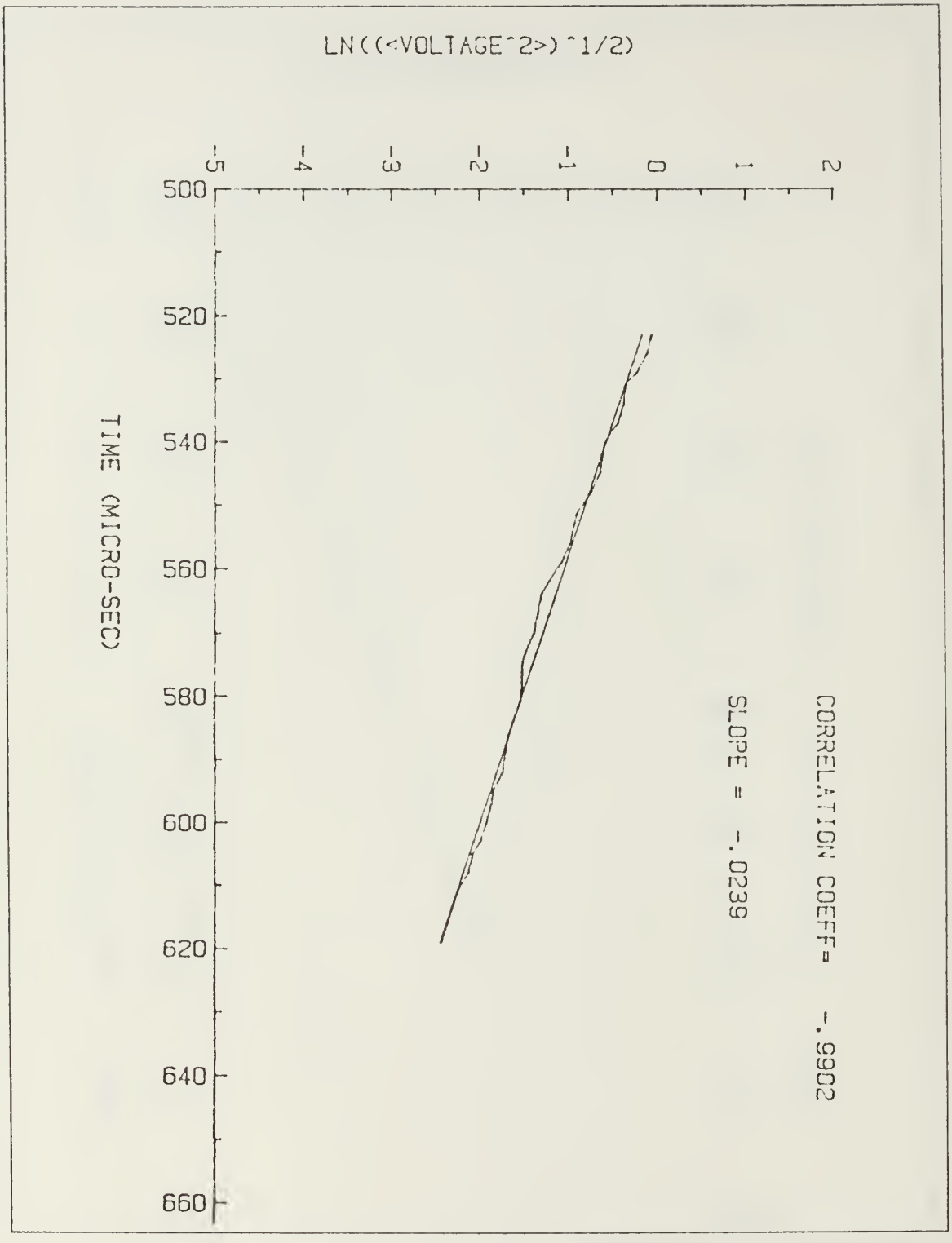

Figure D.17 Decay envelope resulted from the average from data set 55 to 62 for the fine-sand/water surface (data set DAT18).

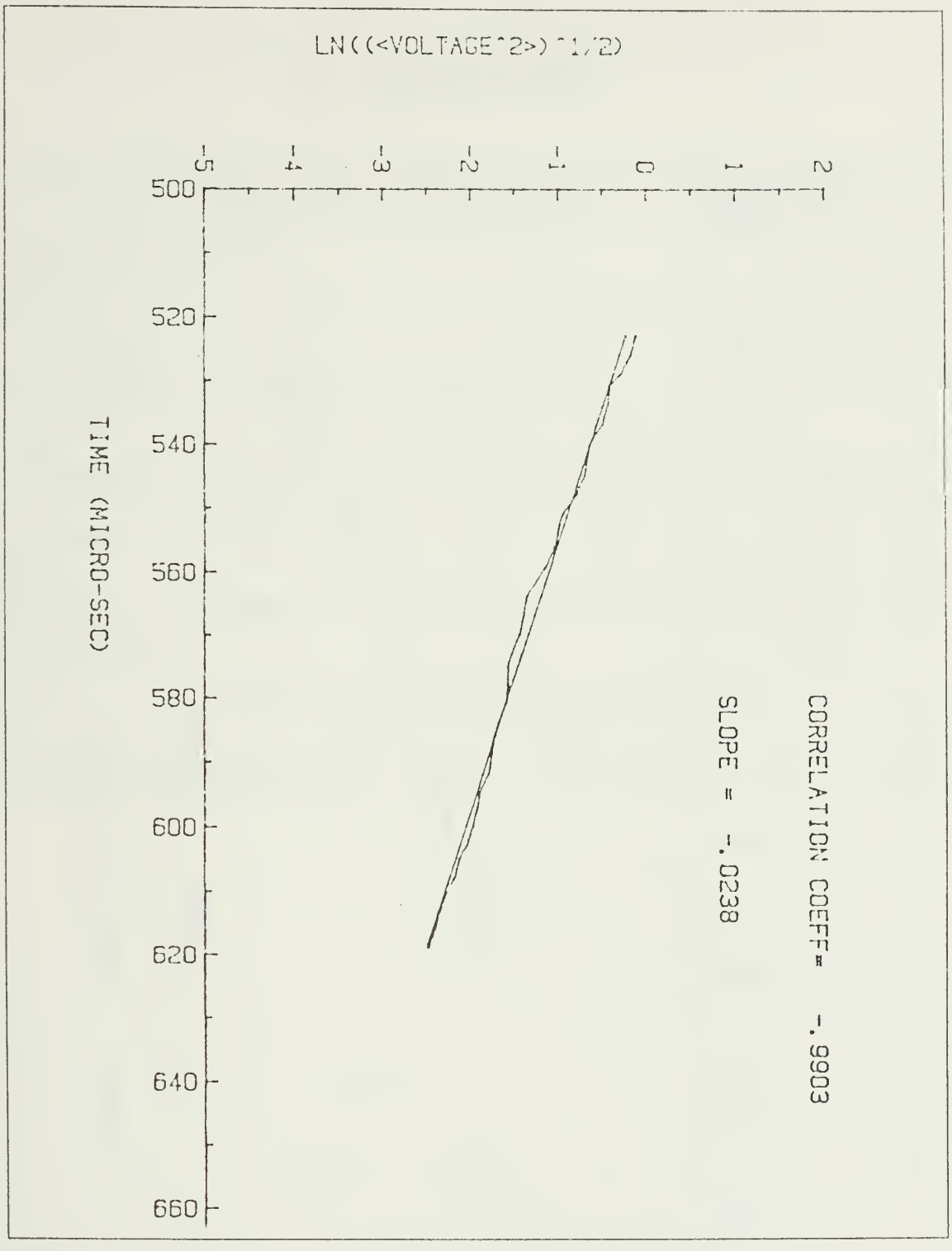

Figure D.18 Decay envelope resulted from the average from data set 55 to 63 for the fine-sand/water surface (data set DAT19).

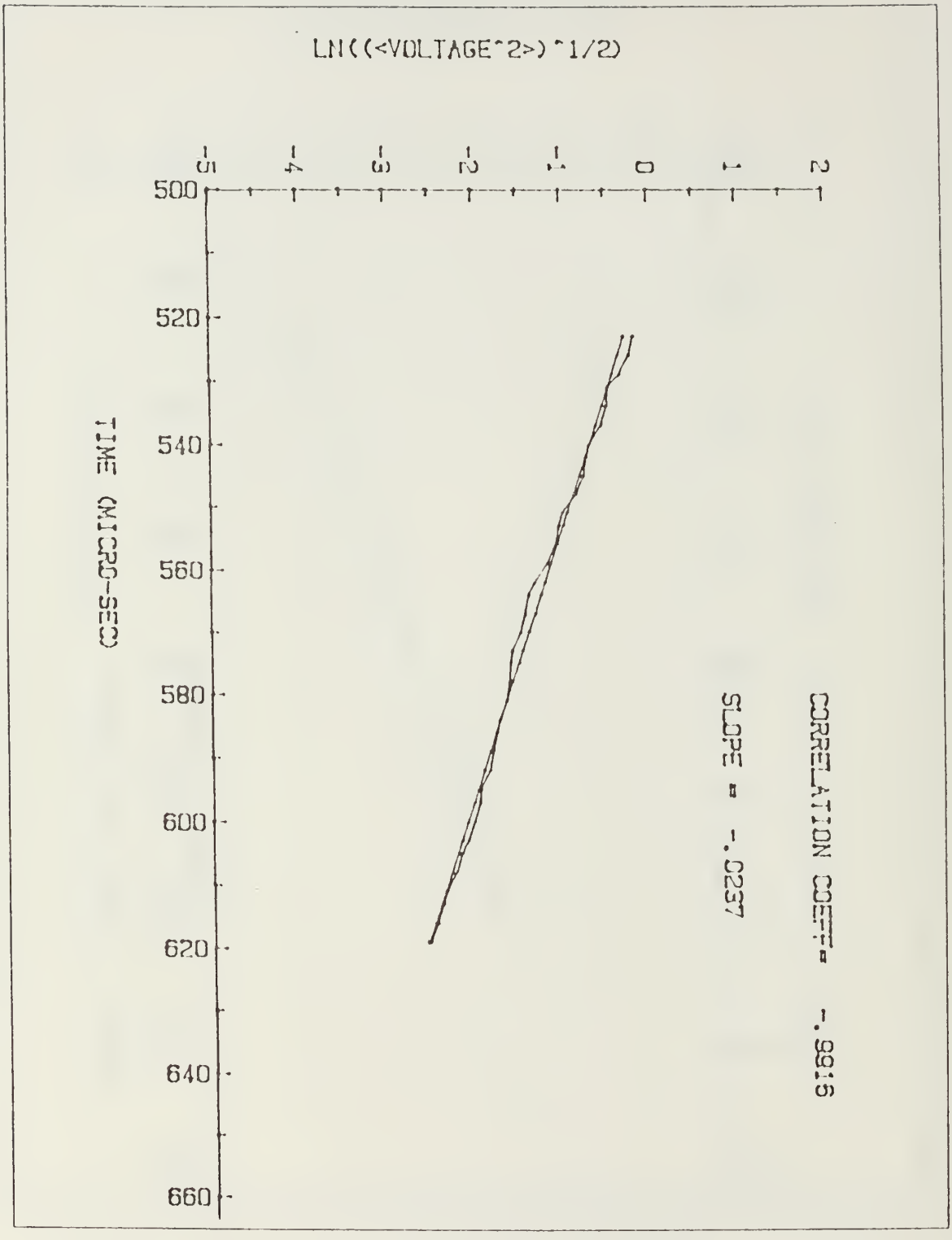

Figure D.19 Decay envelope resulted from the average from data set 55 to 64 for the aggregate/water surface (data set DAT20).

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